

New Bounds on Macroscopic Scalar-Field  
Topological Defects from Non-Transient Signatures  
due to Environmental Dependence and  
Spatial Variations of the Fundamental Constants

Yevgeny Stadnik

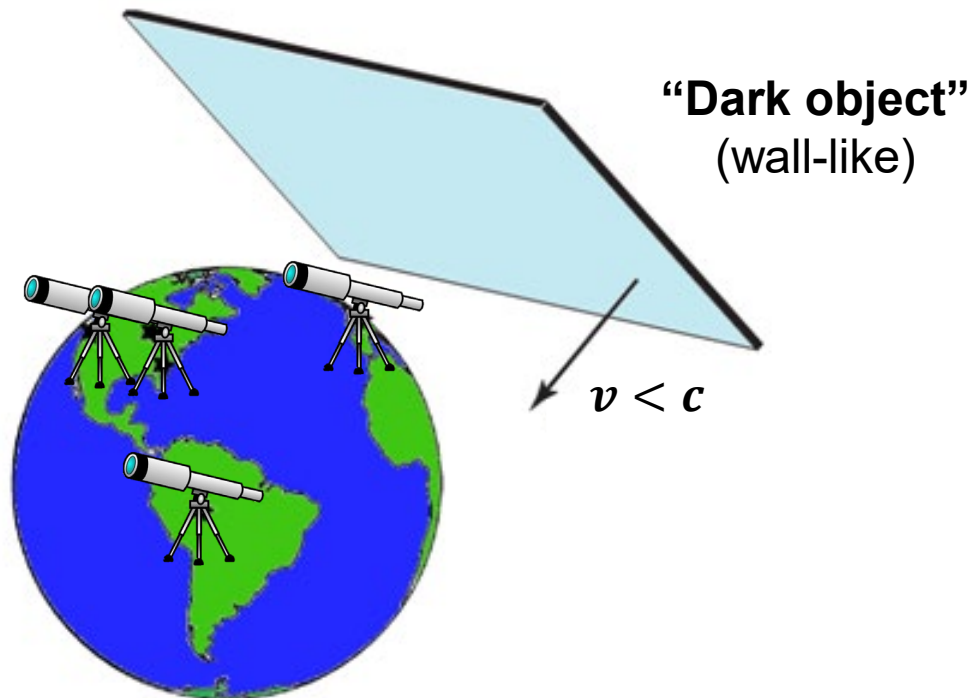
Kavli IPMU, University of Tokyo, Japan



16<sup>th</sup> Marcel Grossmann Meeting, July 2021

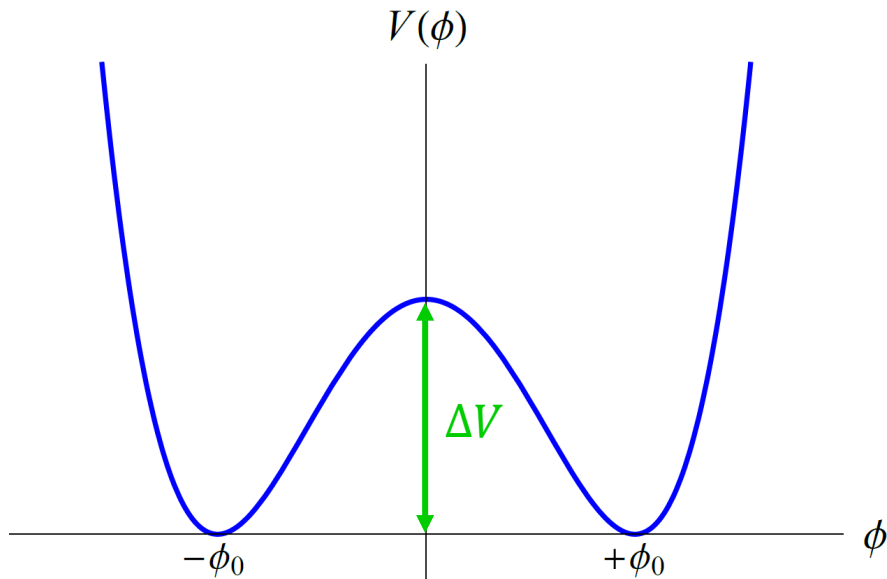
# Dark Objects

- Recent interest to search for possible transient signatures of macroscopic “**dark objects**” that might pass through Earth
- Basic idea: use *terrestrial networks of spatially-separated detectors* to search for *correlated signatures* of passing dark objects (similarly to GW searches)



# Topological Domain Walls

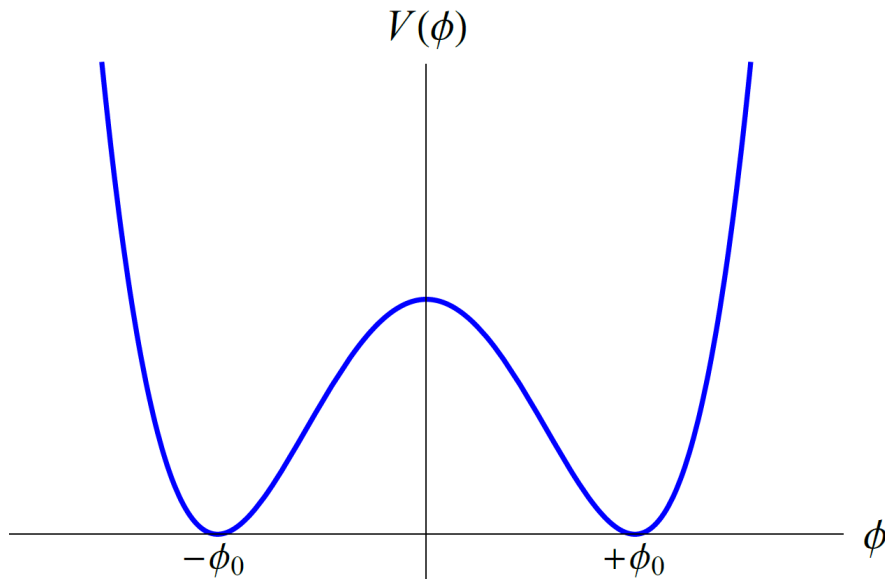
- Consider a real scalar field  $\varphi$  with potential  $V(\varphi) = \lambda(\varphi^2 - \varphi_0^2)^2/4$



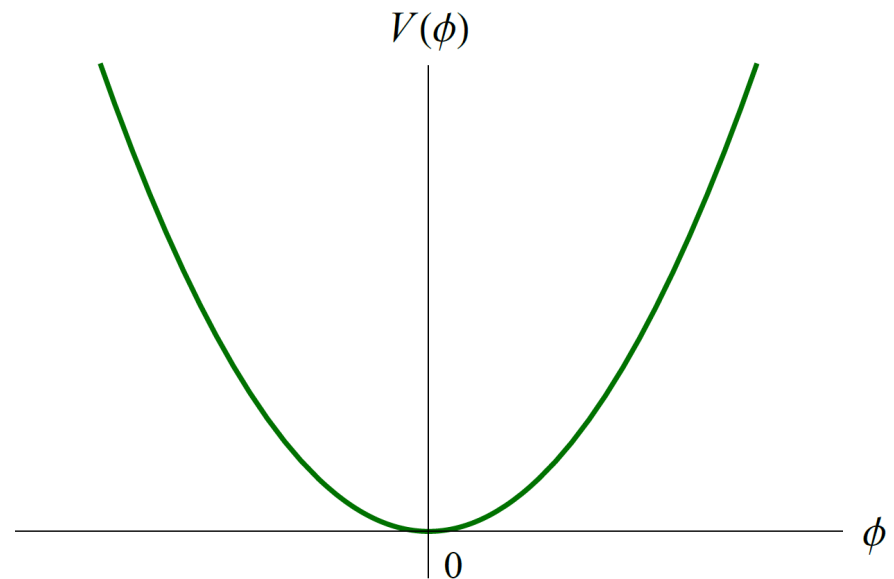
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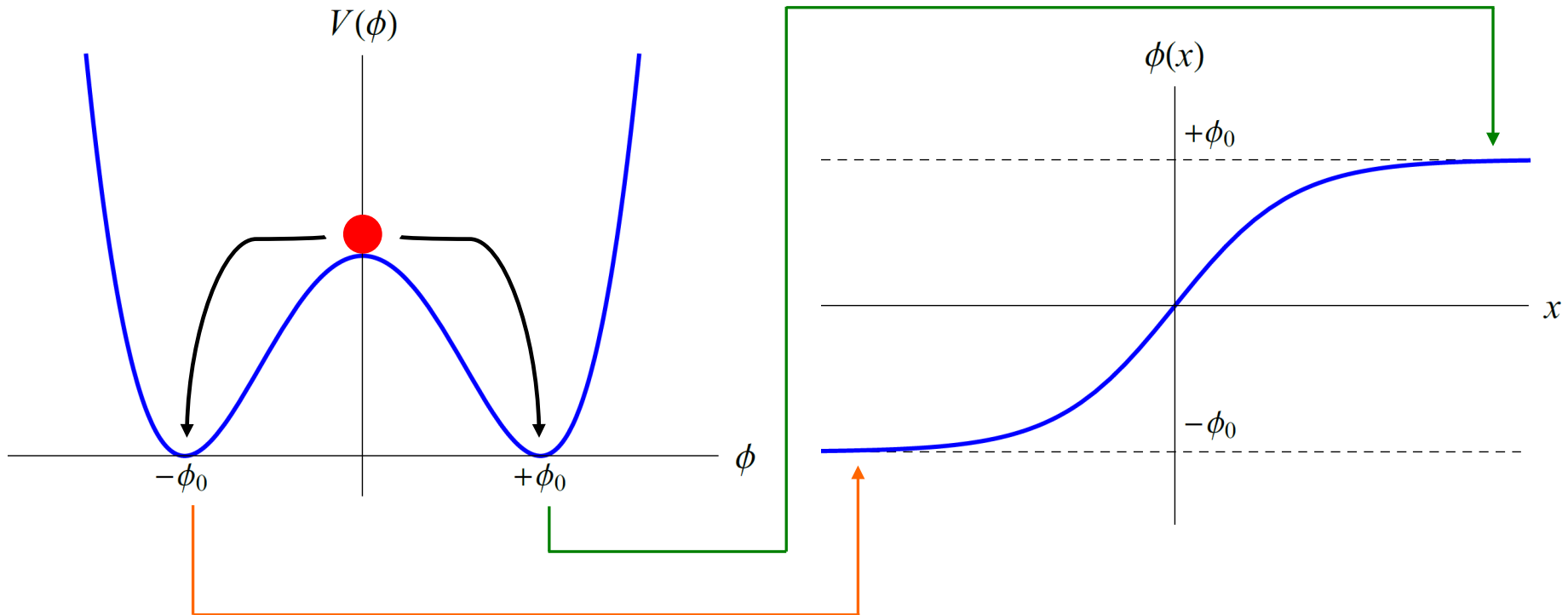
**$\varphi^4$  potential  
(non-trivial topology)**



**$\varphi^2$  potential  
(trivial topology)**

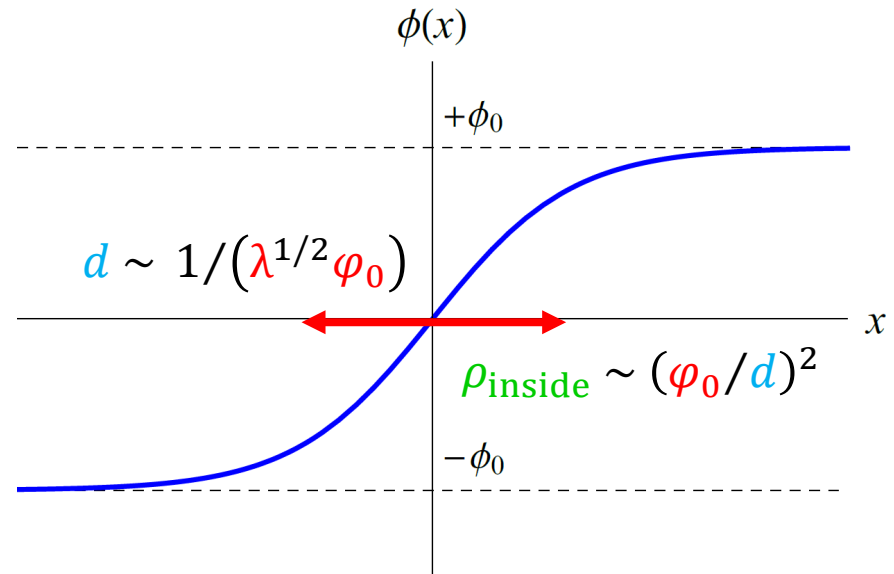
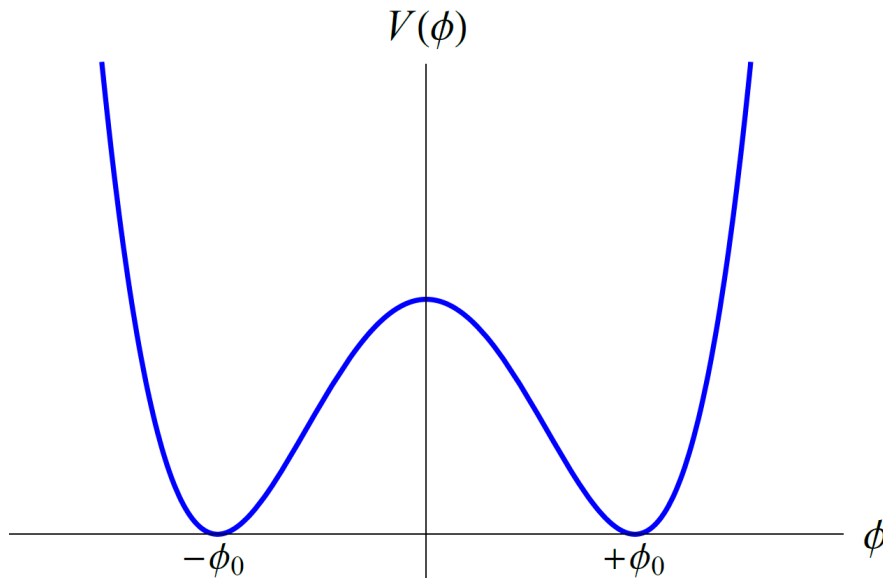
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- Different regions in space may settle in different vacua/minima
- **“Domain wall”** forms – boundary between different **“domains”**



**Domain wall:**  $\varphi(x) = \varphi_0 \tanh(x/d)$

# Variations of Fundamental Constants

$$\mathcal{L}_f = -\frac{\varphi^2}{(\Lambda'_f)^2} m_f \bar{f} f \quad \text{cf.} \quad \mathcal{L}_f^{\text{SM}} = -m_f \bar{f} f \quad \Rightarrow \quad m_f(\varphi^2) = m_{f,0} \left[ 1 + \left( \frac{\varphi}{\Lambda'_f} \right)^2 \right]$$

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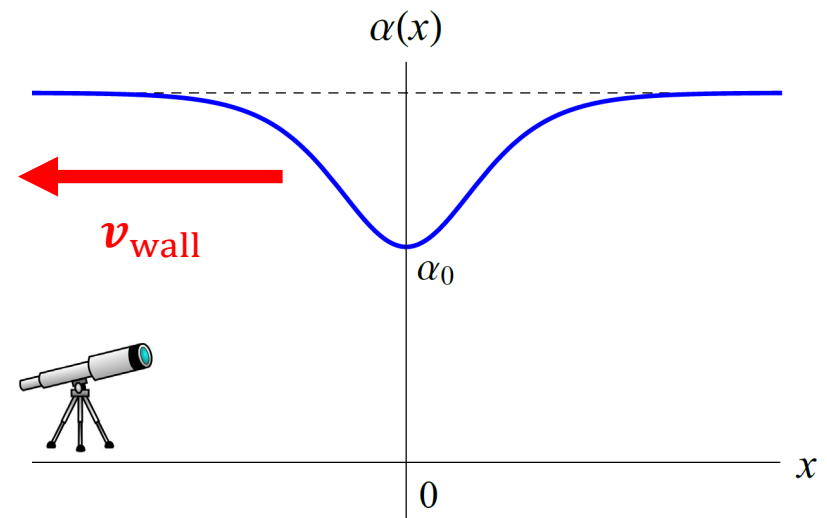
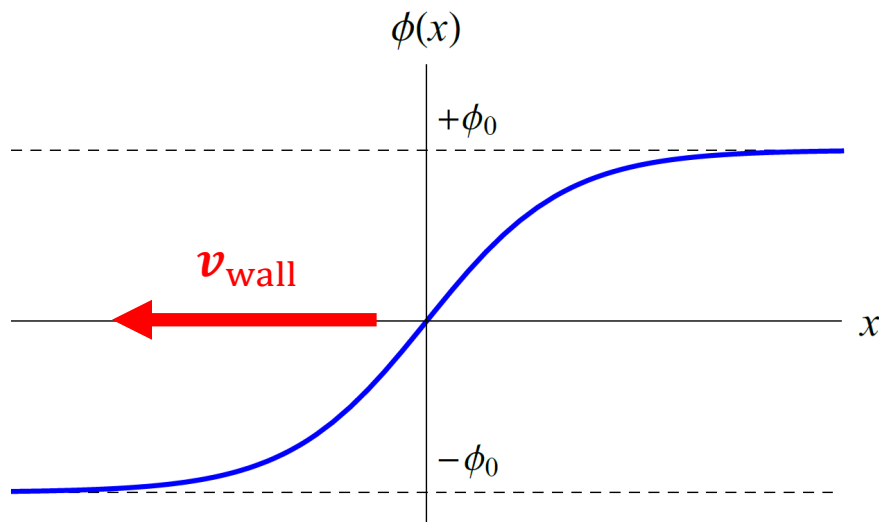


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- A passing domain wall induces apparent **transient** variations of fundamental constants, due to a temporary change in  $\varphi^2$
- Can search for these transient variations of fundamental constants by using various networks of detectors:
  - Clocks [[Derevianko, Pospelov, \*Nature Physics\* \*\*10\*\*, 933 \(2014\)](#)]
  - Pulsars [[Stadnik, Flambaum, \*PRL\* \*\*113\*\*, 151301 \(2014\)](#)]
  - Cavities and laser interferometers [[Stadnik, Flambaum, \*PRL\* \*\*114\*\*, 161301 \(2015\)](#); [PRA \*\*93\*\*, 063630 \(2016\)](#)], [[Grote, Stadnik, \*PRR\* \*\*1\*\*, 033187 \(2019\)](#)]

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- A passing domain wall induces apparent **transient** variations of fundamental constants, due to a temporary change in  $\varphi^2$
- Several clock- and cavity-based searches already performed:
  - [[Wcislo et al., Nature Astronomy 1, 0009 \(2016\)](#)]
  - [[Roberts et al., Nature Communications 8, 1195 \(2017\)](#)]
  - [[Wcislo et al., Science Advances 4, eaau4869 \(2018\)](#)]
  - [[Roberts et al., New J. Phys. 22, 093010 \(2020\)](#)]
  - Several talks outlining results at the previous MG15 meeting

# Variations of Fundamental Constants

[Stadnik, *PRD* **102**, 115016 (2020)]

- Previous work overlooked “**back-action**” **effects** of ambient matter on the domain-wall scalar field with  $\varphi^2$  interactions

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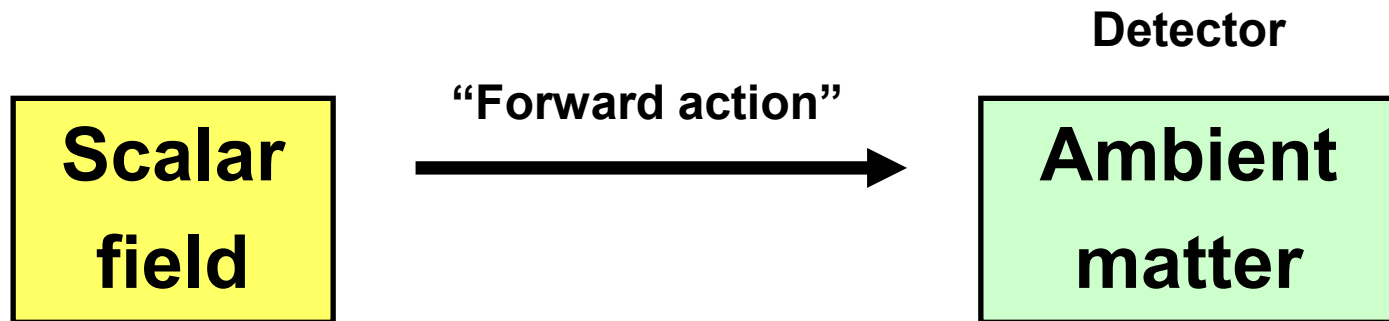
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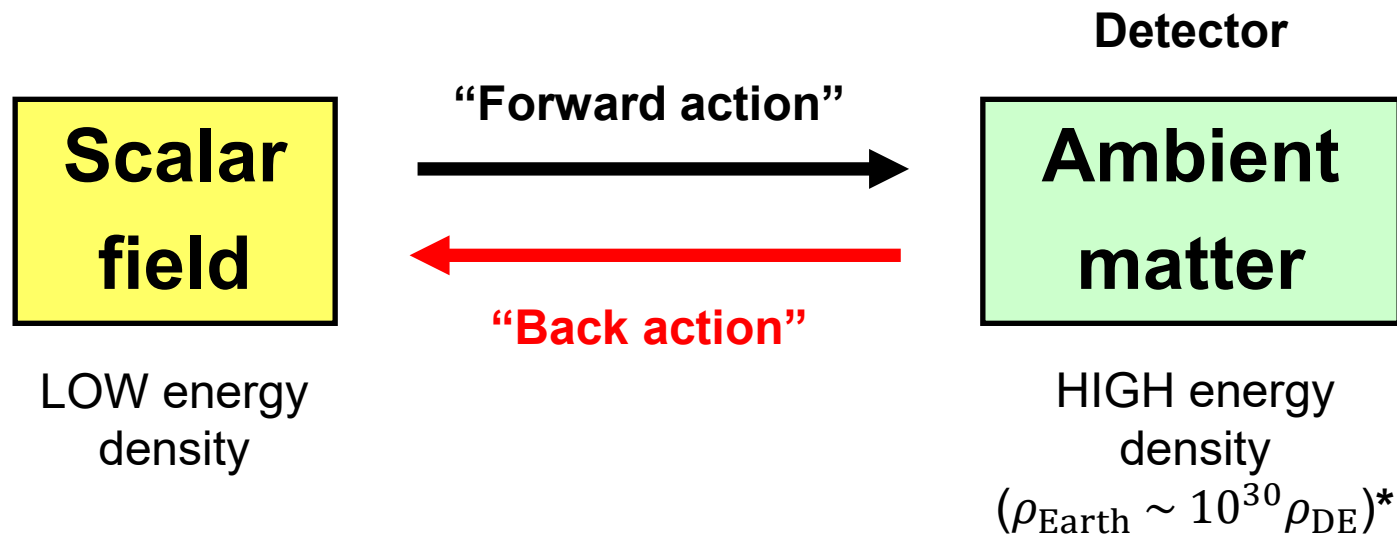
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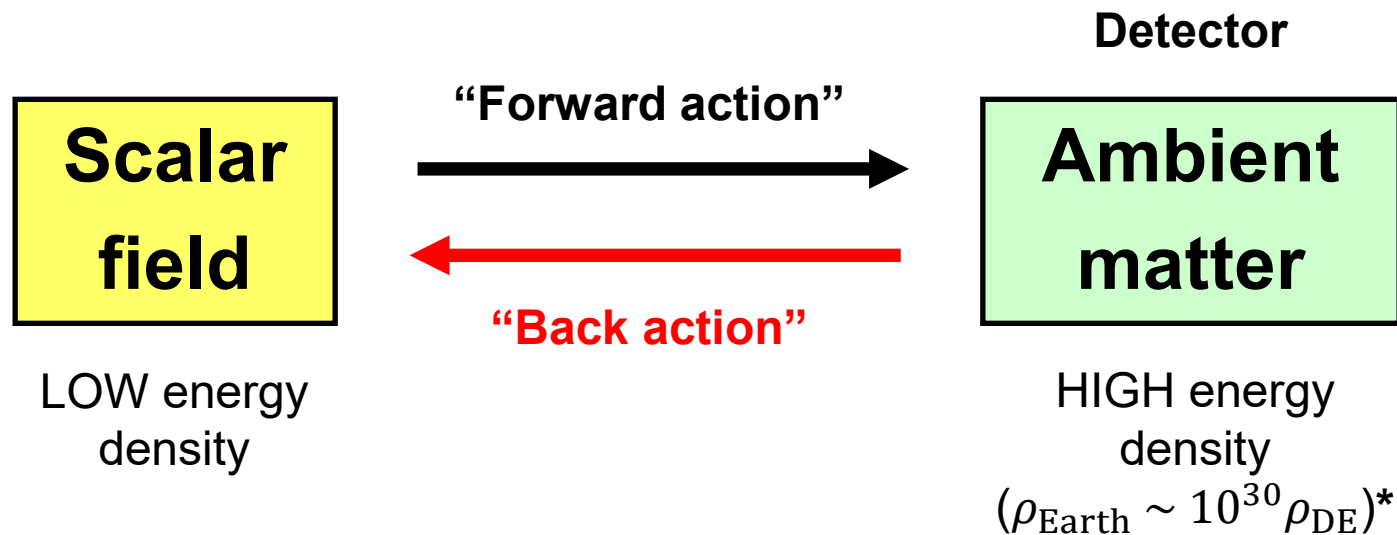


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Non-relativistic  
ambient matter

$\rho_\gamma$  = Coulomb binding energy

$\rho_e$  = electron mass-energy

$\rho_N$  = nucleon mass-energy

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$$\Rightarrow V_{\text{eff}}(\varphi) = V_{\text{bare}}(\varphi) + \sum_{X=\gamma,e,N} \frac{\rho_X \varphi^2}{(\Lambda'_X)^2} \quad \leftarrow \text{Ambient matter contribution}$$

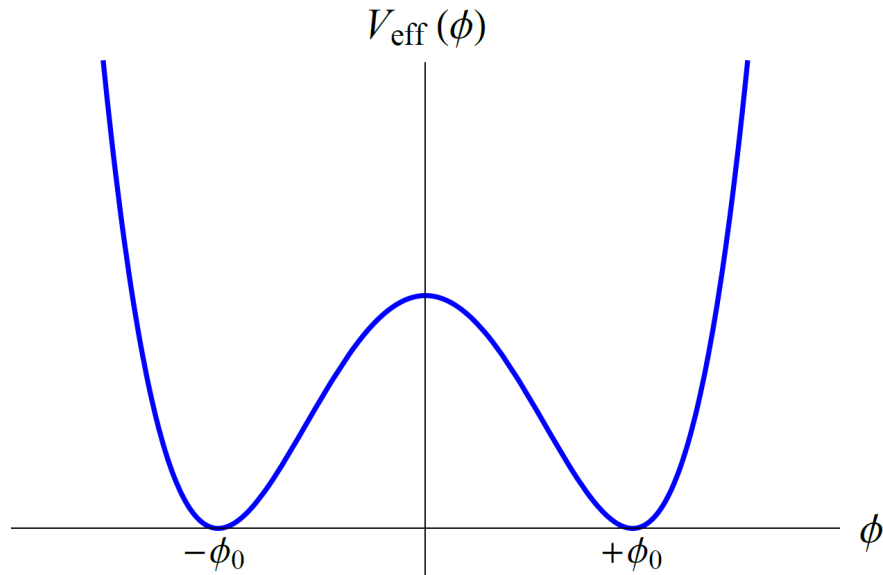
Effective potential

$$= \frac{\lambda}{4} (\varphi^2 - \varphi_0^2)^2 + \sum_{X=\gamma,e,N} \frac{\rho_X \varphi^2}{(\Lambda'_X)^2}$$

# Environmental Dependence of “Constants”

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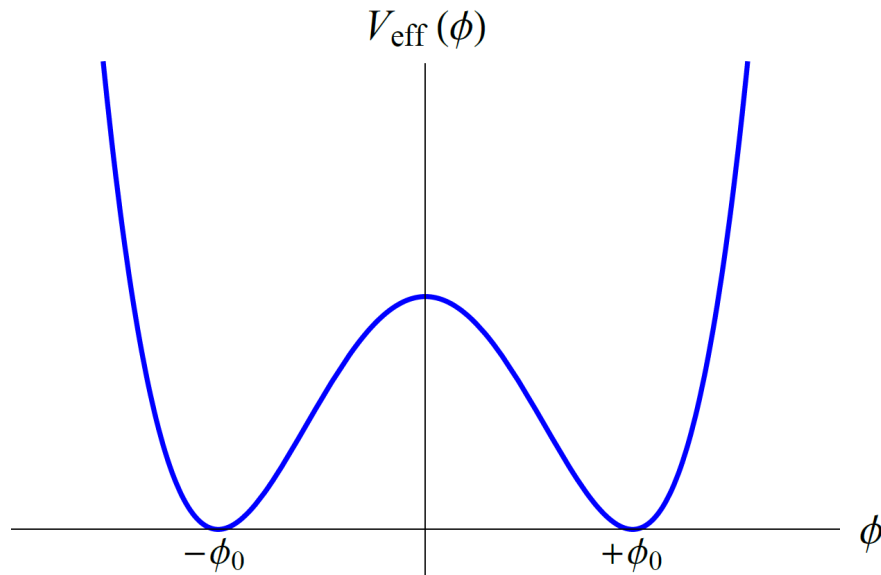


**Low-density environment  
(non-trivial topology,  
supports domain walls)**

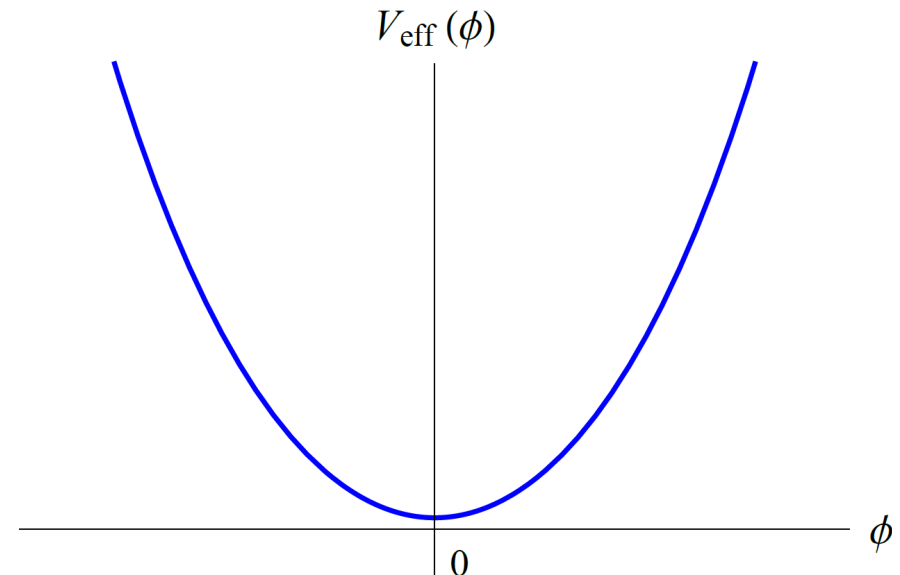
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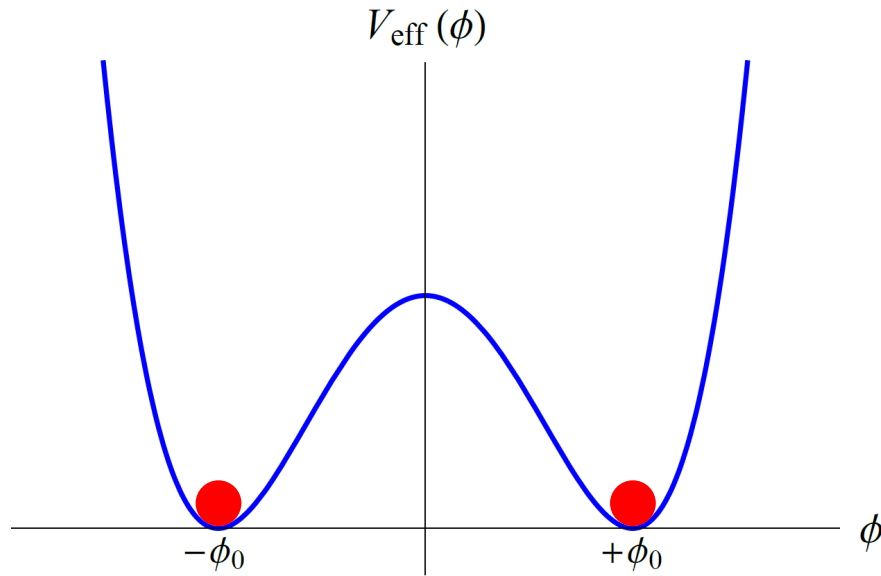


**High-density environment  
(trivial topology,  
destabilises domain walls)**

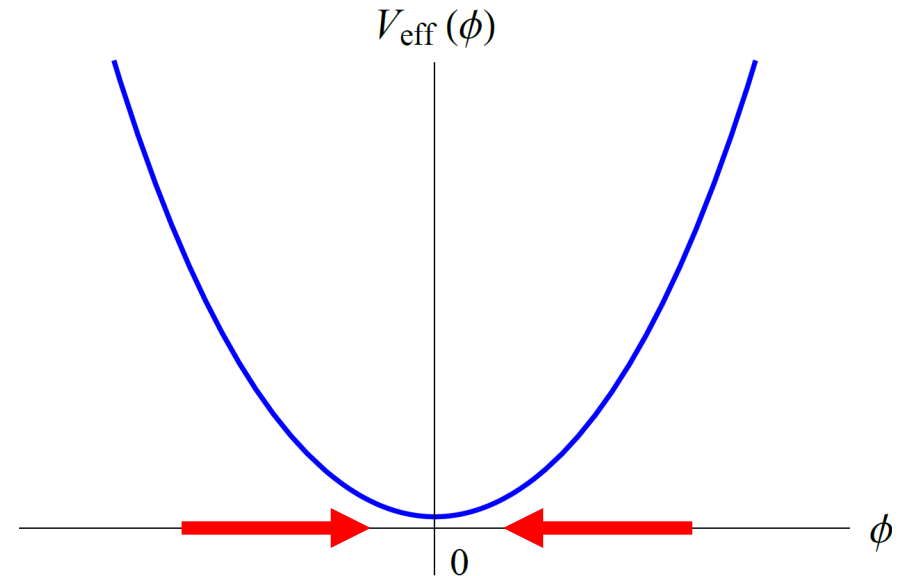
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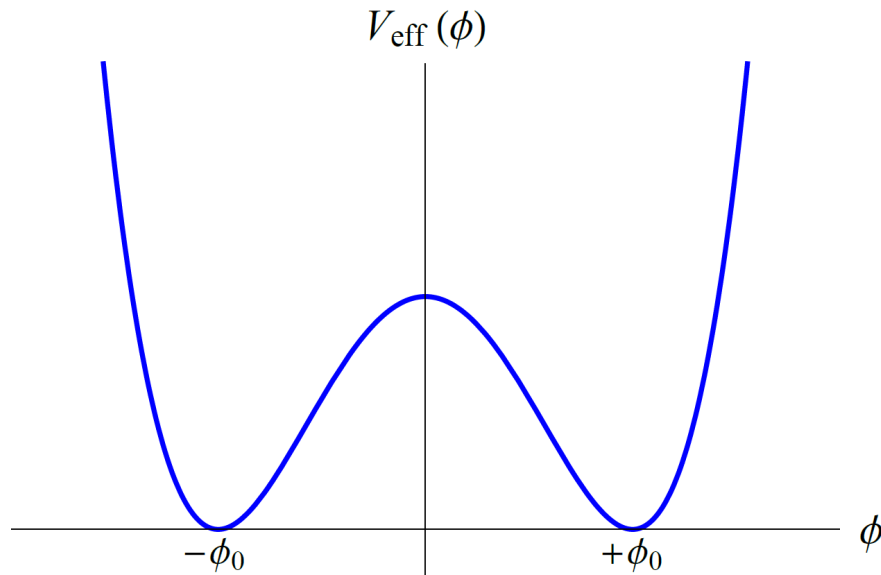
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- Scalar field  $\varphi$  tends to be **screened in dense environments**

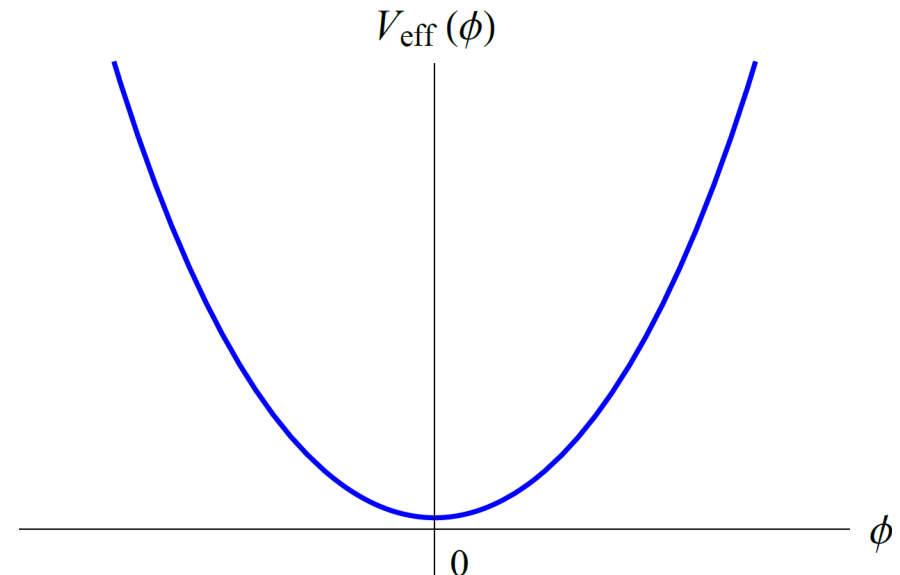
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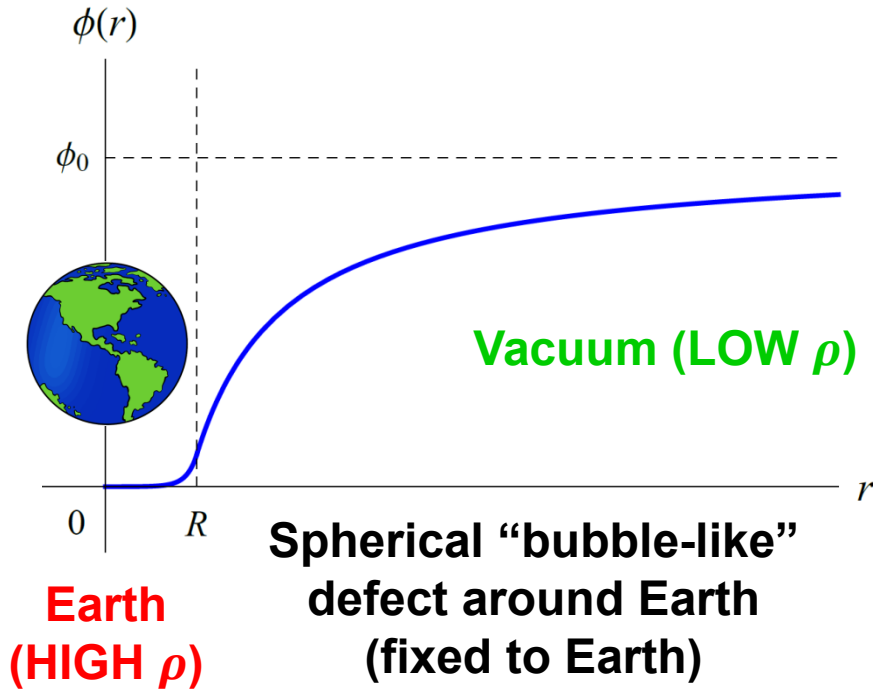


High-density environment

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- $\alpha[\varphi^2(\rho)], m_f[\varphi^2(\rho)] \Rightarrow$  **Environmental dependence of “constants”**

# Spatial Variations of “Constants”

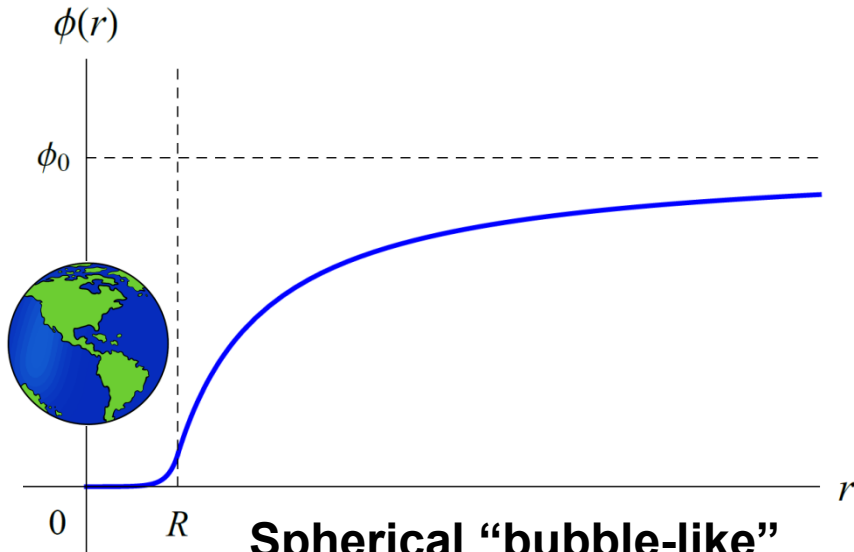
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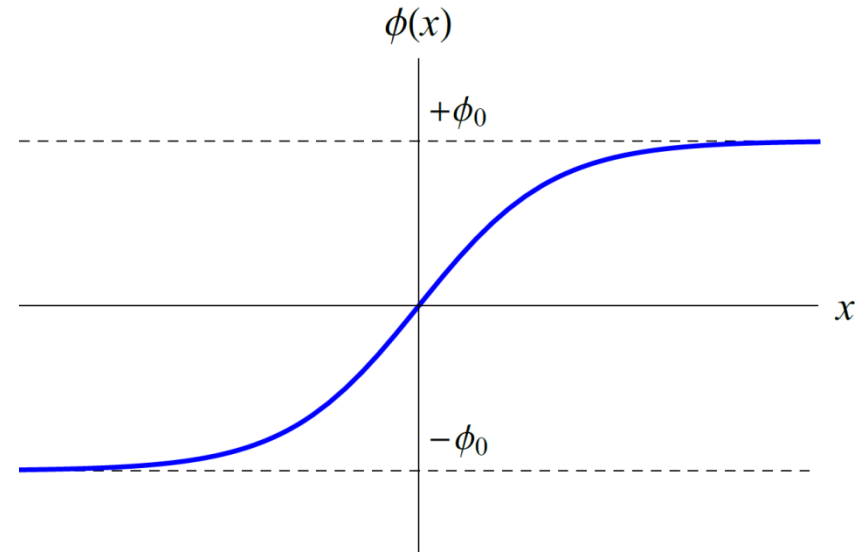


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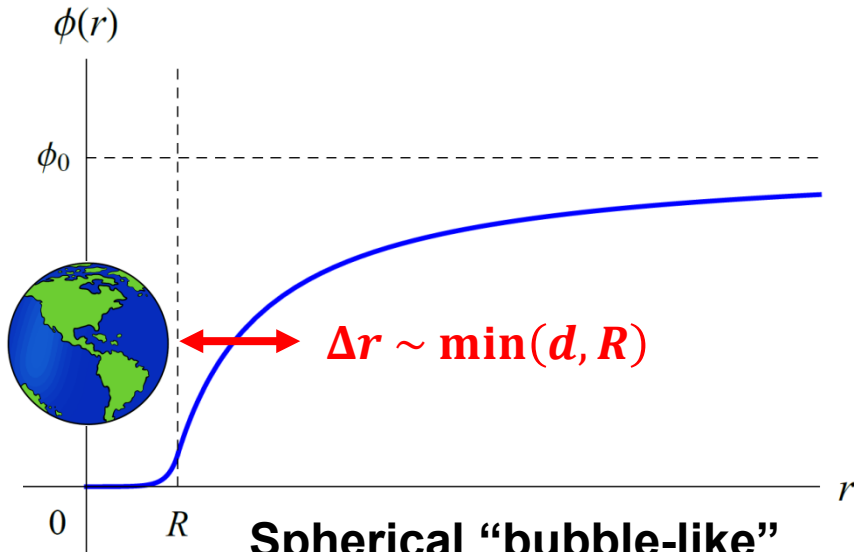
**Spherical “bubble-like”  
defect around Earth  
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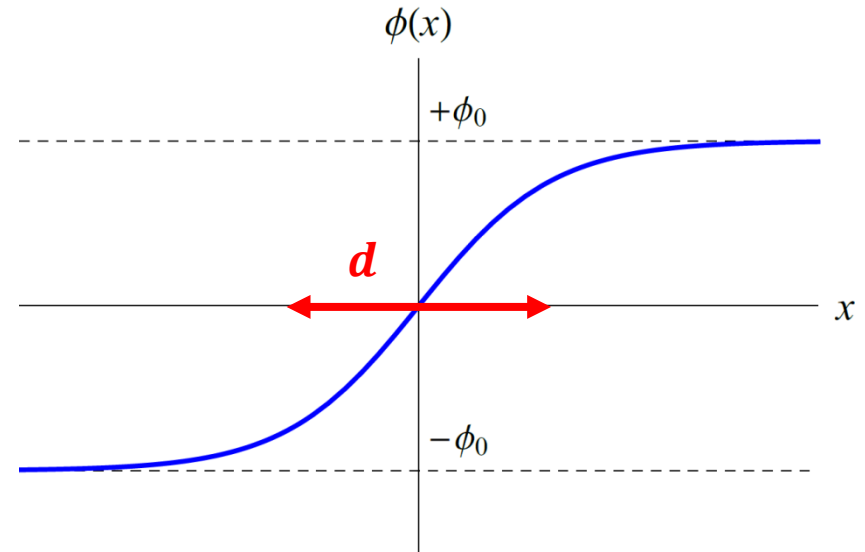
**Planar defect in free space  
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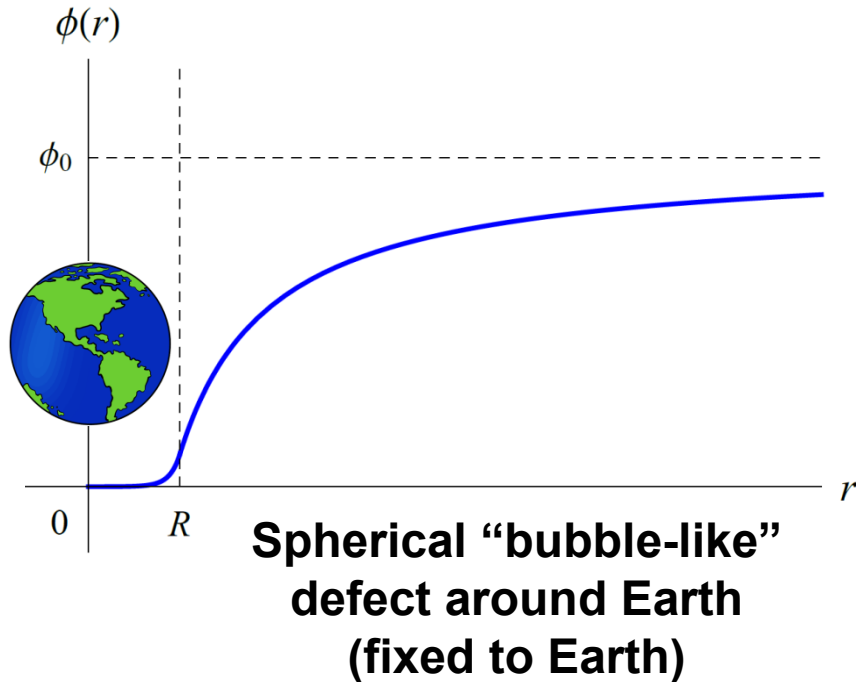
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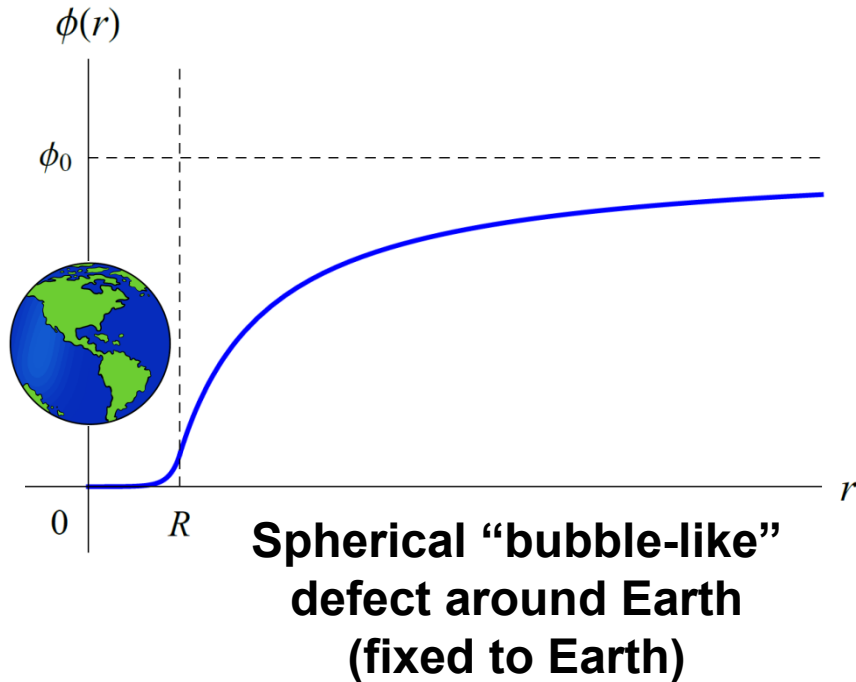
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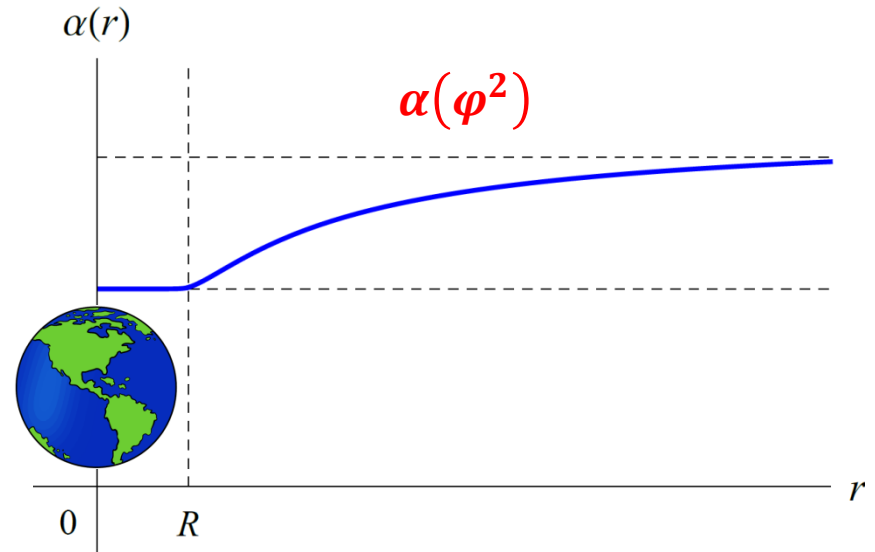
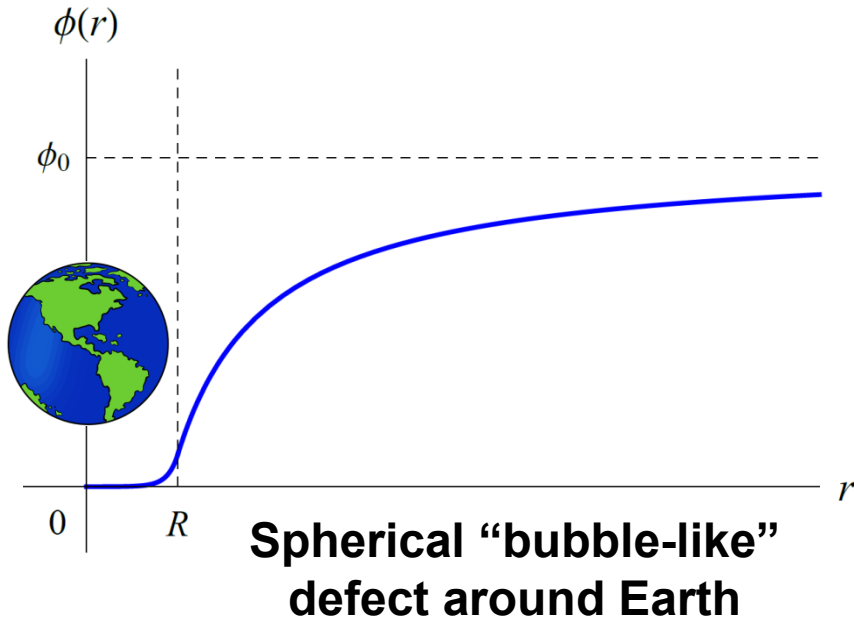


Very generic signatures – present even if Universe consists of only a *single* domain (i.e., when *no cosmological* domain walls)

⇒ We don’t have to wait for a (possibly single or non-existent) domain wall of *cosmological origin* to pass by Earth!

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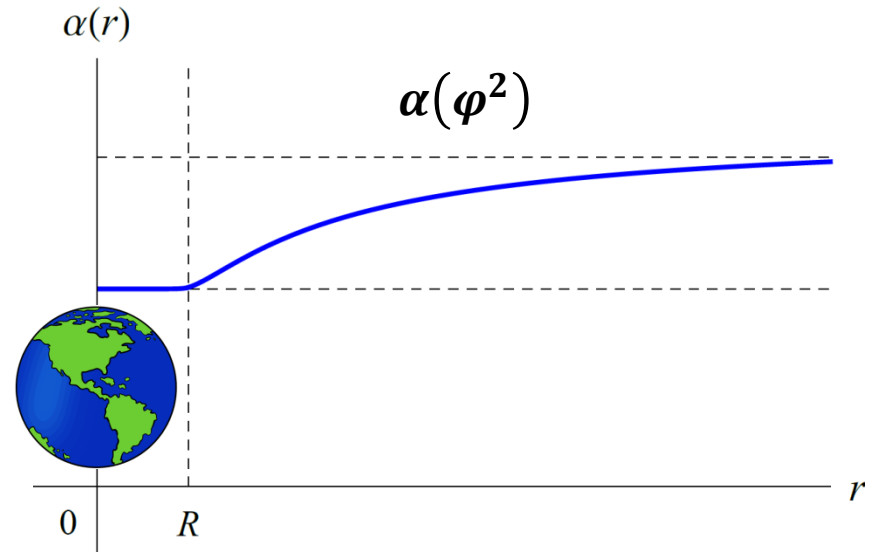
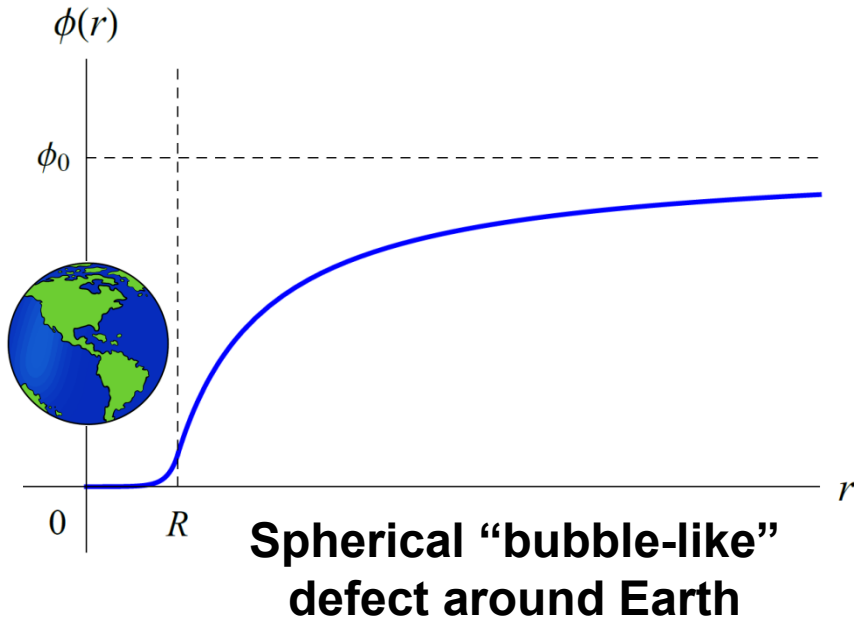
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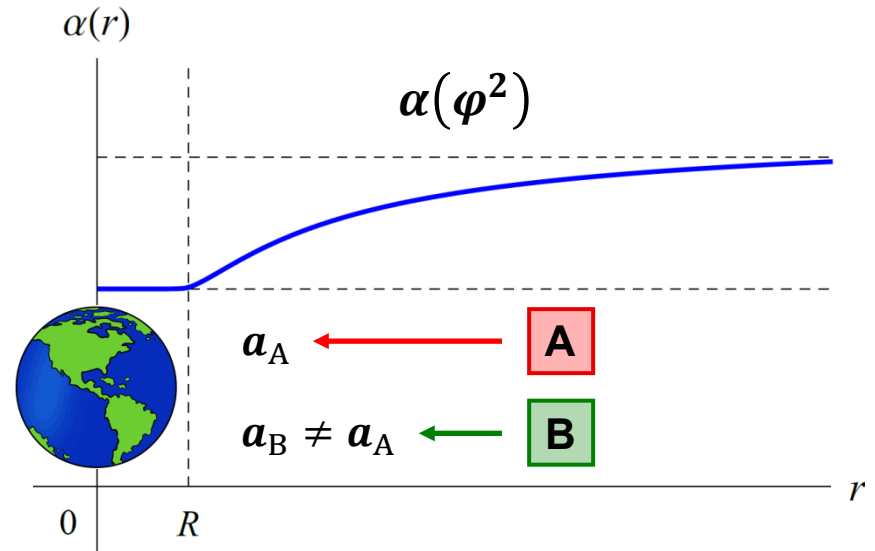
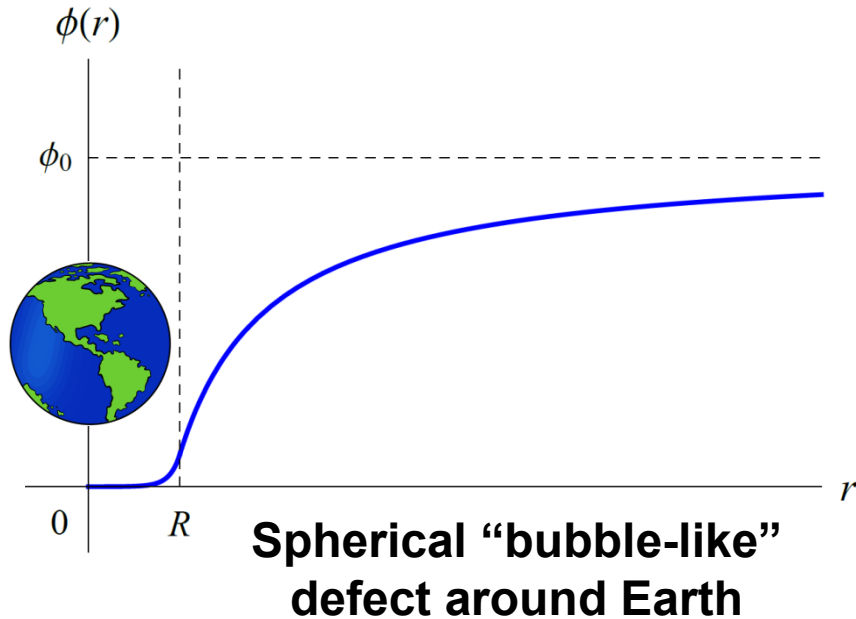
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- Can search for these spatial gradients (e.g.,  $\nabla \alpha / \alpha$ ) with:
  1. Equivalence-principle-violating forces:  $\delta \mathbf{a}_{\text{test}} = -\nabla [m_{\text{test}}(\alpha)] / m_{\text{test}}$
  2. Compare clocks at different heights:  $\Delta v / v = K_\alpha \Delta \alpha / \alpha$
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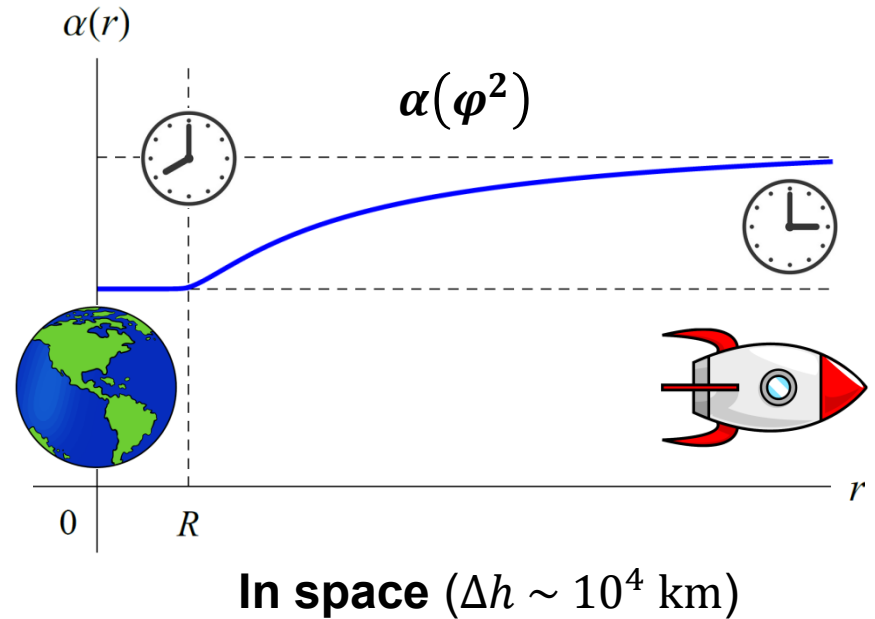
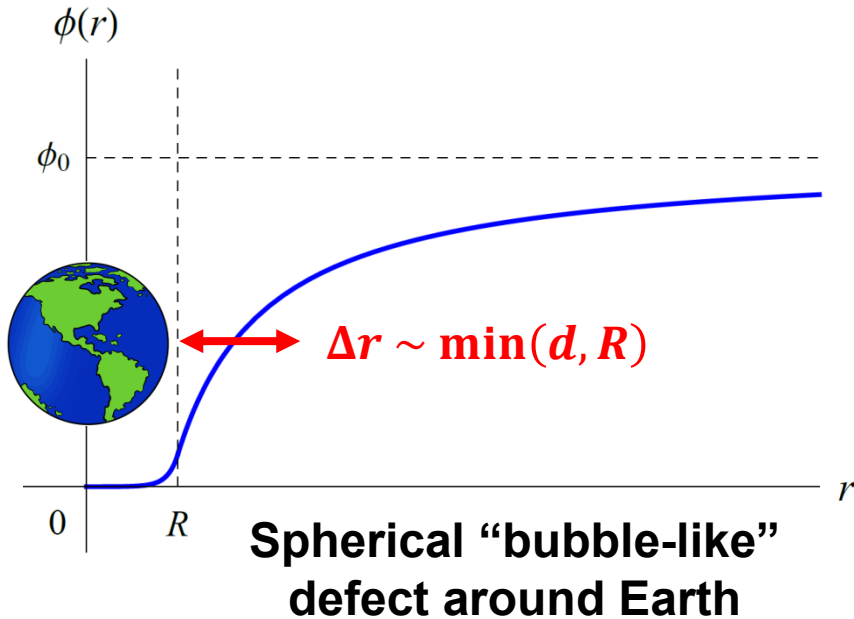
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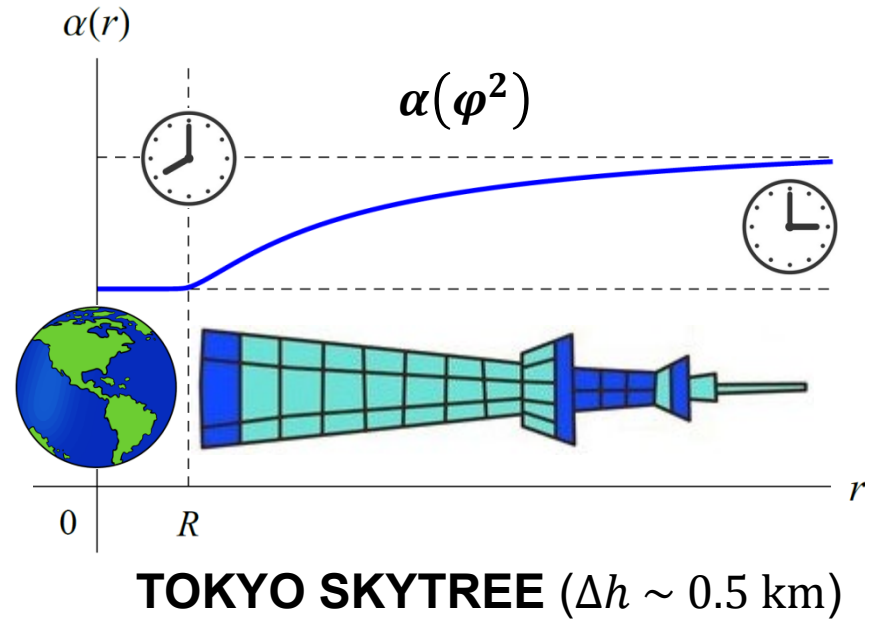
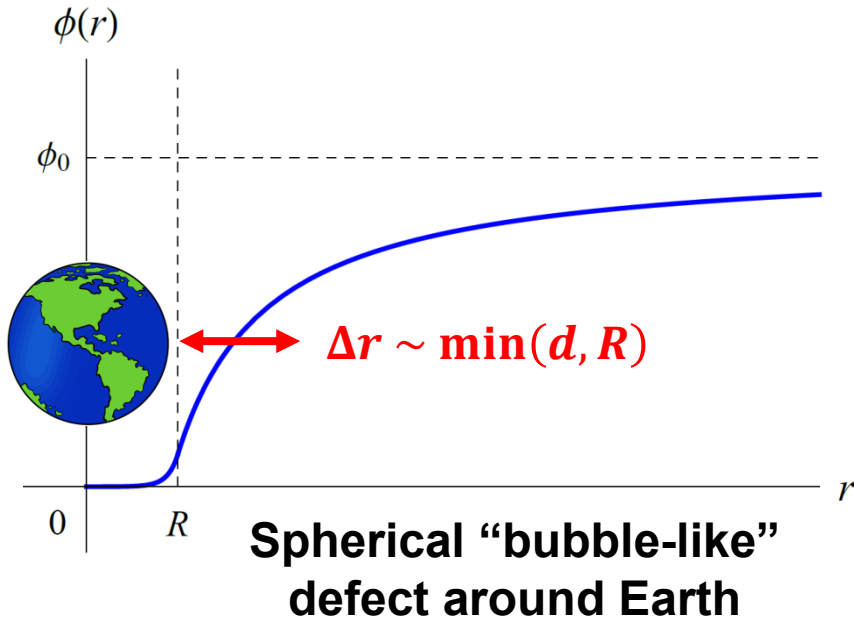


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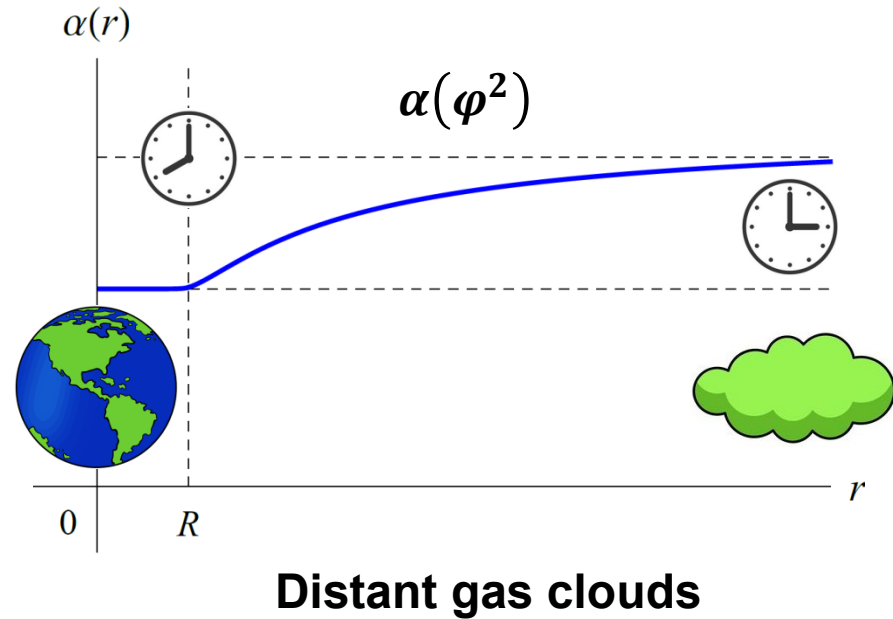
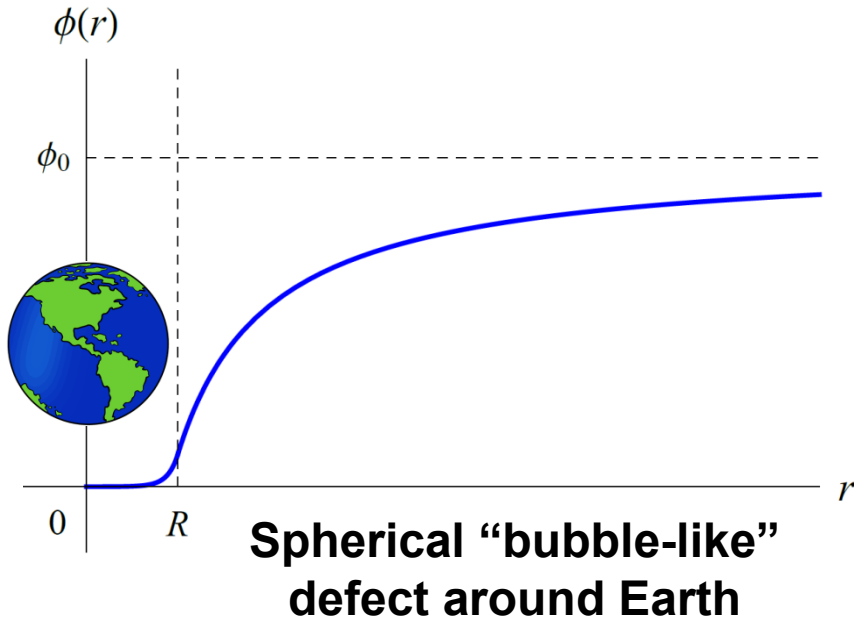
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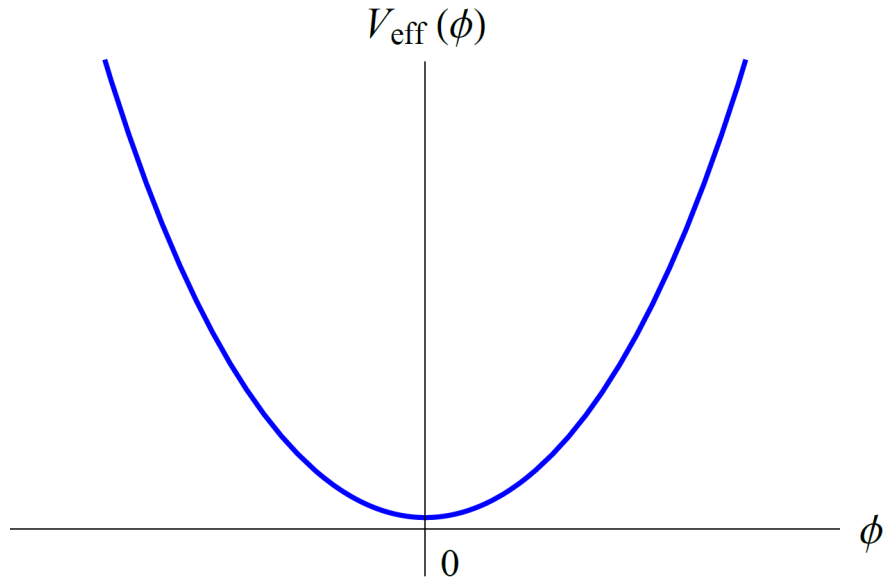
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# Cosmological Production of Domain Walls

[Stadnik, *PRD* **102**, 115016 (2020)]

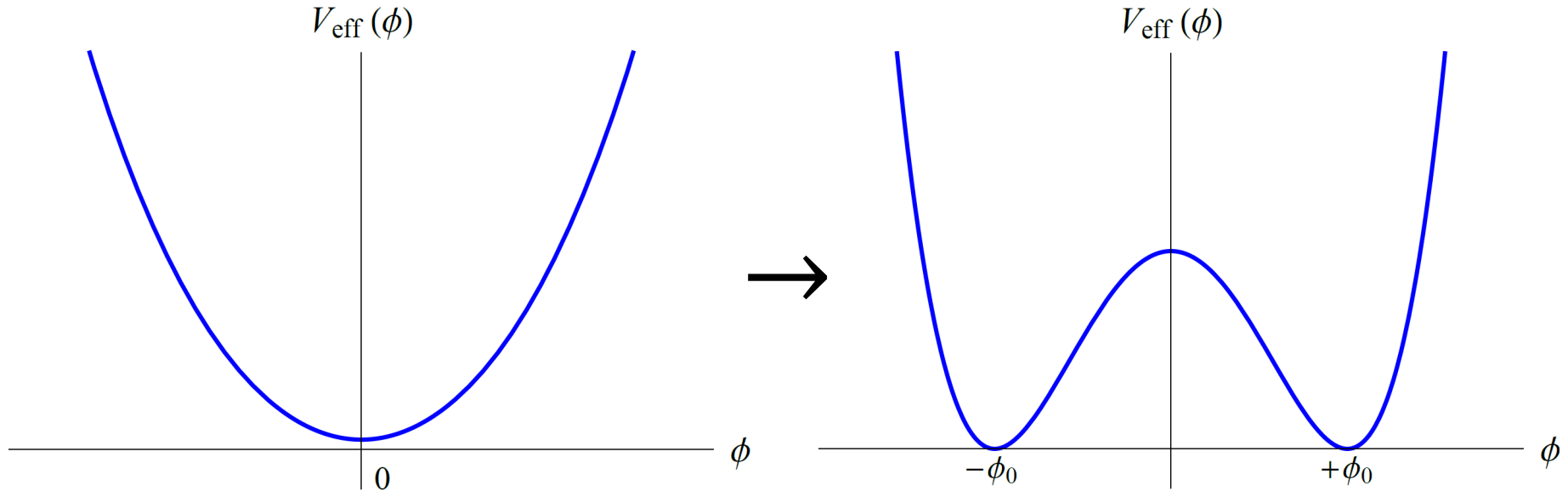


**High-density environment  
("early" Universe, no walls)**

$$V_{\text{eff}}(\varphi) = \frac{\lambda}{4} (\varphi^2 - \varphi_0^2)^2 + \sum_{X=\gamma, e, N} \frac{\rho_X \varphi^2}{(\Lambda'_X)^2}$$

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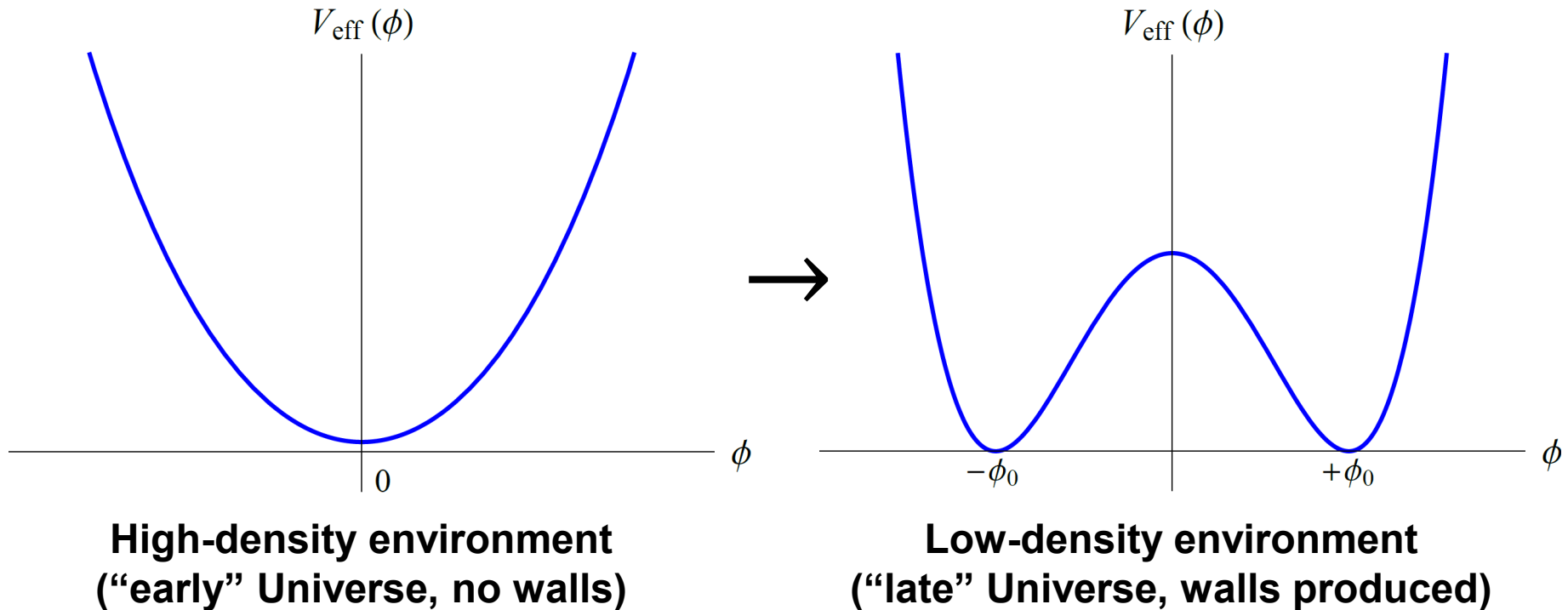
**Low-density environment**  
("late" Universe, walls produced)

- As Universe cools, distant regions tend to settle in different vacua/minima – expect  $\sim \mathcal{O}(1)$  domain wall to survive to present day

$$V_{\text{eff}}(\varphi) = \frac{\lambda}{4} (\varphi^2 - \varphi_0^2)^2 + \sum_{X=\gamma, e, N} \frac{\rho_X \varphi^2}{(\Lambda'_X)^2}$$

# Cosmological Production of Domain Walls

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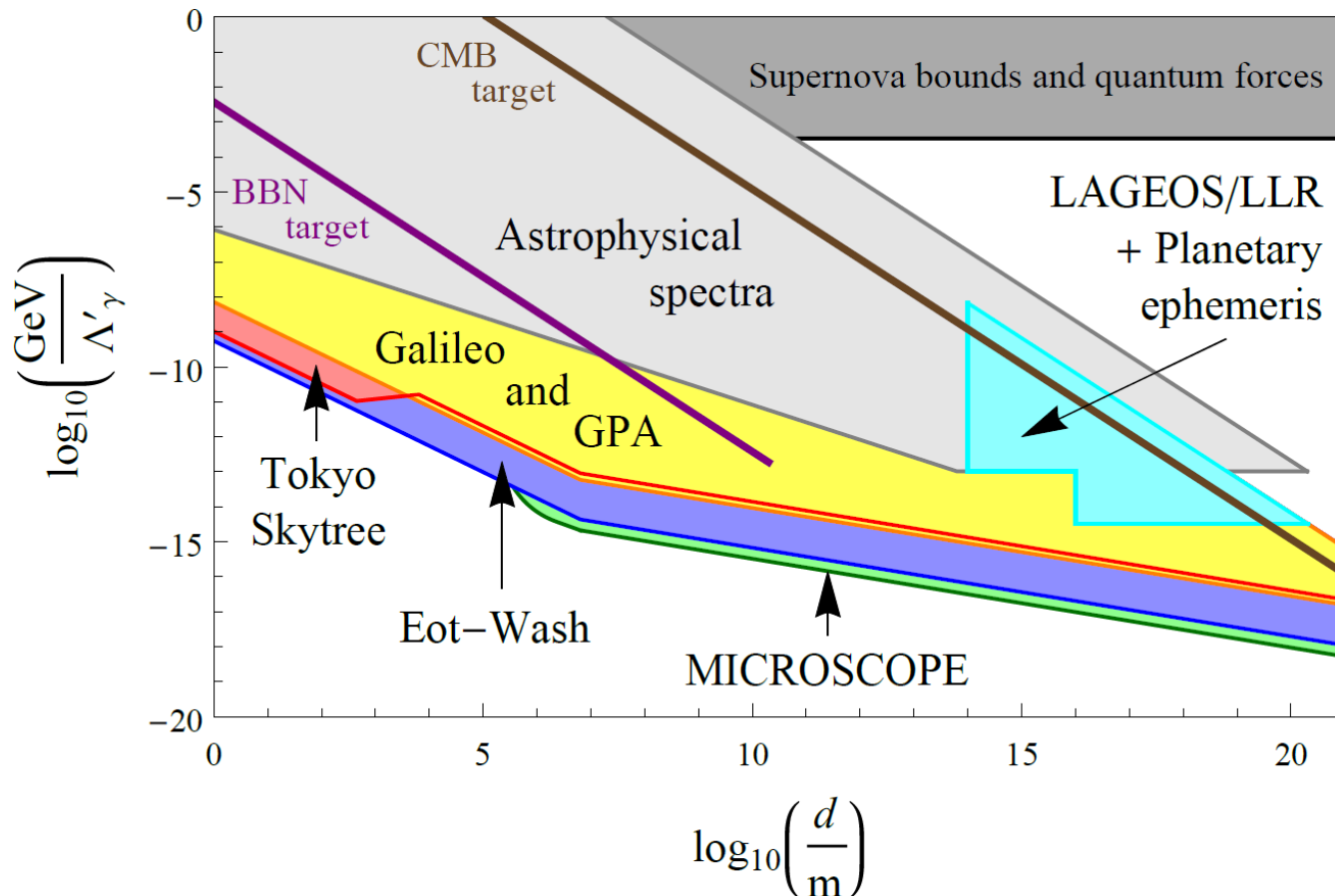
- As Universe cools, distant regions tend to settle in different vacua/minima – expect  $\sim \mathcal{O}(1)$  domain wall to survive to present day
- Even if only 1 wall stretching across the Universe survives, gravitational effects of wall(s) on CMB constrain  $\rho_{\text{wall(s)}} < 10^{-5} \rho_{\text{total}}$

# Constraints on $\varphi^2$ Interaction with the Photon [Single wall, $\rho_{\text{wall}} \sim 10^{-5} \rho_{\text{total}}$ ]

[Stadnik, *PRD* **102**, 115016 (2020)]

Improvement over previous bounds from different non-transient signatures (by up to  $\sim 10^{15}$ !)

Leading new limits scale as  $\propto \rho_{\text{wall}}^{1/4} \Rightarrow$  Constrain  $\rho_{\text{wall}} \ll 10^{-10} \rho_{\text{total}}$ !

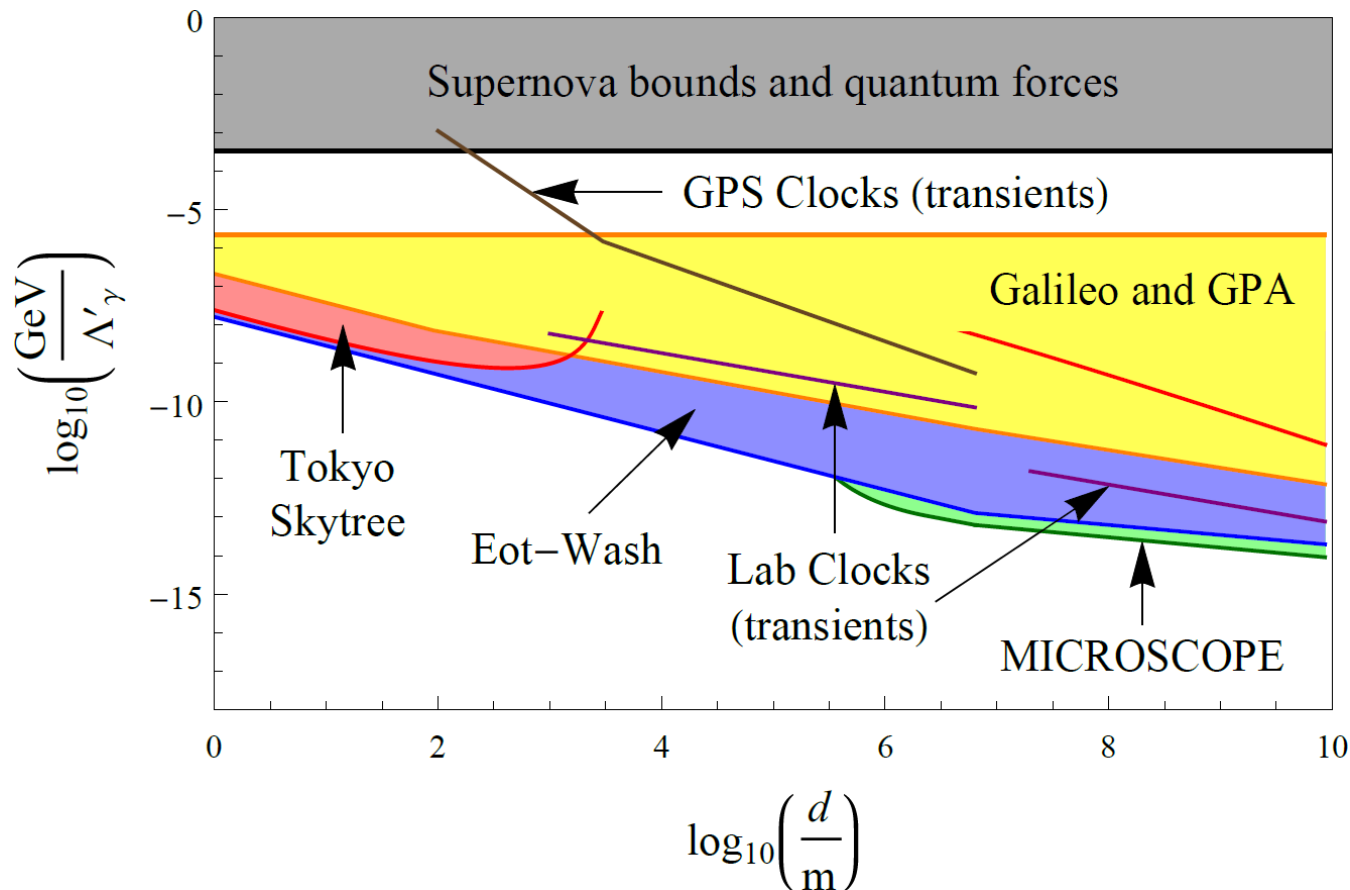


# Constraints on $\varphi^2$ Interaction with the Photon

$[\rho_{\text{walls}} \sim \rho_{\text{DM}}, T_{\text{avg}} \sim 1 \text{ day} \gg \Delta t_{\text{transient}}]$

[Stadnik, *PRD* **102**, 115016 (2020)]

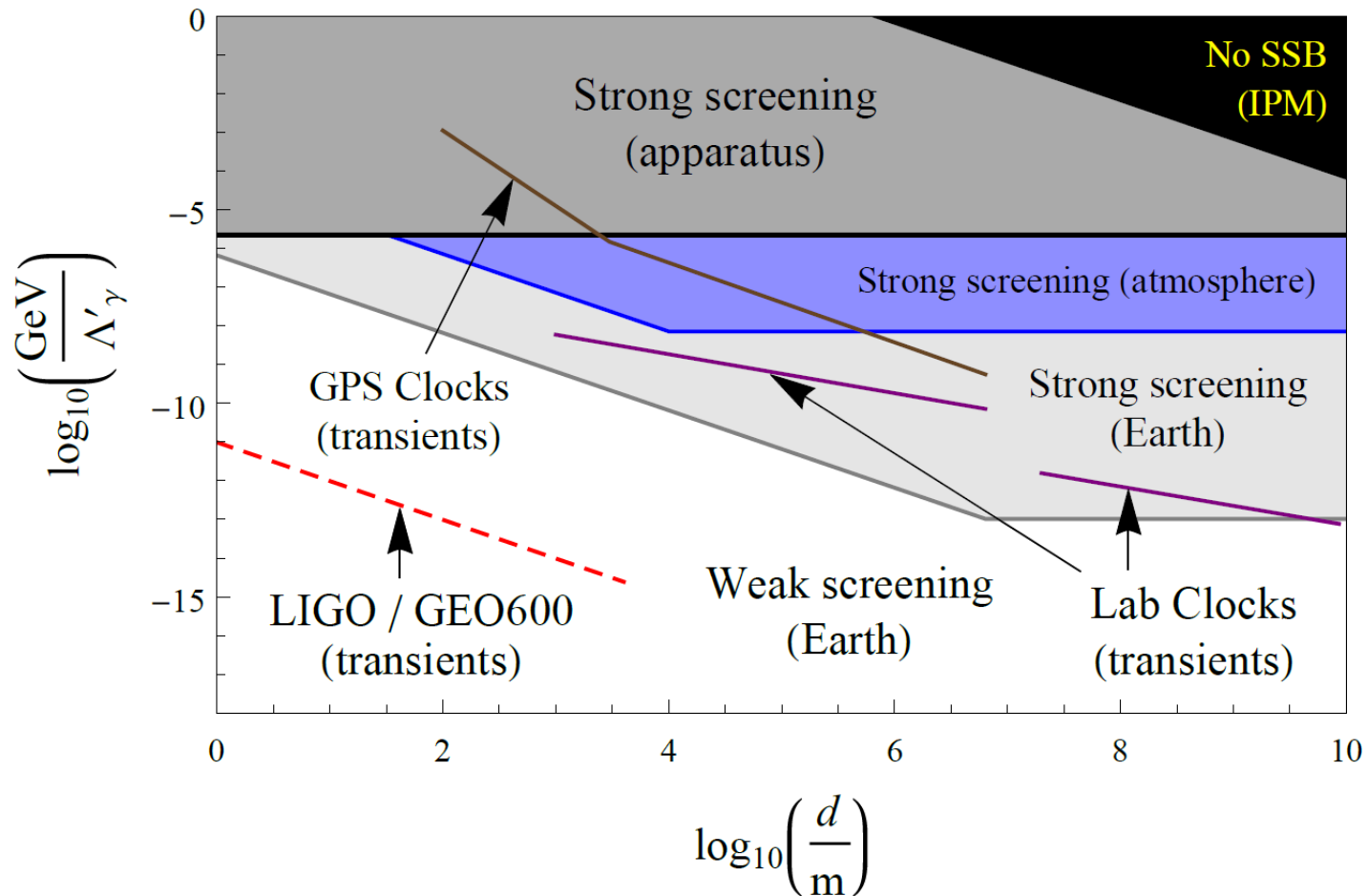
Our new limits from quasi-non-transient effects improve over transient signatures and over previous bounds from different non-transient signatures (by up to  $\sim 10^{10}$ )!



# Scrutinising Bounds from Transient Signatures

[Stadnik, *PRD* **102**, 115016 (2020)]

Strongly repulsive potential generated by Earth may **prevent the unperturbed passage of a domain wall through Earth** – contrary to earlier assumptions

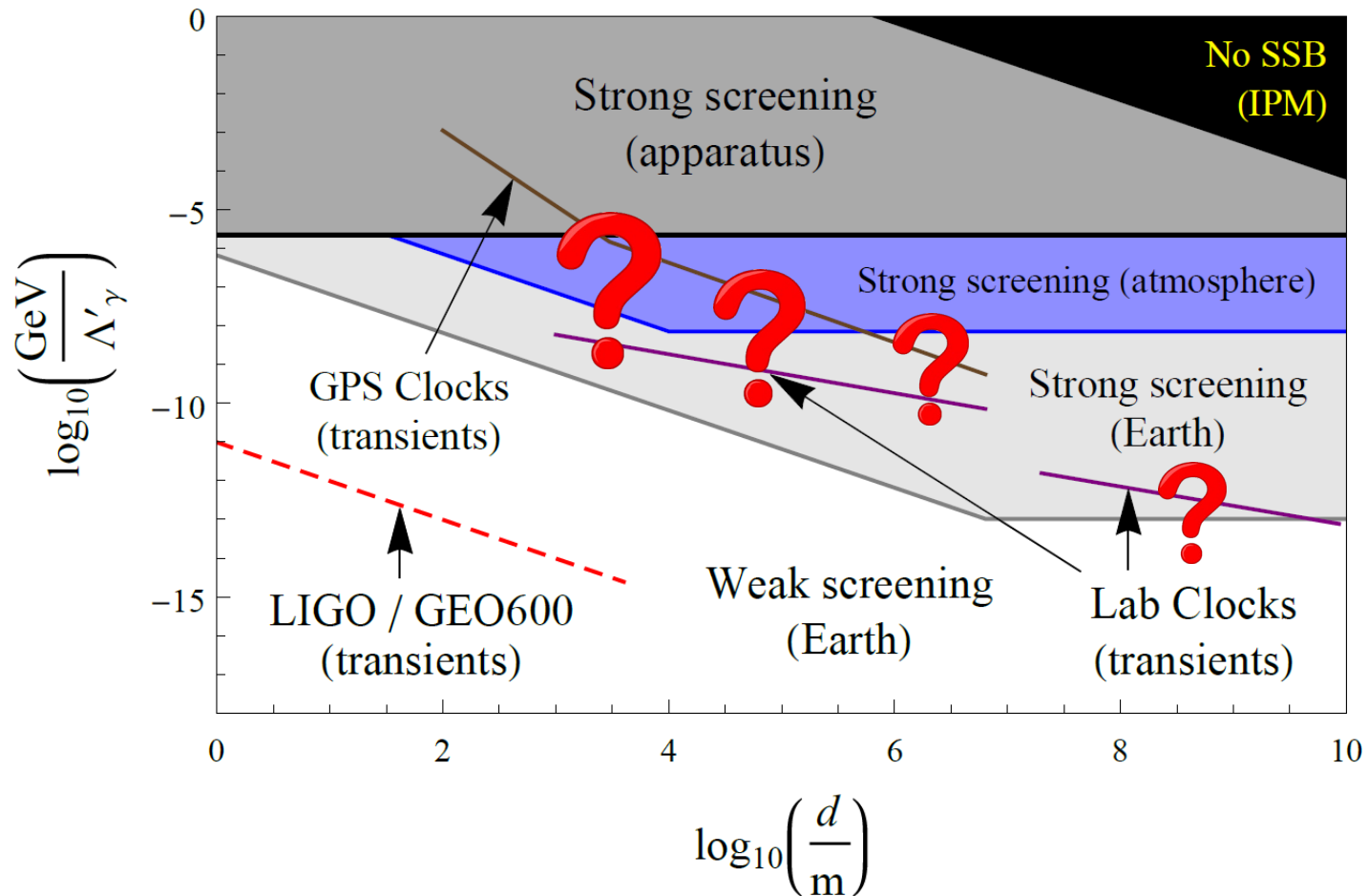




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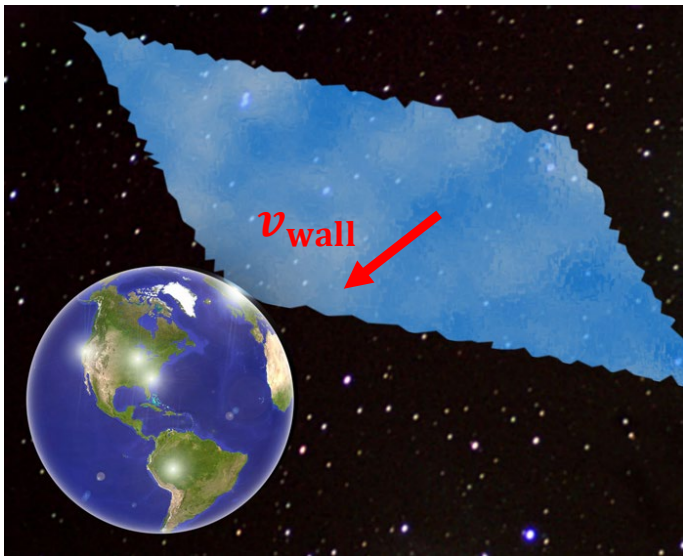
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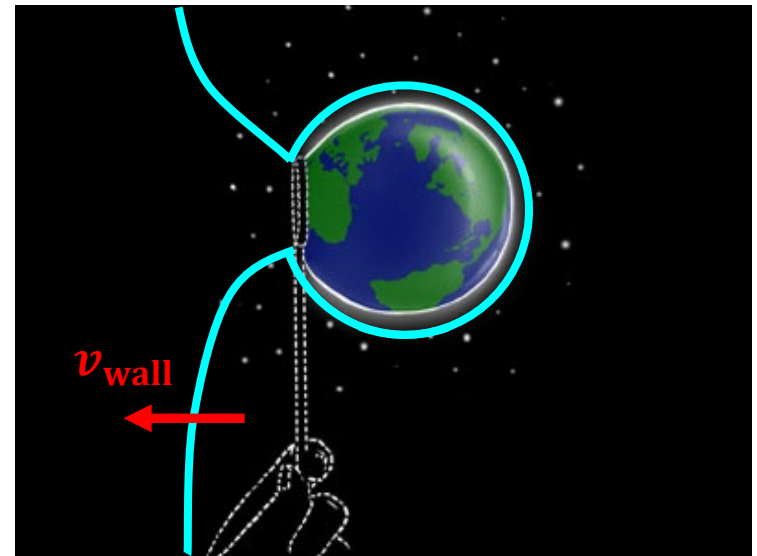
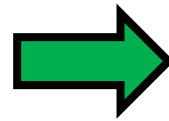
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Domain wall  
incident on Earth

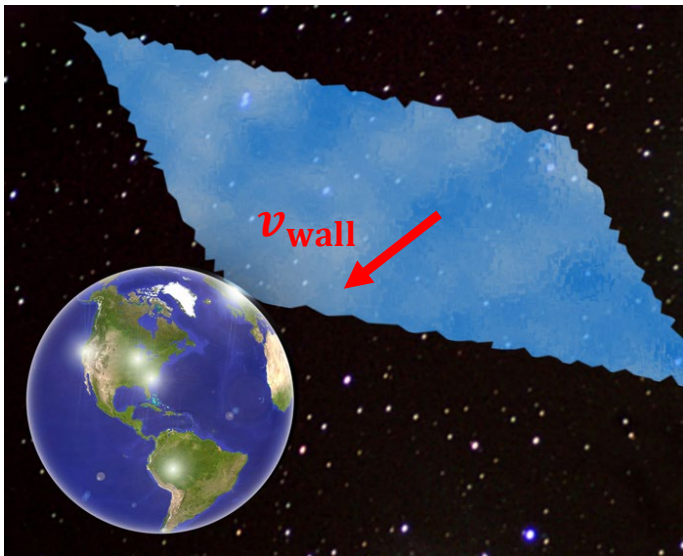


(Meta)stable bubble  
around Earth?

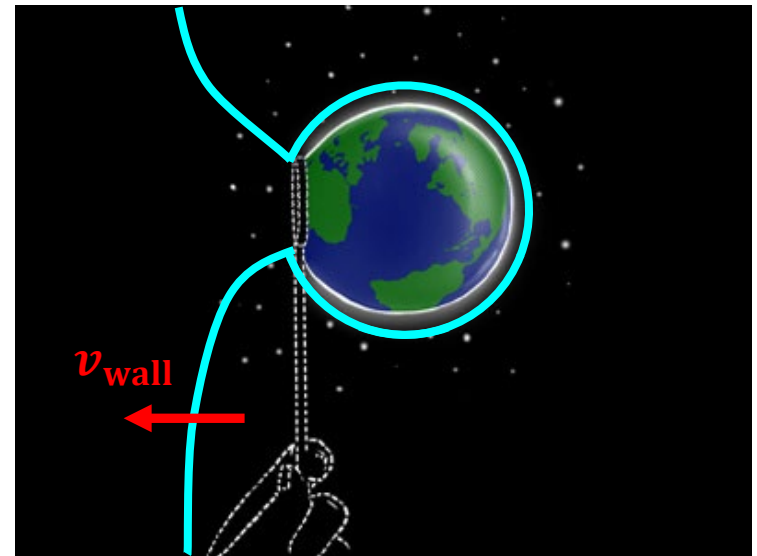
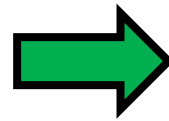
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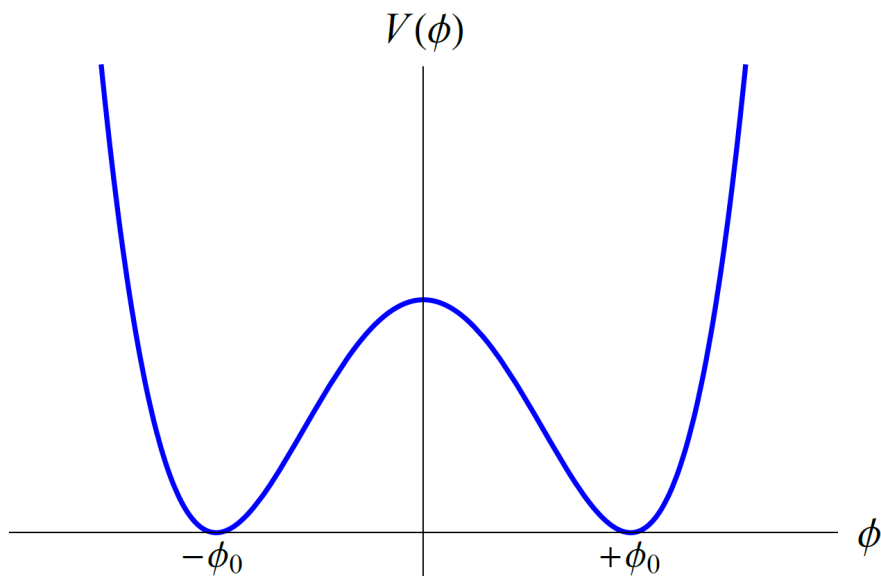
Transient signatures may be qualitatively different from those assumed previously – ongoing work

# Comparison to Oscillating Scalar Field

## Domain wall

$$\varphi(x) = \varphi_0 \tanh(x/d)$$

$$\varphi_0^2 \sim \rho v d T_{\text{avg}} \ll \rho (v T_{\text{avg}})^2 = \rho L_{\text{avg}}^2$$

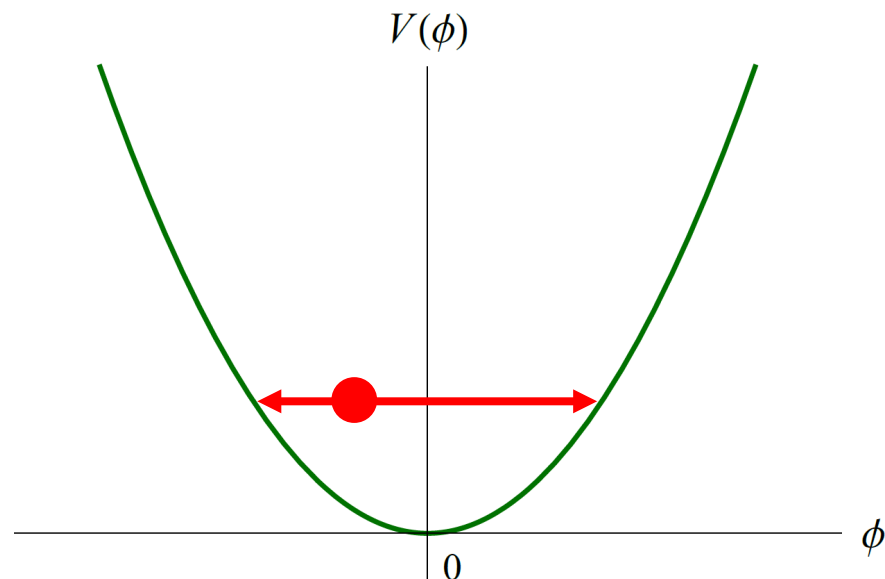


$$V(\varphi) = \frac{\lambda}{4} (\varphi^2 - \varphi_0^2)^2$$

## Oscillating field [may explain dark matter]

$$\varphi(t) = \varphi_0 \cos(m_\varphi c^2 t / \hbar)$$

$$\varphi_0^2 \sim \rho / m_\varphi^2 \sim \rho T_{\text{osc},\varphi}^2 = \rho \lambda_{\text{Comp},\varphi}^2$$



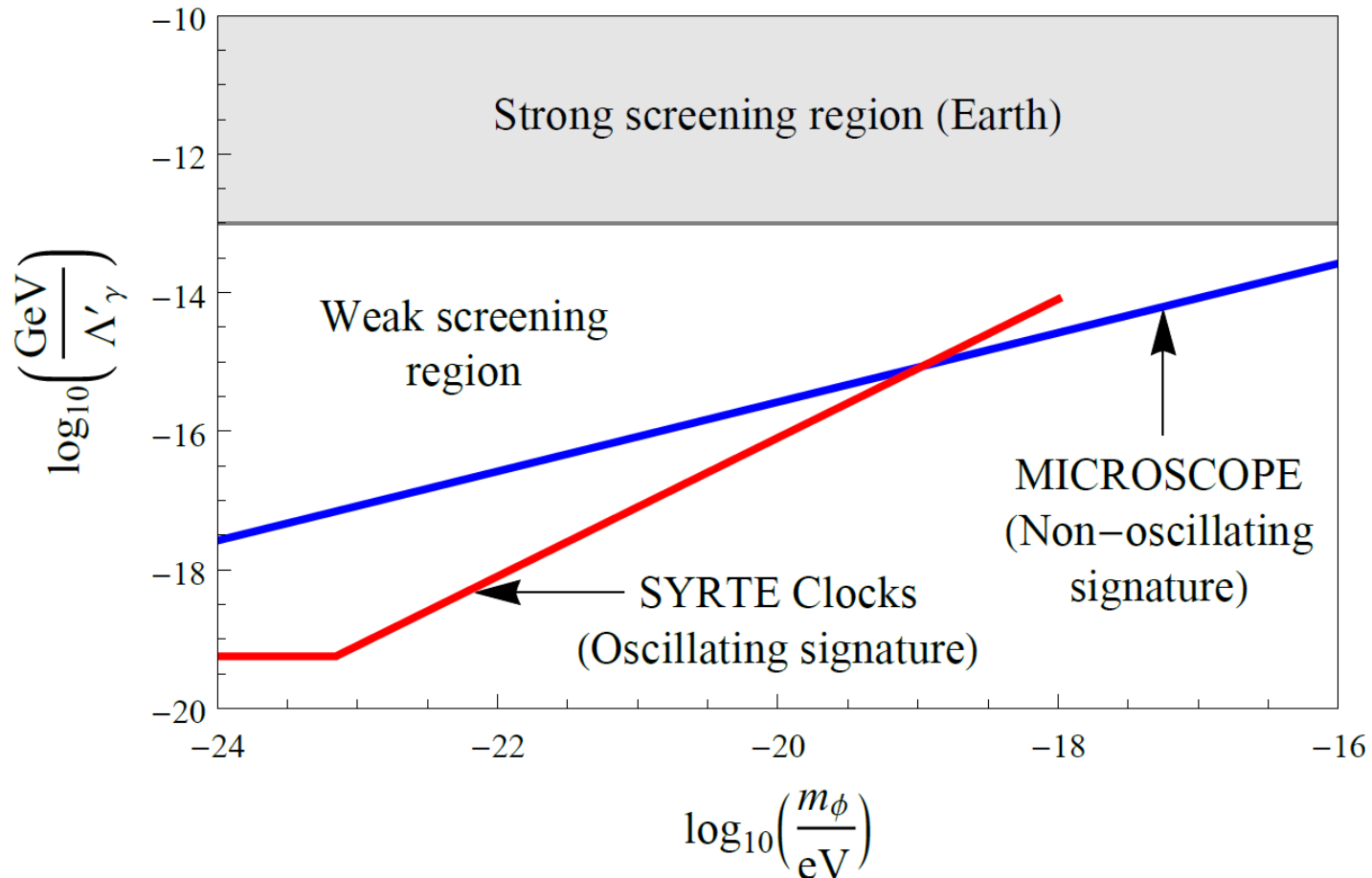
$$V(\varphi) = \frac{m_\varphi^2 \varphi^2}{2}$$

# $\varphi^2$ Interaction of Oscillating Scalar Dark Matter Field with the Photon

Clock constraints: [Stadnik, Flambaum, *PRL* **115**, 201301 (2015); *PRA* **94**, 022111 (2016)]

MICROSCOPE constraints: [Hees *et al.*, *PRD* **98**, 064051 (2018)]

When screening is sufficiently weak, oscillating signatures tend to dominate



# Summary

- “Back-action” effects of ambient matter onto the scalar field in models of topological defects with  $\varphi^2$  interactions induce “quasi-non-transient” variations of the fundamental constants
- Using data from accelerometers and clock-comparison experiments to search for these quasi-non-transient signatures, we’ve obtained more stringent limits than previous bounds from *complementary types of transient and non-transient signatures* (by up to **15 orders of magnitude**)
- Previous clock-based searches for transient signatures of passing domain walls may have assumed qualitatively incorrect signatures by neglecting “back-action” effects

# Back-Up Slides

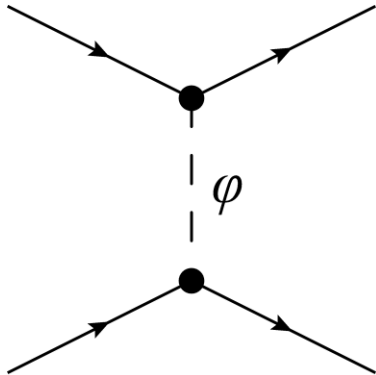
# Fifth Forces: Linear vs Quadratic Couplings

[Hees, Minazzoli, Savalle, Stadnik, Wolf, *PRD* **98**, 064051 (2018)]

Consider the effect of a massive body (e.g., Earth) on the scalar DM field

**Linear couplings ( $\varphi\bar{X}X$ )**

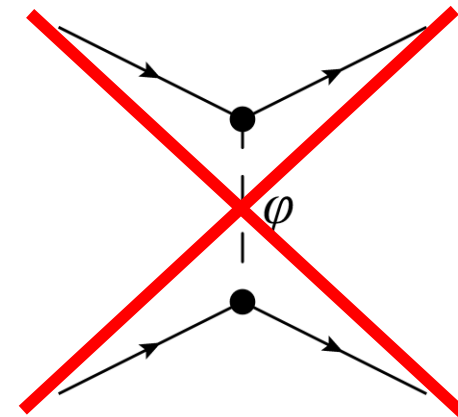
$$\square\varphi + m_\varphi^2\varphi = \pm\kappa\rho \quad \text{Source term}$$



$$\varphi = \varphi_0 \cos(m_\varphi t) \pm A \frac{e^{-m_\varphi r}}{r}$$

**Quadratic couplings ( $\varphi^2\bar{X}X$ )**

$$\square\varphi + m_\varphi^2\varphi = \pm\kappa'\rho\varphi \quad \text{Potential term}$$



$$\varphi = \varphi_0 \cos(m_\varphi t) \left( 1 \pm \frac{B}{r} \right)$$



**Gradients + amplification/screening**



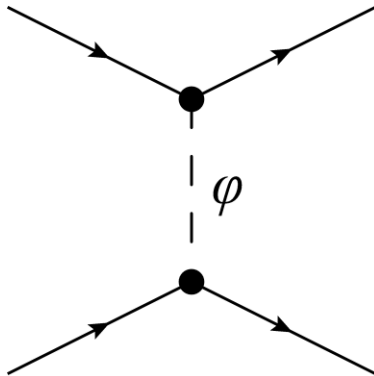
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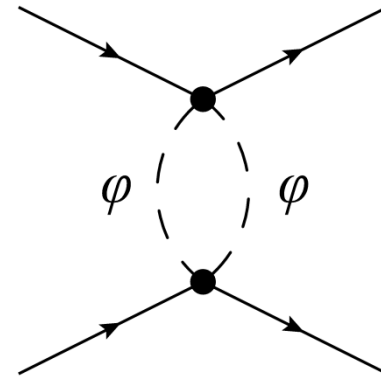
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$$\varphi = \varphi_0 \cos(m_\varphi t) \left( 1 \pm \frac{B}{r} \right) - C \frac{e^{-2m_\varphi r}}{r^3}$$

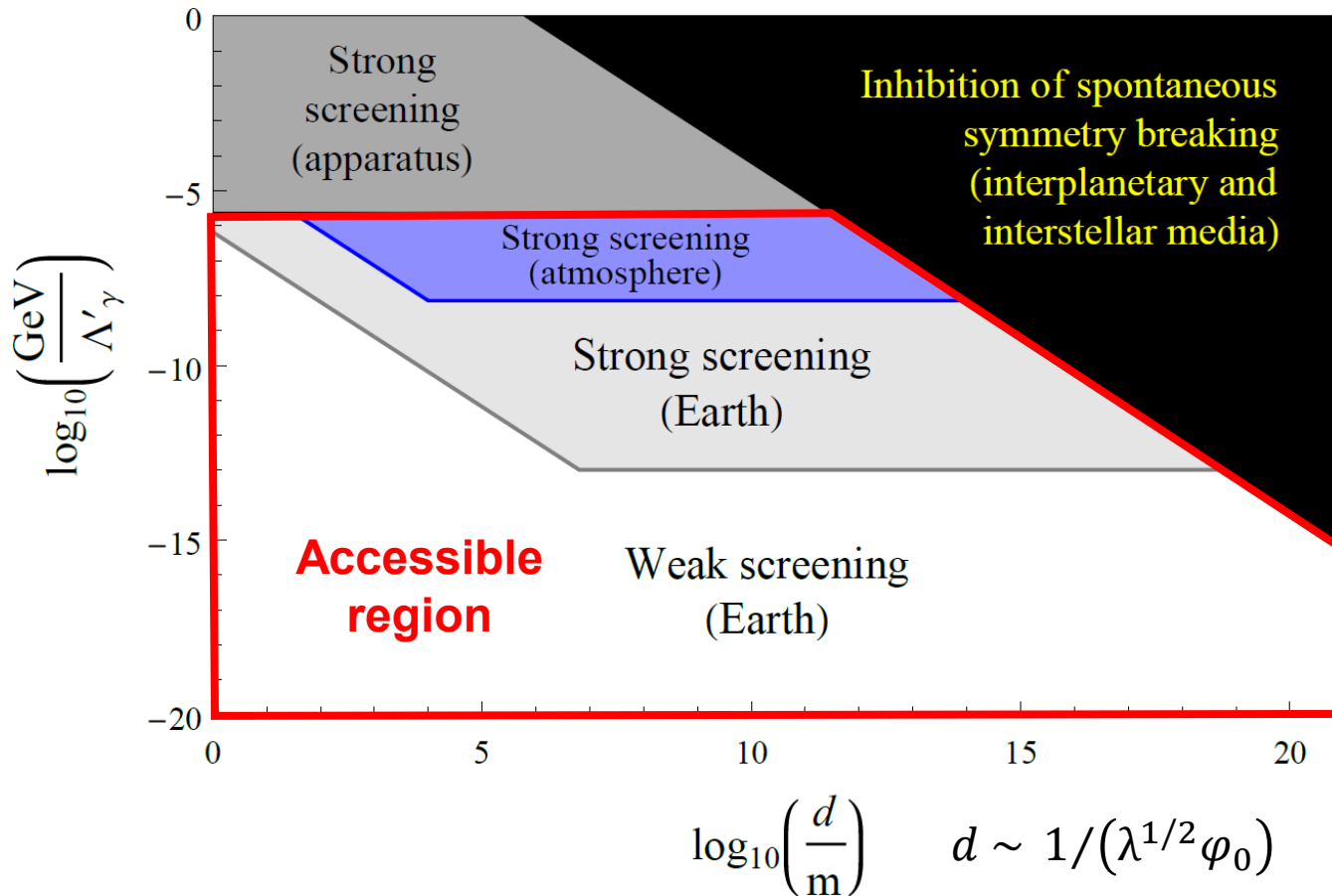


**Gradients + amplification/screening**

# Screening of Scalar Field $\varphi$

[Stadnik, *PRD* **102**, 115016 (2020)]

$$V_{\text{eff}}(\varphi) = \frac{\lambda}{4} (\varphi^2 - \varphi_0^2)^2 + \sum_{X=\gamma, e, N} \frac{\rho_X \varphi^2}{(\Lambda'_X)^2}$$



# Interpretation of Single-Clock-Type Experiments

[Stadnik, *PRD* **102**, 115016 (2020)]

- The Tokyo Skytree experiment measured the gravitational potential difference between a pair of Sr optical clocks separated by a height difference of  $\Delta h \approx 450$  m; for details, see: [Takamoto *et al.*, *Nature Photonics* **14**, 411 (2020) – talk in our Tuesday session]
- To distinguish the effects of a scalar field  $\varphi$  from the usual gravitational redshift effect, can “reference” a single pair of clocks against a combination of laser-ranging and gravimeter measurements (which provide an independent prediction of the clock frequency shift within the framework of relativity)

$$\left. \begin{array}{l} \Delta v_{\text{Sr}} \propto \Delta(m_e \alpha^2) \\ \Delta \mathbf{a}_{\text{grav}} \propto \nabla m_N \end{array} \right\} \Rightarrow \left( \frac{\Delta v_{\text{Sr}}}{v_{\text{Sr}}} \right)_{\text{eff}} \approx \Delta(\varphi^2) \left[ \frac{2}{(\Lambda'_\gamma)^2} + \frac{1}{(\Lambda'_e)^2} - \frac{1}{(\Lambda'_N)^2} \right]$$

# “Dark Matter” Network of Domain Walls?

- **Many open questions and unsubstantiated assumptions!**
- How to increase  $\rho_{\text{walls}}$  inside a galaxy by at least  $\sim 10^5$  times, compared to the density outside of the galaxy?

[Expect wall network to be “stiff”.]

- How to form networks of domain walls that pass through Earth on a “convenient” average timescale,  $T_{\text{avg}}$ , of hours to years?

[Numerical simulations indicate that walls tend to efficiently annihilate over time, leaving only  $\sim \mathcal{O}(1)$  wall at present day.]

- How to form “simple” domain-wall networks with non-relativistic wall speeds in galaxies ( $\sim 300$  km/s locally)?

[Numerical simulations indicate that domain walls travel at semi-relativistic speeds.]