

# **Measuring Hubble's Constant with the Inverse Distance Ladder**

**Ed Macaulay**  
**[www.ed-macaulay.com](http://www.ed-macaulay.com)**  
**[edward.macaulay@gmail.com](mailto:edward.macaulay@gmail.com)**

# Inverse Distance Ladder

MNRAS 000, 1–14 (2019)

Preprint 29 May 2019

Compiled using MNRAS L<sup>A</sup>T<sub>E</sub>X style file v3.0

## First Cosmological Results using Type Ia Supernovae from the Dark Energy Survey: Measurement of the Hubble constant

E. Macaulay<sup>1</sup>\*, R. C. Nichol,<sup>1</sup> D. Bacon,<sup>1</sup> D. Brout,<sup>2</sup> T. M. Davis,<sup>3</sup> B. Zhang,<sup>4,5</sup> B. A. Bassett,<sup>6,7</sup> D. Scolnic,<sup>8</sup> A. Möller,<sup>4,5</sup> C. B. D'Andrea,<sup>2</sup> S. R. Hinton,<sup>3</sup> R. Kessler,<sup>9,8</sup> A. G. Kim,<sup>10</sup> J. Lasker,<sup>9,8</sup> C. Lidman,<sup>5</sup> M. Sako,<sup>2</sup> M. Smith,<sup>11</sup> M. Sullivan,<sup>11</sup> T. M. C. Abbott,<sup>12</sup> S. Allam,<sup>13</sup> J. Annis,<sup>13</sup> J. Asorey,<sup>14</sup> S. Avila,<sup>1</sup> K. Bechtol,<sup>15</sup> D. Brooks,<sup>16</sup> P. Brown,<sup>17</sup> D. L. Burke,<sup>18,19</sup> J. Calcinò,<sup>3</sup> A. Carnero Rosell,<sup>20,21</sup> D. Carollo,<sup>22</sup> M. Carrasco Kind,<sup>23,24</sup> J. Carretero,<sup>25</sup> F. J. Castander,<sup>26,27</sup> T. Collett,<sup>1</sup> M. Crocce,<sup>26,27</sup> C. E. Cunha,<sup>18</sup> L. N. da Costa,<sup>21,28</sup> C. Davis,<sup>18</sup> J. De Vicente,<sup>20</sup> H. T. Diehl,<sup>13</sup> P. Doel,<sup>16</sup> A. Drlica-Wagner,<sup>13,8</sup> T. F. Eifler,<sup>29,30</sup> J. Estrada,<sup>13</sup> A. E. Evrard,<sup>31,32</sup> A. V. Filippenko,<sup>33,34</sup> D. A. Finley,<sup>13</sup> B. Flaugher,<sup>13</sup> R. J. Foley,<sup>35</sup> P. Fosalba,<sup>26,27</sup> J. Frieman,<sup>13,8</sup> L. Galbany,<sup>36</sup> J. García-Bellido,<sup>37</sup> E. Gaztanaga,<sup>26,27</sup> K. Glazebrook,<sup>38</sup> S. González-Gaitán,<sup>39</sup> D. Gruen,<sup>18,19</sup> R. A. Gruendl,<sup>23,24</sup> J. Gschwend,<sup>21,28</sup> G. Gutierrez,<sup>13</sup> W. G. Hartley,<sup>16,40</sup> D. L. Hollowood,<sup>35</sup> K. Honscheid,<sup>41,42</sup> J. K. Hoormann,<sup>3</sup> B. Hoyle,<sup>43,44</sup> D. Huterer,<sup>32</sup> B. Jain,<sup>2</sup> D. J. James,<sup>45</sup> T. Jeltema,<sup>35</sup> E. Kasai,<sup>46,7</sup> E. Krause,<sup>29</sup> K. Kuehn,<sup>47</sup> N. Kuropatkin,<sup>13</sup> O. Lahav,<sup>16</sup> G. F. Lewis,<sup>48</sup> T. S. Li,<sup>13,8</sup> M. Lima,<sup>49,21</sup> H. Lin,<sup>13</sup> M. A. G. Maia,<sup>21,28</sup> J. L. Marshall,<sup>17</sup> P. Martini,<sup>41,50</sup> R. Miquel,<sup>51,25</sup> P. Nugent,<sup>10</sup> A. Palmese,<sup>13</sup> Y.-C. Pan,<sup>52,53</sup> A. A. Plazas,<sup>30</sup> A. K. Romer,<sup>54</sup> A. Roodman,<sup>18,19</sup> E. Sanchez,<sup>20</sup> V. Scarpine,<sup>13</sup> R. Schindler,<sup>19</sup> M. Schubnell,<sup>32</sup> S. Serrano,<sup>26,27</sup> I. Sevilla-Noarbe,<sup>20</sup> R. Sharp,<sup>5</sup> M. Soares-Santos,<sup>55</sup> F. Sobreira,<sup>56,21</sup> N. E. Sommer,<sup>4,5</sup> E. Suchyta,<sup>57</sup> E. Swann,<sup>1</sup> M. E. C. Swanson,<sup>24</sup> G. Tarle,<sup>32</sup> D. Thomas,<sup>1</sup> R. C. Thomas,<sup>10</sup> B. E. Tucker,<sup>4,5</sup> S. A. Uddin,<sup>58</sup> V. Vikram,<sup>59</sup> A. R. Walker,<sup>12</sup> and P. Wiseman<sup>11</sup>

(DES Collaboration)

Author affiliations are shown in Appendix B

Accepted 2019 April 03. Received 2019 April 02; in original form 2018 November 08

### ABSTRACT

We present an improved measurement of the Hubble constant ( $H_0$ ) using the ‘inverse distance ladder’ method, which adds the information from 207 Type Ia supernovae (SNe Ia) from the Dark Energy Survey (DES) at redshift  $0.018 < z < 0.85$  to existing distance measurements of 122 low redshift ( $z < 0.07$ ) SNe Ia (Low- $z$ ) and measurements of Baryon Acoustic Oscillations (BAOs). Whereas traditional measurements of  $H_0$  with SNe Ia use a distance ladder of parallax and Cepheid variable stars, the inverse distance ladder relies on absolute distance measurements from the BAOs to calibrate the intrinsic magnitude of the SNe Ia. We find  $H_0 = 67.8 \pm 1.3 \text{ km s}^{-1} \text{ Mpc}^{-1}$  (statistical and systematic uncertainties, 68% confidence). Our measurement makes minimal assumptions about the underlying cosmological model, and our analysis was blinded to reduce confirmation bias. We examine possible systematic uncertainties and all are below the statistical uncertainties. Our  $H_0$  value is consistent with estimates derived from the Cosmic Microwave Background assuming a  $\Lambda$ CDM universe (Planck Collaboration et al. 2018).

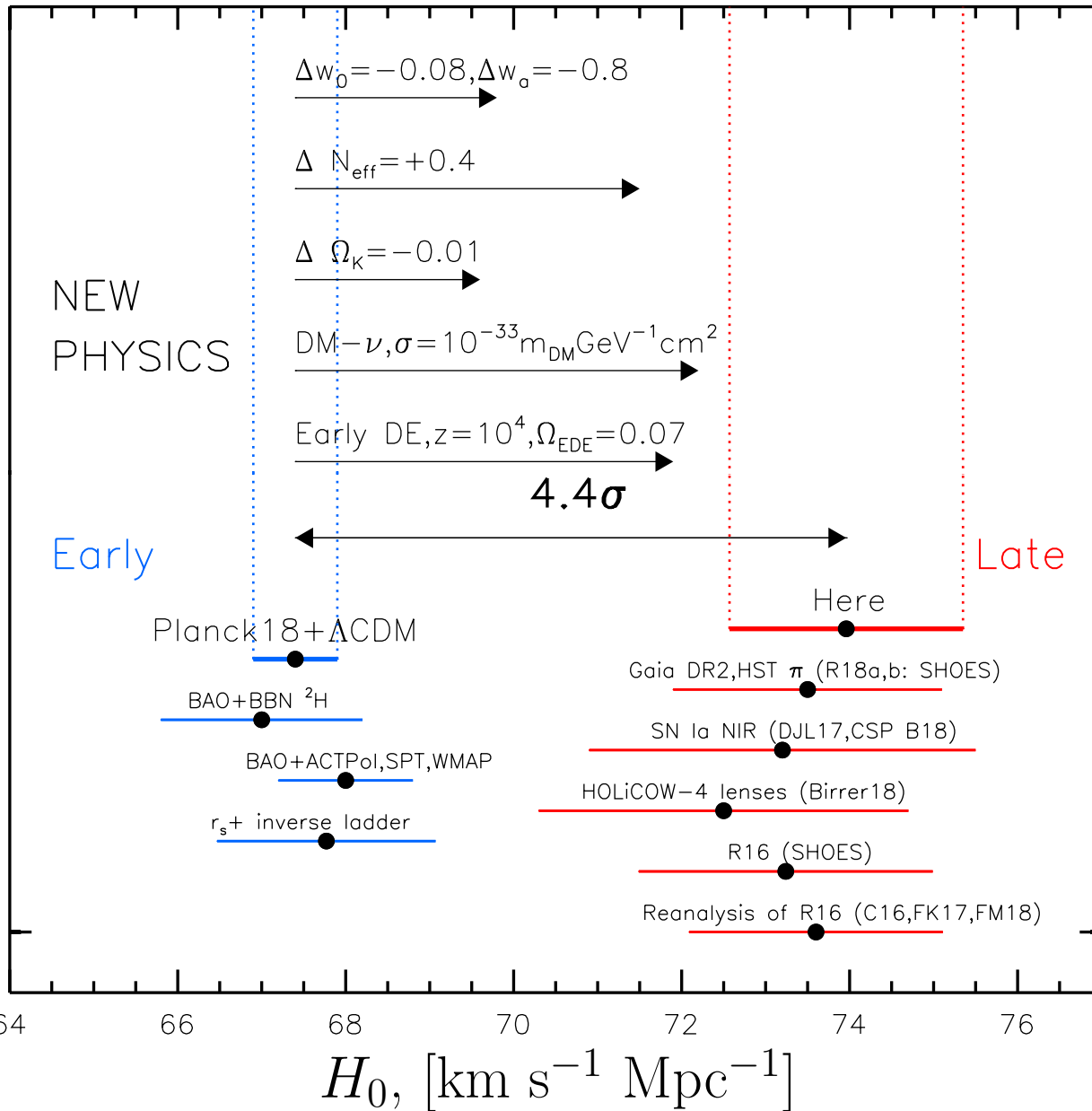
**Key words:** cosmology: observations – cosmology: cosmological parameters – cosmology: distance scale

© 2019 The Authors  
Reproduction permitted under the terms of the Creative Commons Attribution License (<http://creativecommons.org/licenses/by/4.0/>)

arXiv:1811.02376v2 [astro-ph.CO] 27 May 2019

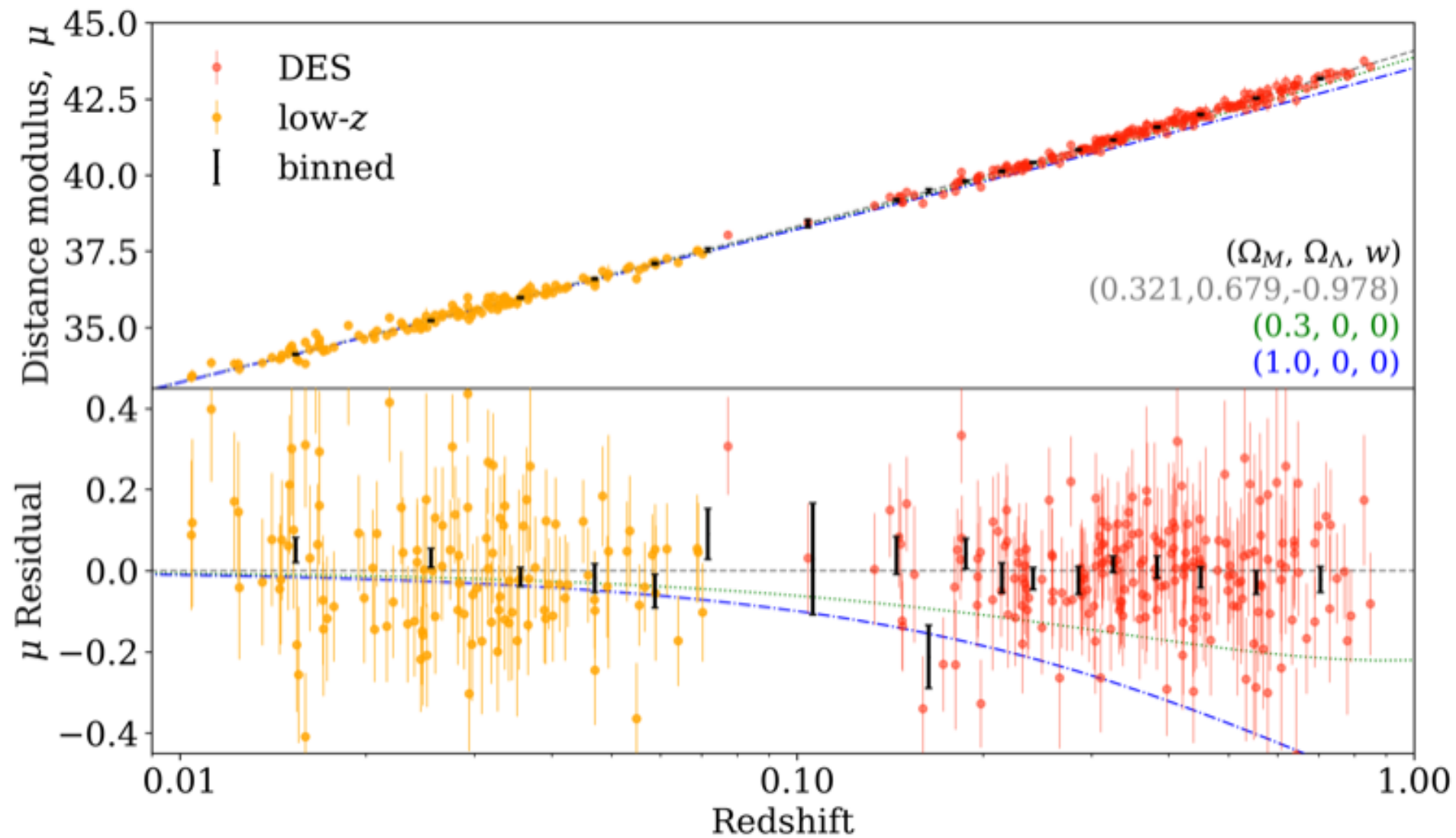
- Results from 3-year DES-SN sample in 2019
- Total of 329 spectroscopically observed SNe
- Blind analysis to reduce confirmation bias
- $H_0 = 67.8 \pm 1.3 \text{ km s}^{-1} \text{ Mpc}^{-1}$

# Overview of Tension



- **Difficult to reconcile results even observationally**

# DES 3-year SNe



# Supernova $H_0$ - $M_B$ Degeneracy

**Supernova  
Observations**

$$\mu = m_B^* - (M_B - \alpha X_1 + \beta C)$$


**Observed  
Measurements**

**Fitted  
Parameters**

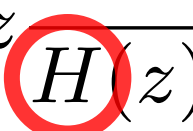
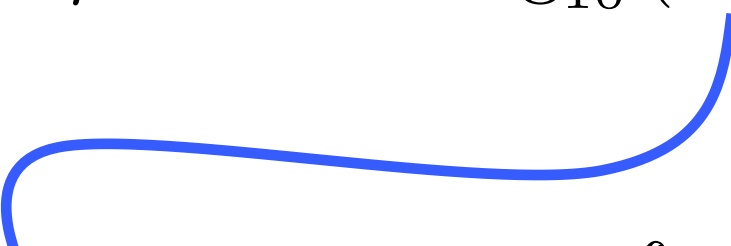
**Distance  
Modulus**

$$\mu = 25 + 5 \log_{10} (D_L)$$

**Degenerate**



**Luminosity  
Distance**

$$D_L = (1 + z_{\text{obs}}) \int dz \frac{c}{H(z)}$$


# Cosmographic Model

**Agnostic to physics of  
distance-redshift relation**

$$D_L = \frac{cz}{H_0} \left[ 1 + \frac{z}{2}(1 - q_0) - \frac{z^2}{6}(1 - q_0 - 3q_0^2 + j_0) \right]$$

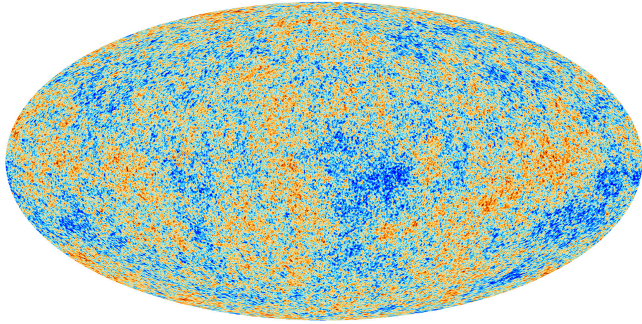
**'linear'**  
**Hubble's Law**

**Extra terms,  
describe expansion history**

**eg., Feeney et al (2018)  
arXiv: 1802.03404**

# Inverse Distance Ladder

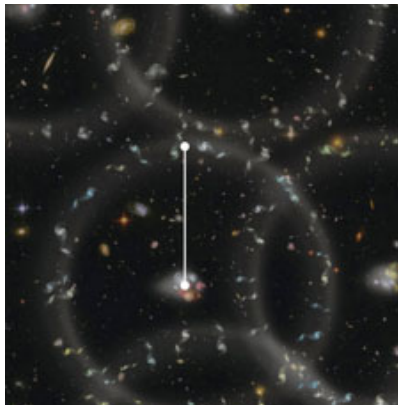
Planck



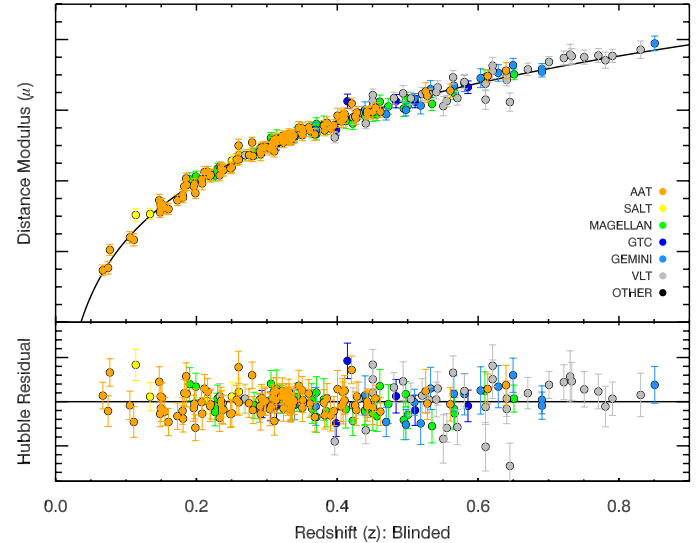
$$r_d = 147 \text{ Mpc}$$



BOSS



DES

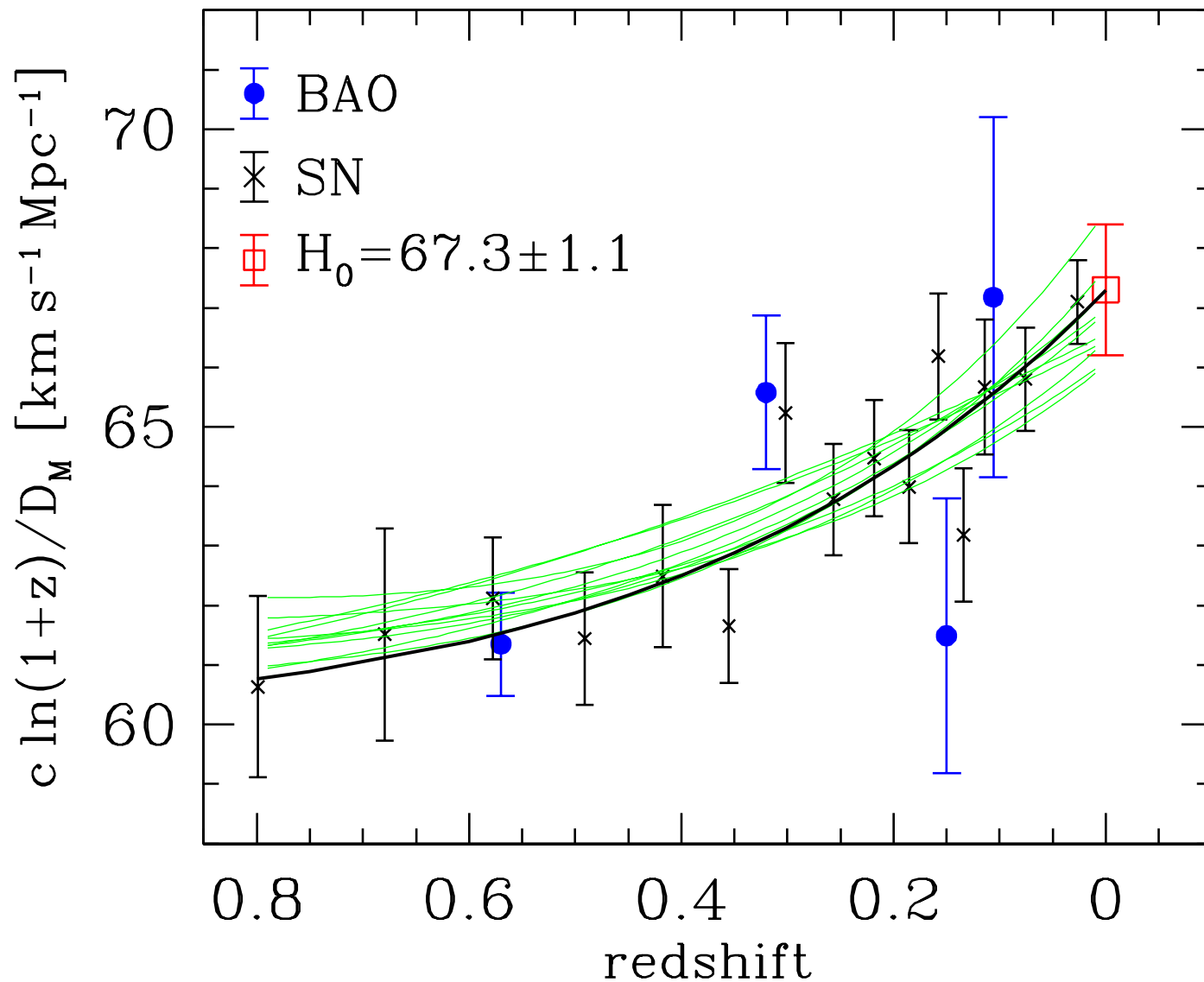


$D_L(z)$

$H_0$

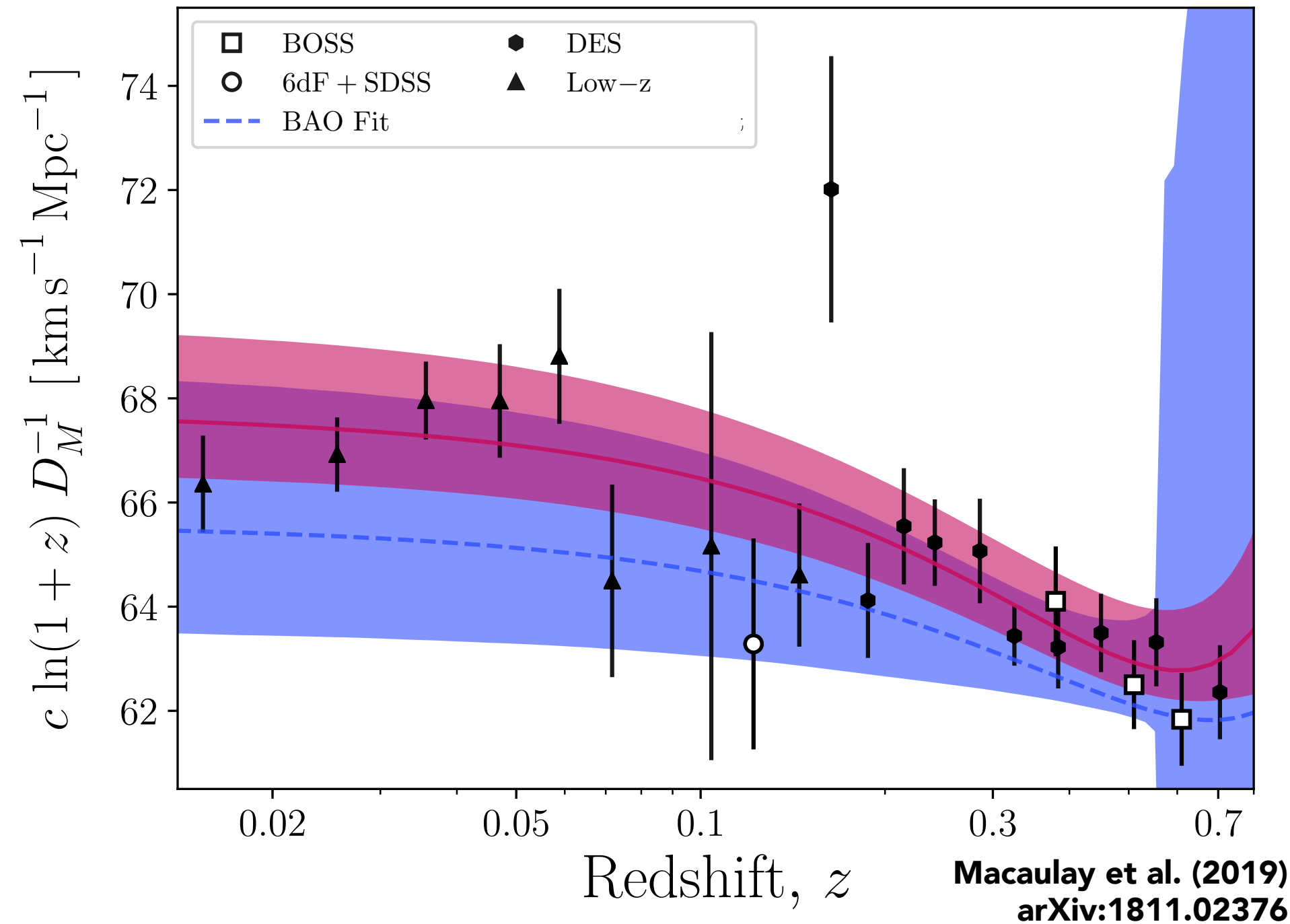
$D_M(z)$ ,  $D_H(z)$  or  $D_V(z)$

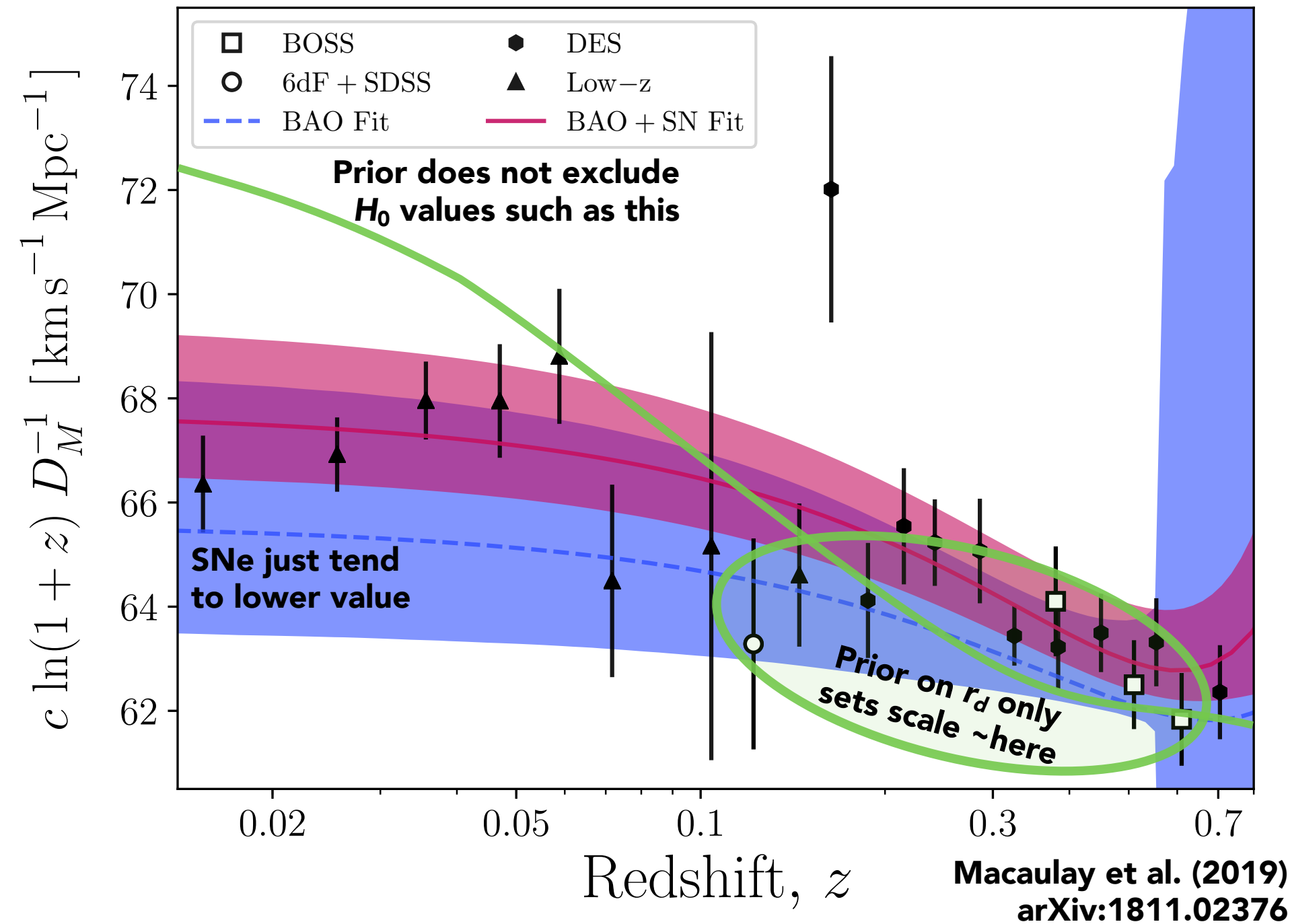
# Results with JLA



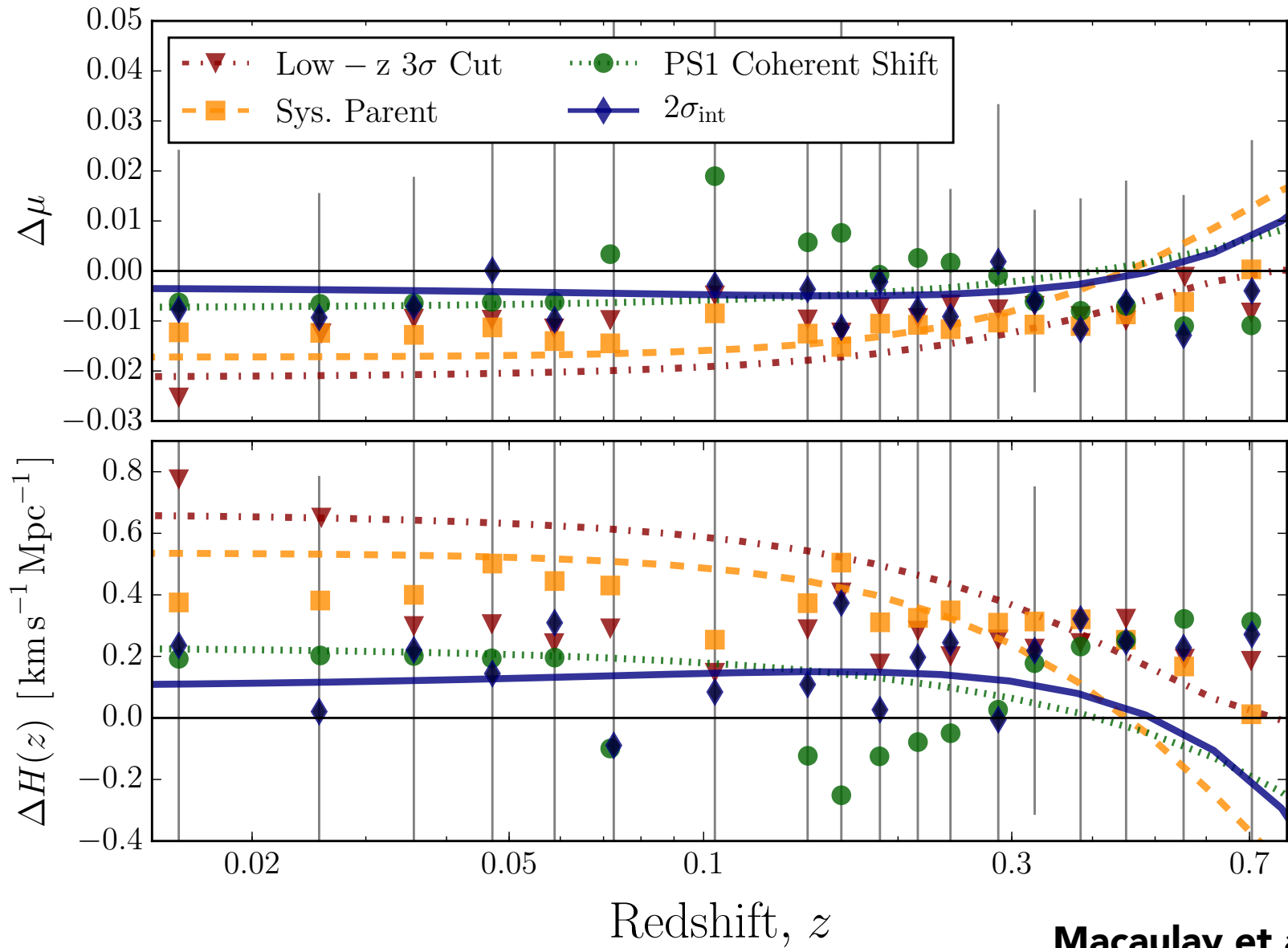
**Axis Converges  
to  $H_0$  as  $z \rightarrow 0$**



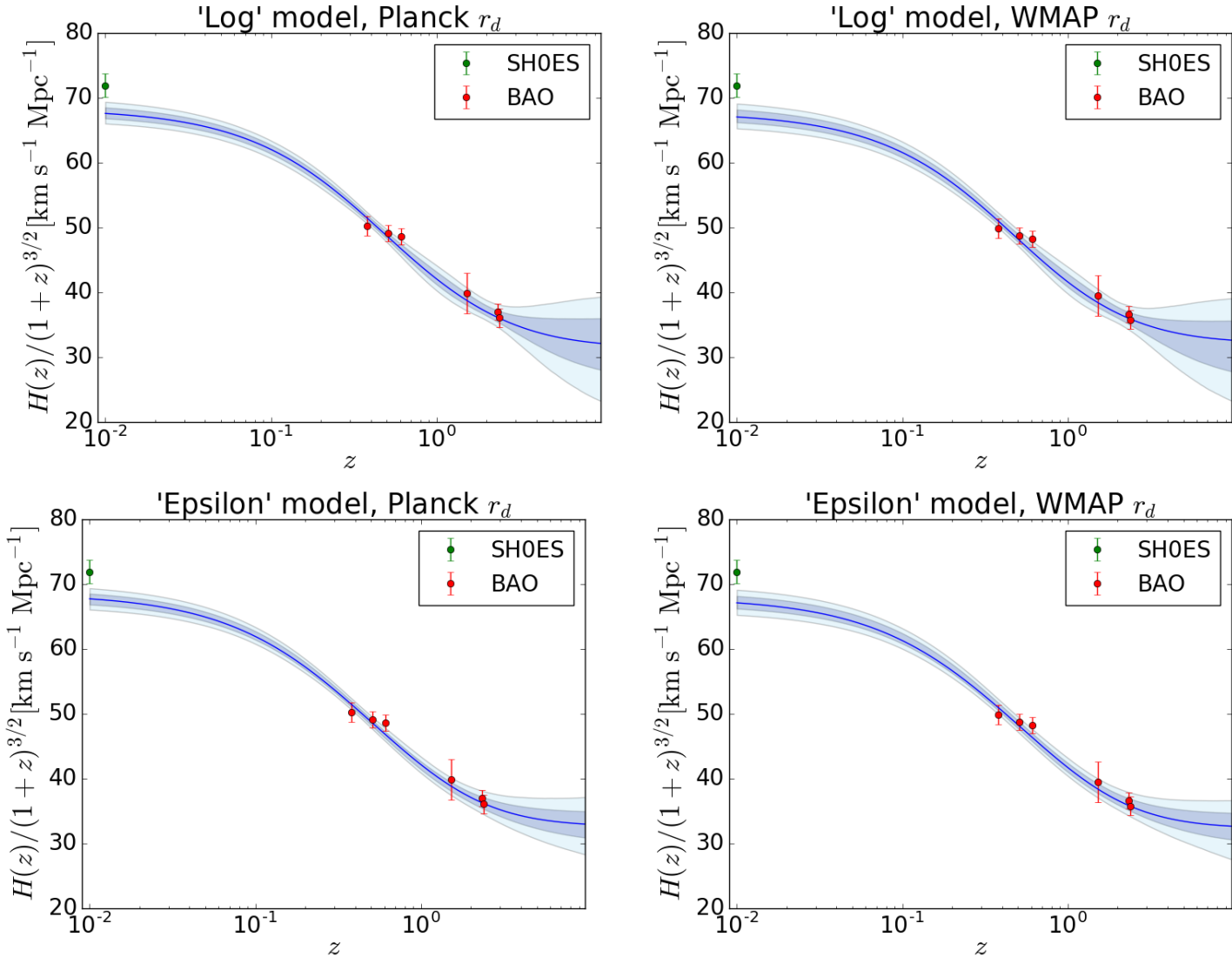




# Sensitivity to Systematics

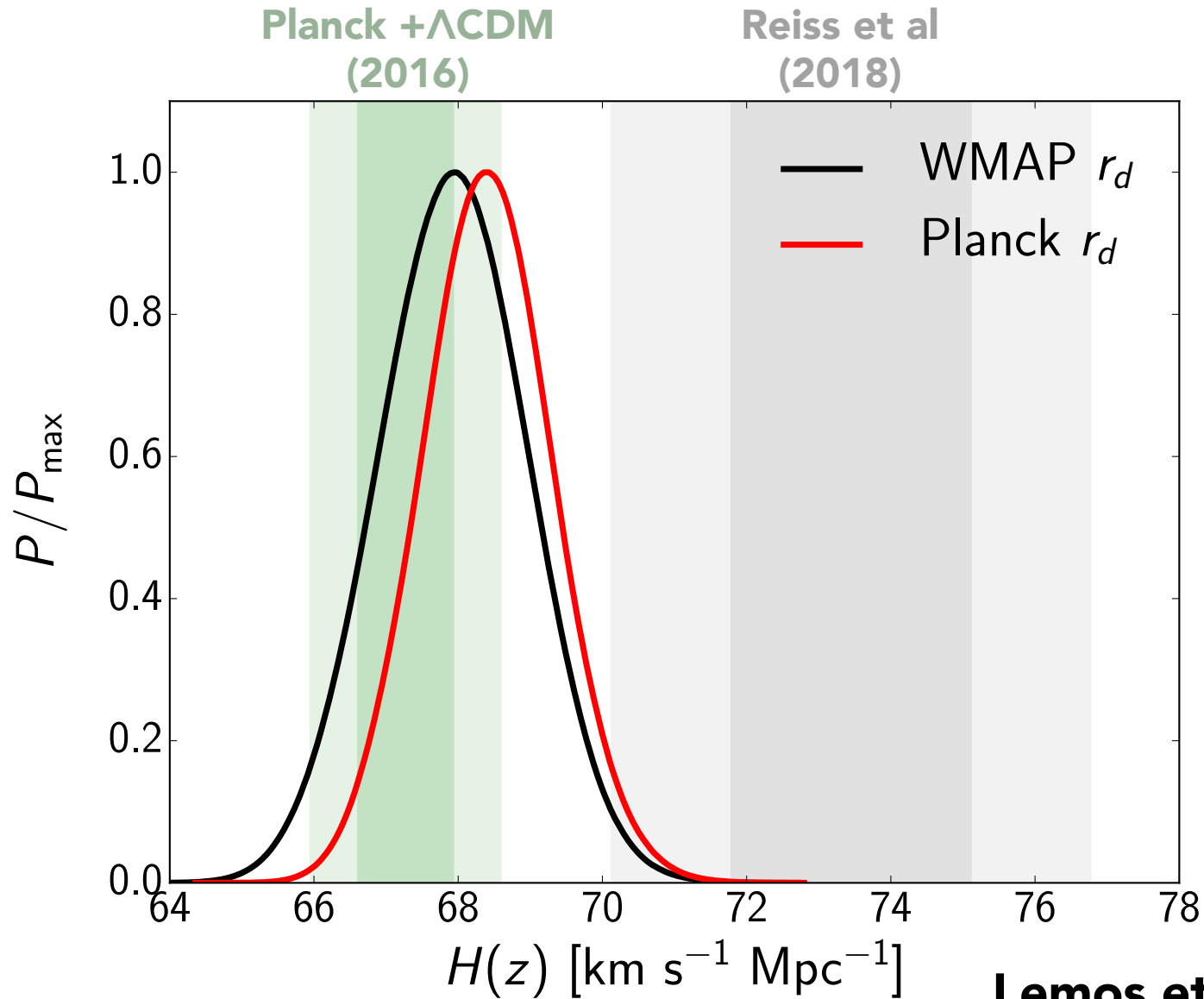


# Model & Prior Sensitivity



**Lemos et al. (2019)**  
**arXiv: 1806.06781**

# Model & Prior Sensitivity

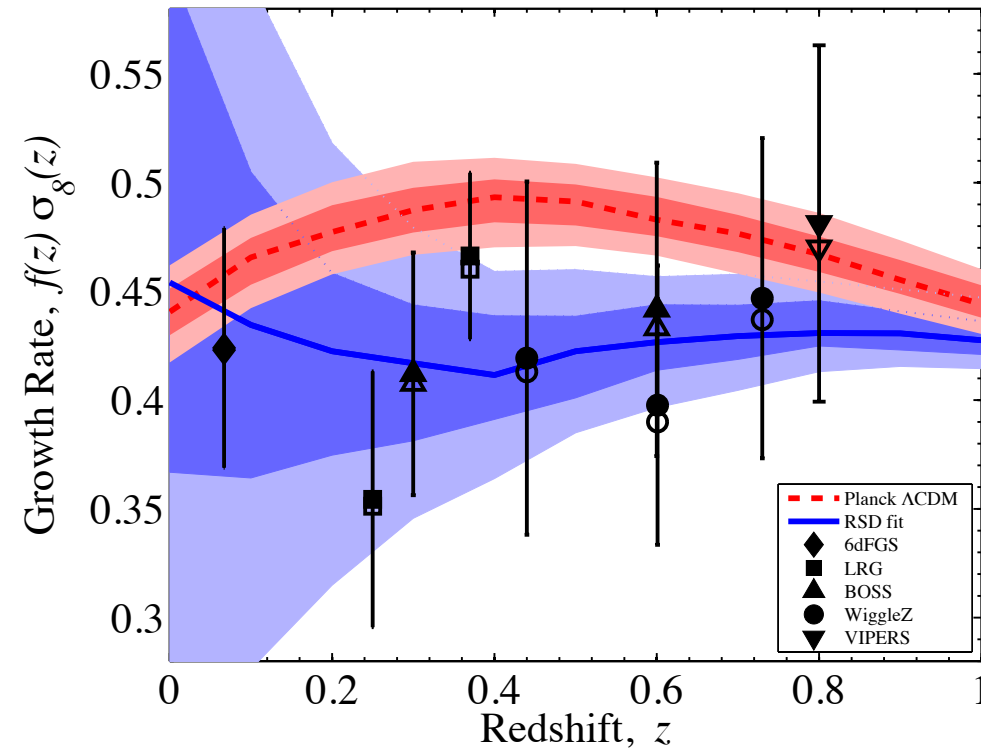


**Lemos et al. (2019)**  
**arXiv: 1806.06781**

# Take Home Points

- **Inverse Distance Ladder value of  $H_0$  consistent with Planck+ $\Lambda$ CDM**
- **CMB: the value of  $r_d$  is not sensitive to late-time cosmology**
- **Statistical & systematic uncertainties not enough to reconcile with Distance Ladder measurements**
- **Robust to distance-redshift model and Planck/WMAP**

# Speculation(?)



- **Difficult to reconcile observations with a single explanation.**
- **Several different observational effects?**
- **Are  $H_0$  and  $\sigma_8$  tensions related?**
- **Single theoretical explanation, or just different phenomena?**