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FRANKFURT AM MAIN

ICRANet  
International Center for Relativistic Astrophysics Network

# Gravitational-wave signatures of the hadron-quark phase transition in binary compact star mergers

*Parallel session: Numerical Relativity and Gravitational Wave Observations  
05.07.2021, 17:50*

*In collaboration with Lukas Weih, Elias R. Most,  
Jens Papenfort, Luke Bovard, Gloria Montana,  
Laura Tolos, Jan Steinheimer, Anton Motornenko,  
Veronica Dexheimer, Horst Stöcker, and Luciano Rezzolla*

MG16  5-10 JULY 2021  
SIXTEENTH MARCEL GROSSMANN MEETING  
ON RECENT DEVELOPMENTS IN THEORETICAL AND EXPERIMENTAL GENERAL RELATIVITY, ASTROPHYSICS AND RELATIVISTIC FIELD THEORIES

**VIRTUAL MEETING**  
websites:  
<http://www.kira.it/mg16/>  
<https://indico.icranet.org/event/1/>  
email:  
mg16@icranet.org  
6:30-19:30 CENTRAL EUROPEAN SUMMER TIME

50TH ANNIVERSARY OF  
"INTRODUCING THE BLACK HOLE"



# Numerical Relativity and Relativistic Hydrodynamics of Binary Neutron Star Mergers

Einstein's theory of general relativity and the resulting general relativistic conservation laws for energy-momentum in connection with the rest-mass conservation are the theoretical groundings of neutron star binary mergers:

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R = 8\pi T_{\mu\nu}$$

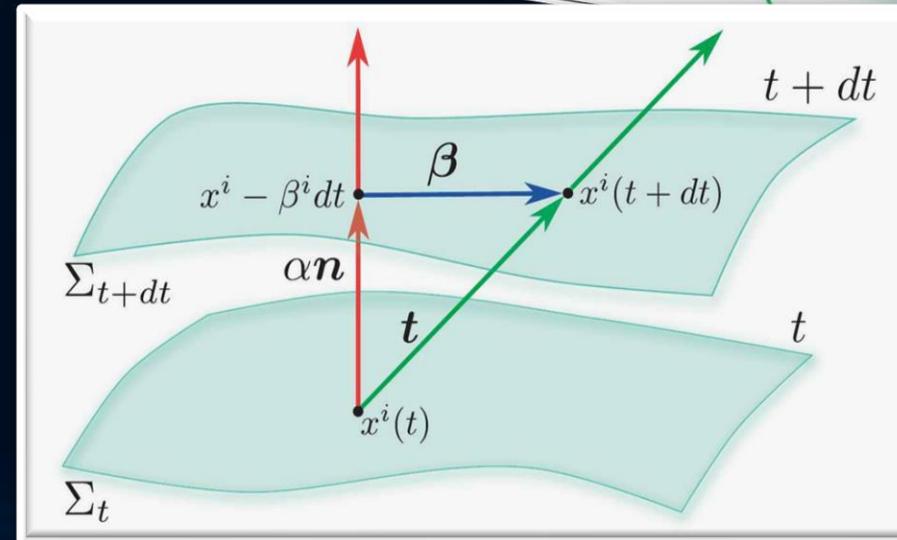
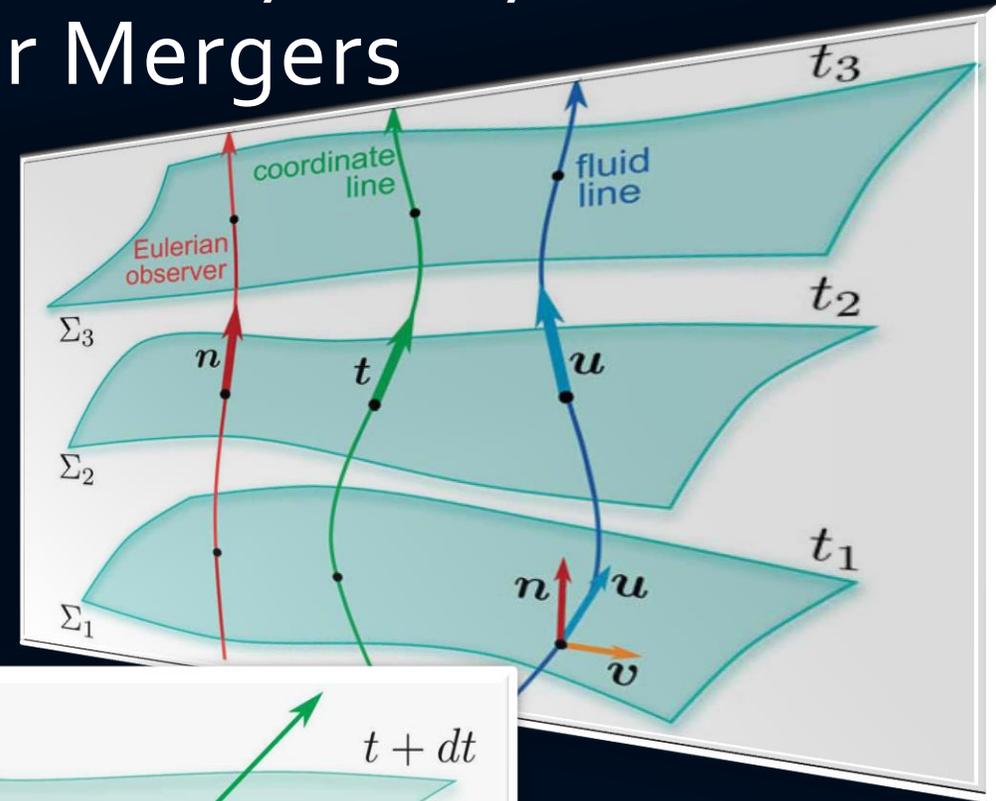
$$\begin{aligned}\nabla_{\mu}(\rho u^{\mu}) &= 0, \\ \nabla_{\nu}T^{\mu\nu} &= 0.\end{aligned}$$

(3+1) decomposition of spacetime

$$g_{\mu\nu} = \begin{pmatrix} -\alpha^2 + \beta_i\beta^i & \beta_i \\ \beta_i & \gamma_{ij} \end{pmatrix}$$

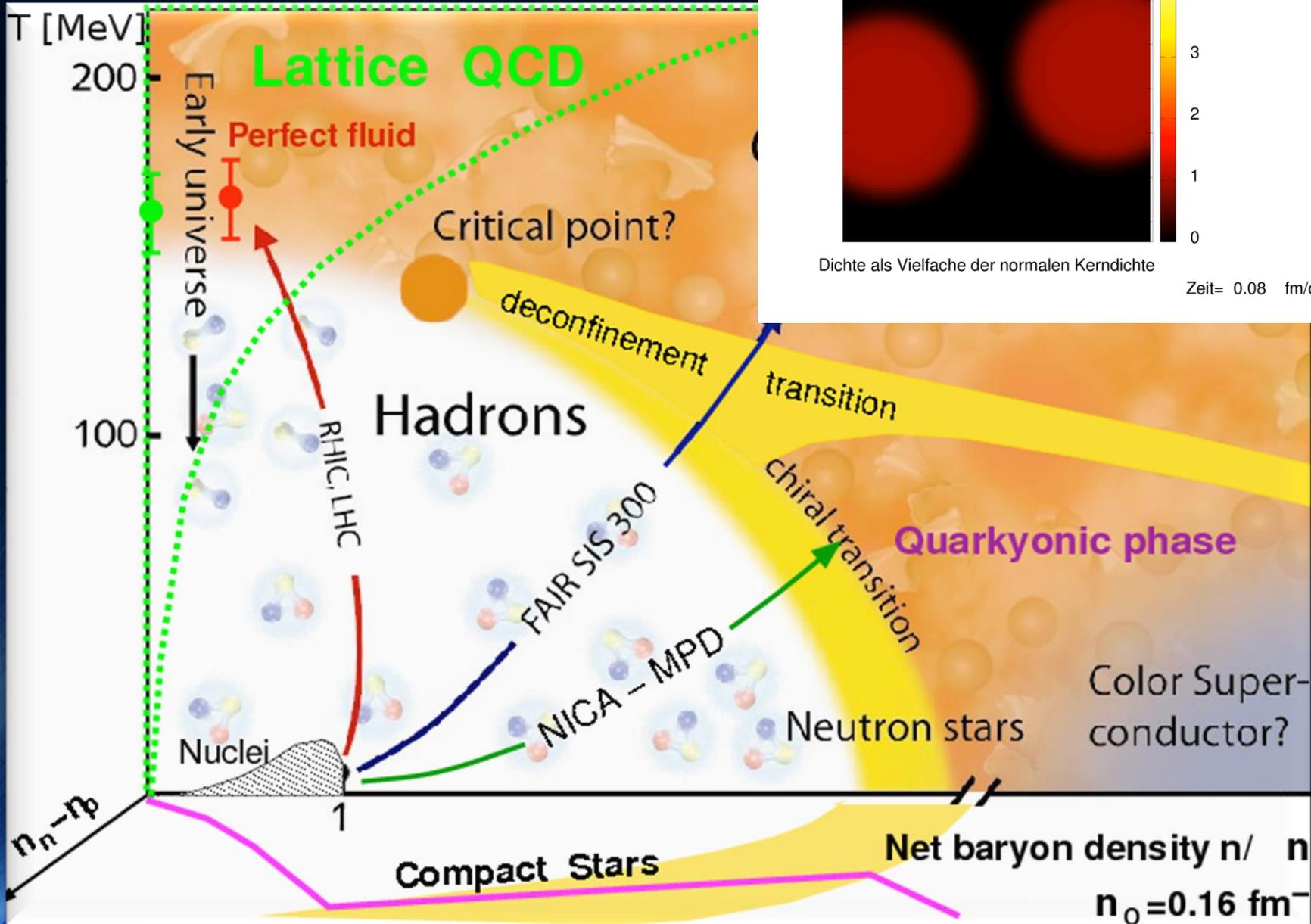
$$d\tau^2 = \alpha^2(t, x^j)dt^2$$

$$x^i_{t+dt} = x^i_t - \beta^i(t, x^j)dt$$

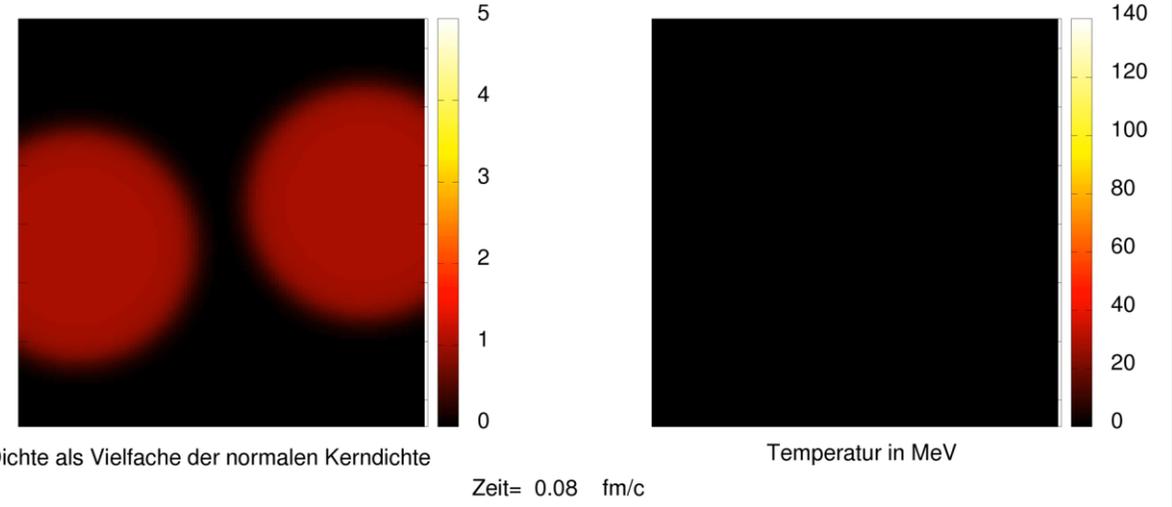


# The Hadron-Quark Phase Transition

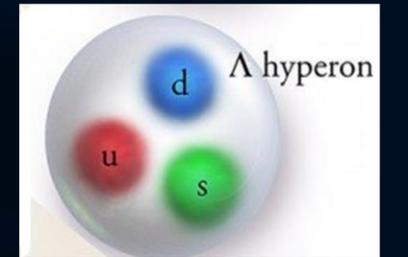
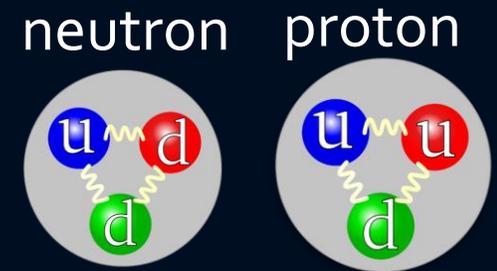
The QCD Phase Diagram



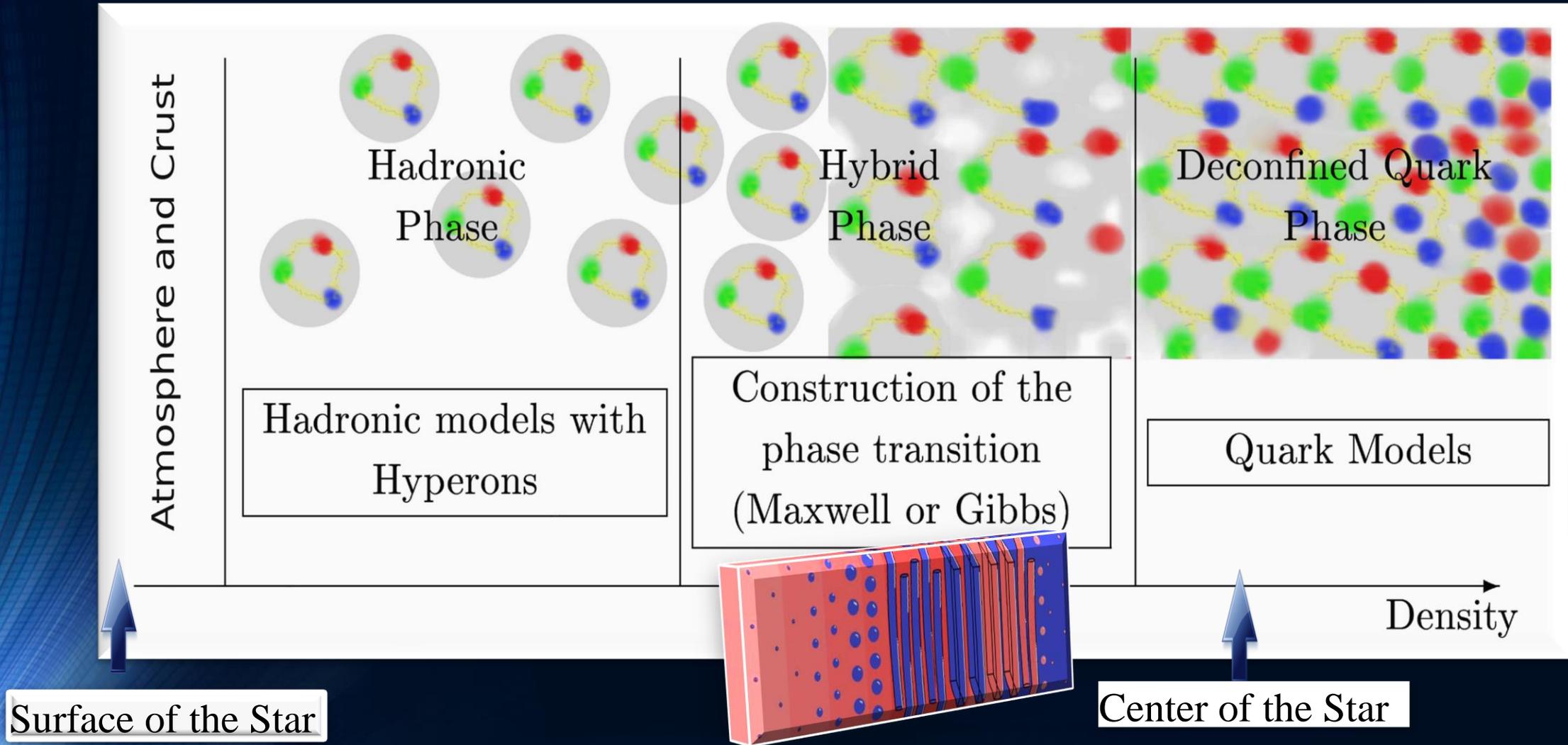
Gold+Gold Kollision am GSI: Helmholtz Zentrum für Schwerionenforschung / HADES Experiment  
Am FAIR Beschleuniger: noch höhere Strahlintensität



Credits:  
Jan Steinheimer



# The QCD – Phase Transition and the Interior of a Hybrid Star



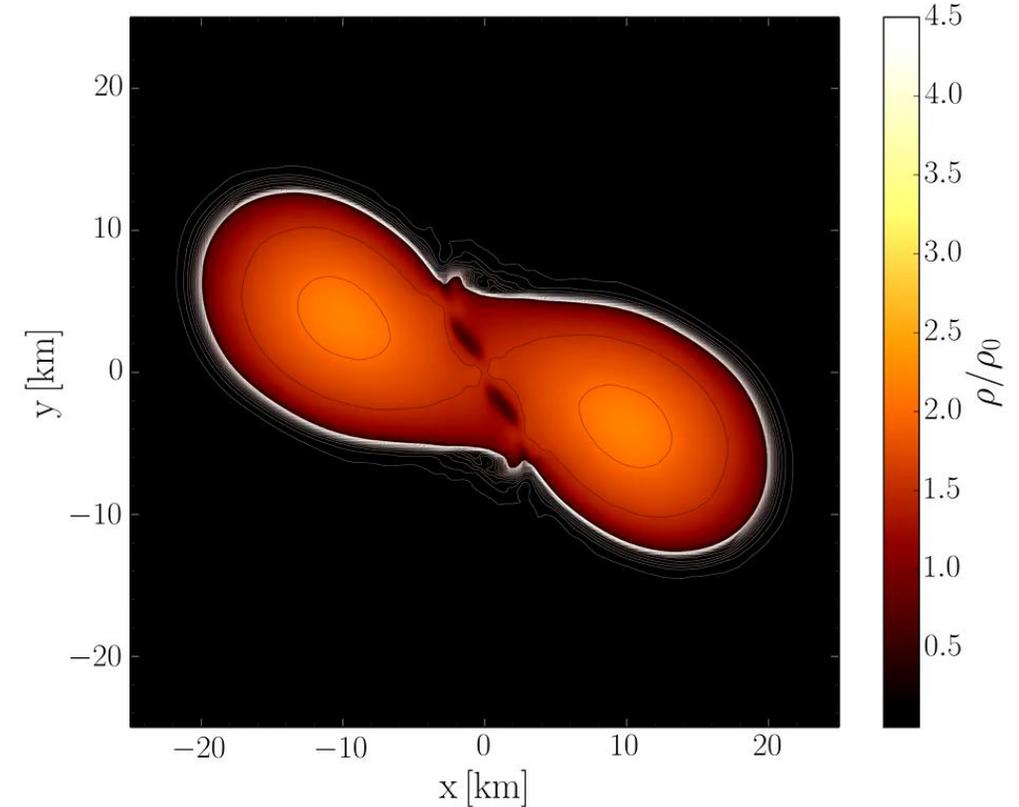
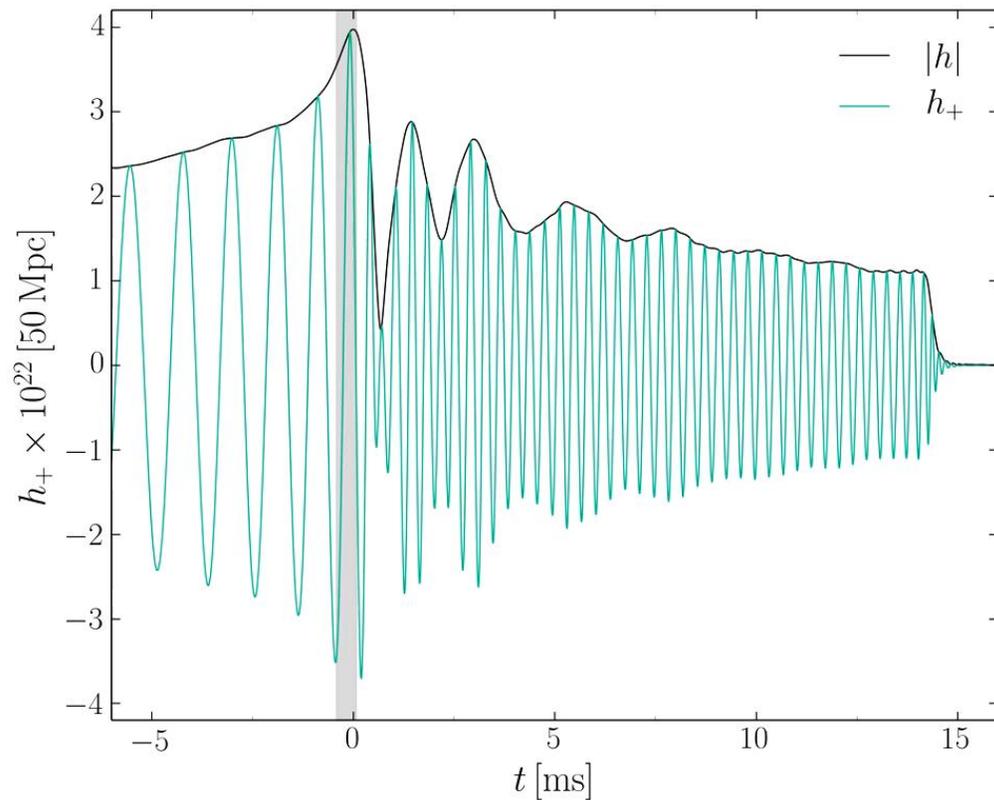
*Matthias Hanauske; Doctoral Thesis:*

*Properties of Compact Stars within QCD-motivated Models; University Library Publication Frankfurt (2004)*

# Gravitational Waves and Hypermassive Hybrid Stars

ALF2-EOS: Mixed phase region starts at  $3\rho_0$  (see red curve), initial NS mass:  $1.35 M_{\text{solar}}$

Hanauske, et.al. PRD, 96(4), 043004 (2017)

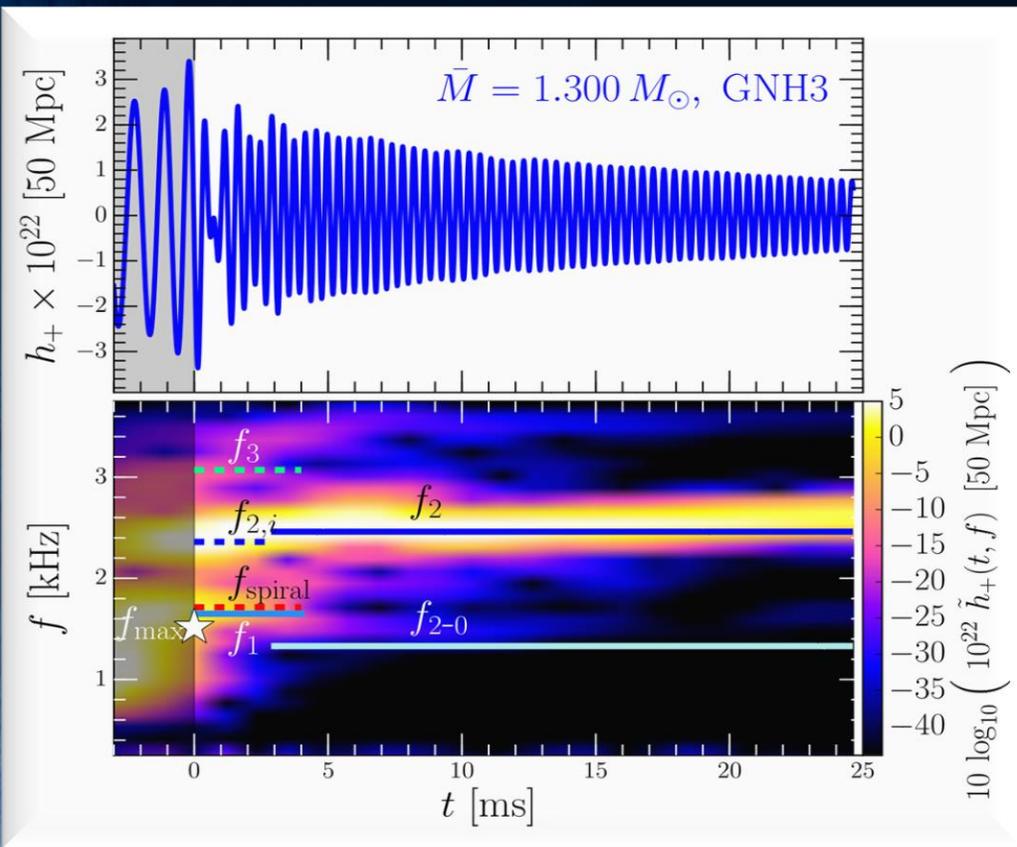


Gravitational wave amplitude  
at a distance of 50 Mpc

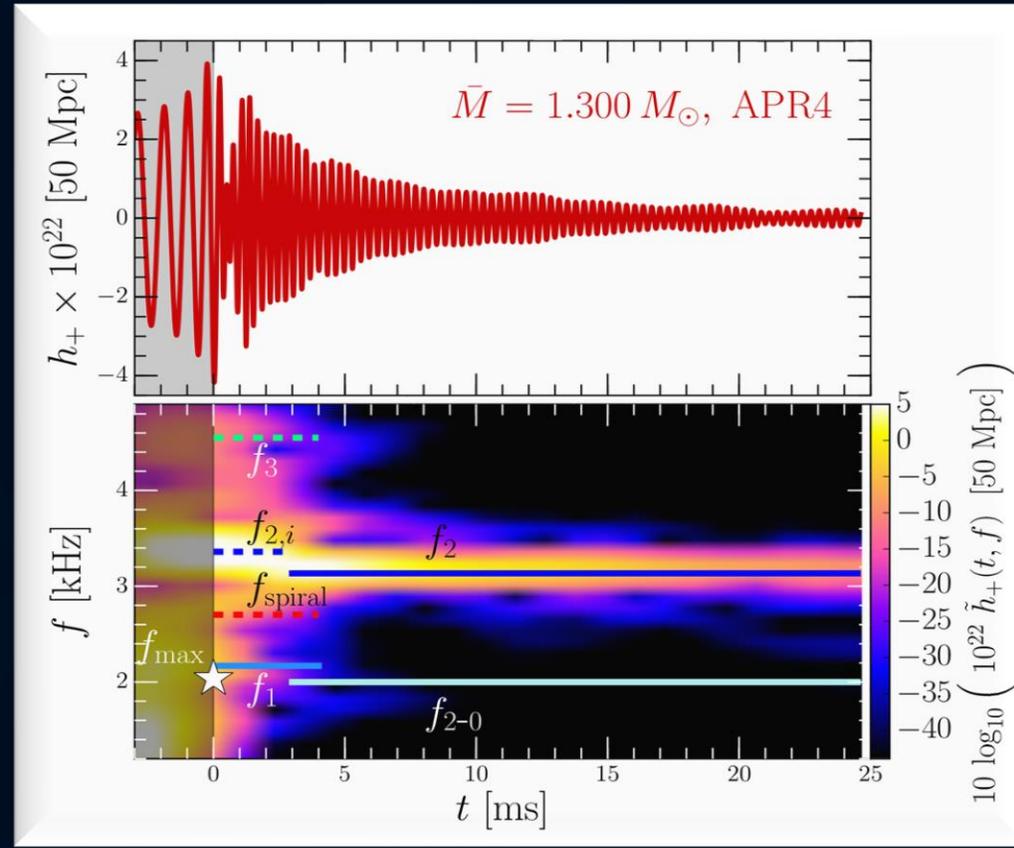
Rest mass density distribution  $\rho(x,y)$   
in the equatorial plane  
in units of the nuclear matter density  $\rho_0$

# Time Evolution of the GW-Spectrum

The power spectral density profile of the post-merger emission is characterized by several distinct frequencies. After approximately 5 ms after merger, the only remaining dominant frequency is the  $f_2$ -frequency (See e.g. L.Rezzolla and K.Takami, PRD, 93(12), 124051 (2016))



Stiff EOS



Soft EOS

Unfortunately, due to the low sensitivity at high gravitational wave frequencies, no post-merger signal has been found in GW170817.

But advanced detectors / next-generation detectors might be able to detect!!?

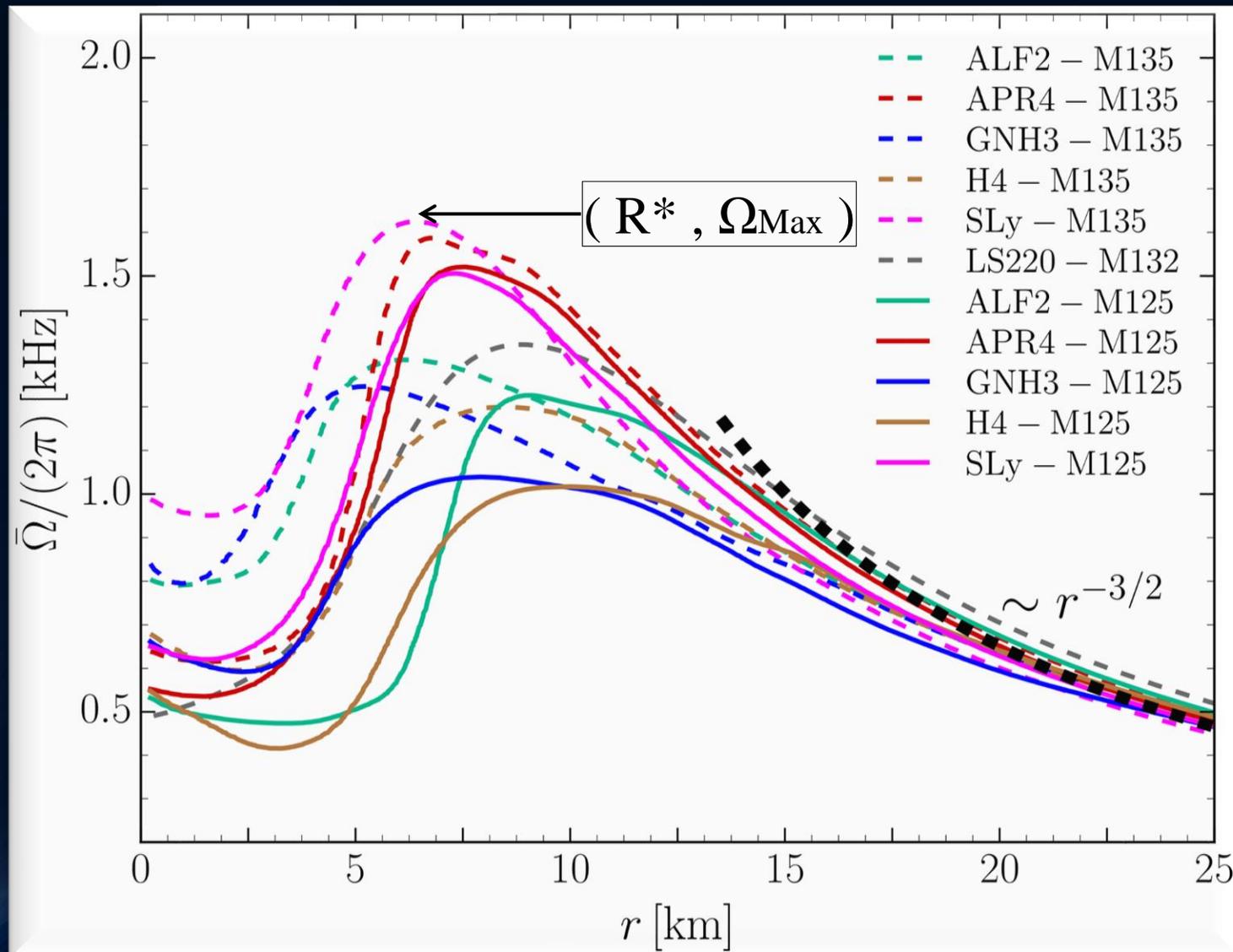
# Time-averaged Rotation Profiles of the HMNSs

Talk on  
Thursday

*On the properties  
of metastable  
hypermassive  
hybrid stars*

*Parallel session*

*Neutron stars: Dense  
matter in compact stars,  
08.07.2021, 18:10*



Soft EoSs:

Sly  
APR4

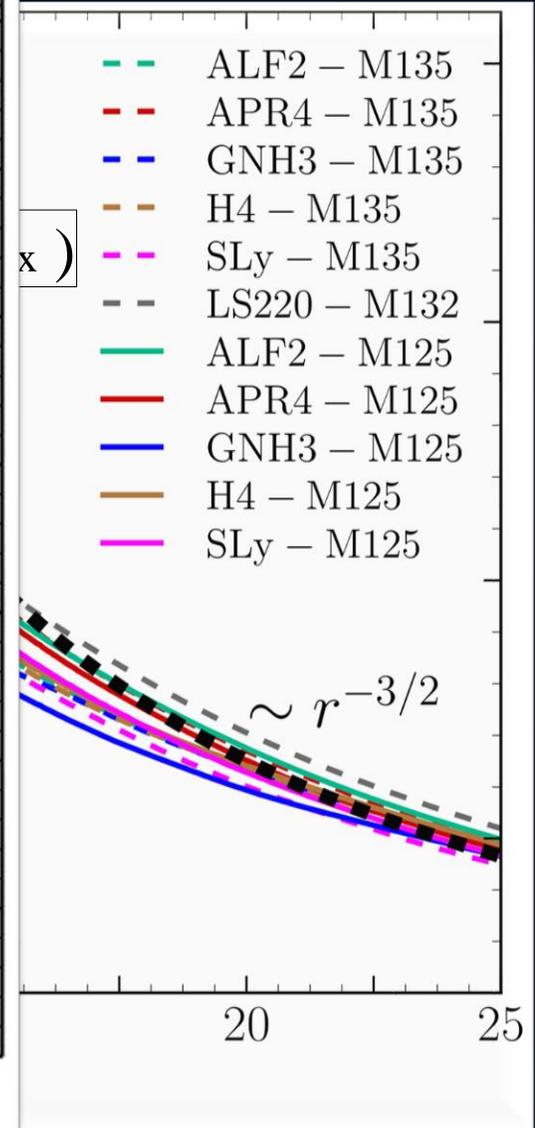
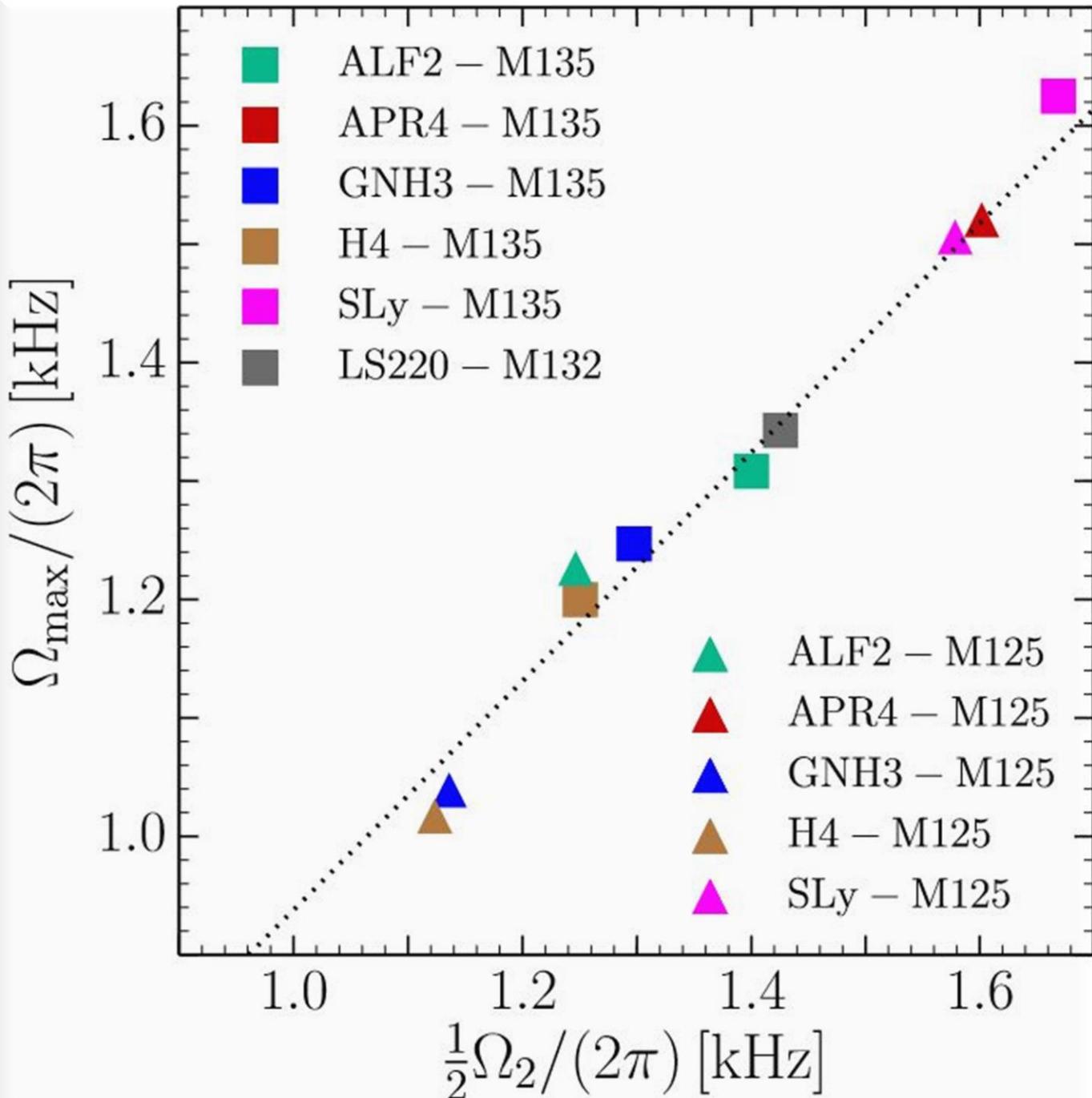
Stiff EoSs:

GNH3  
H4

Time-averaged rotation profiles for different EoS  
Low mass runs (solid curves), high mass runs (dashed curves).

Hanuske, et.al. PRD, 96(4), 043004 (2017)

# files of the HMNSs



Soft EoSs:  
Sly  
APR4

Stiff EoSs:  
GNH3  
H4

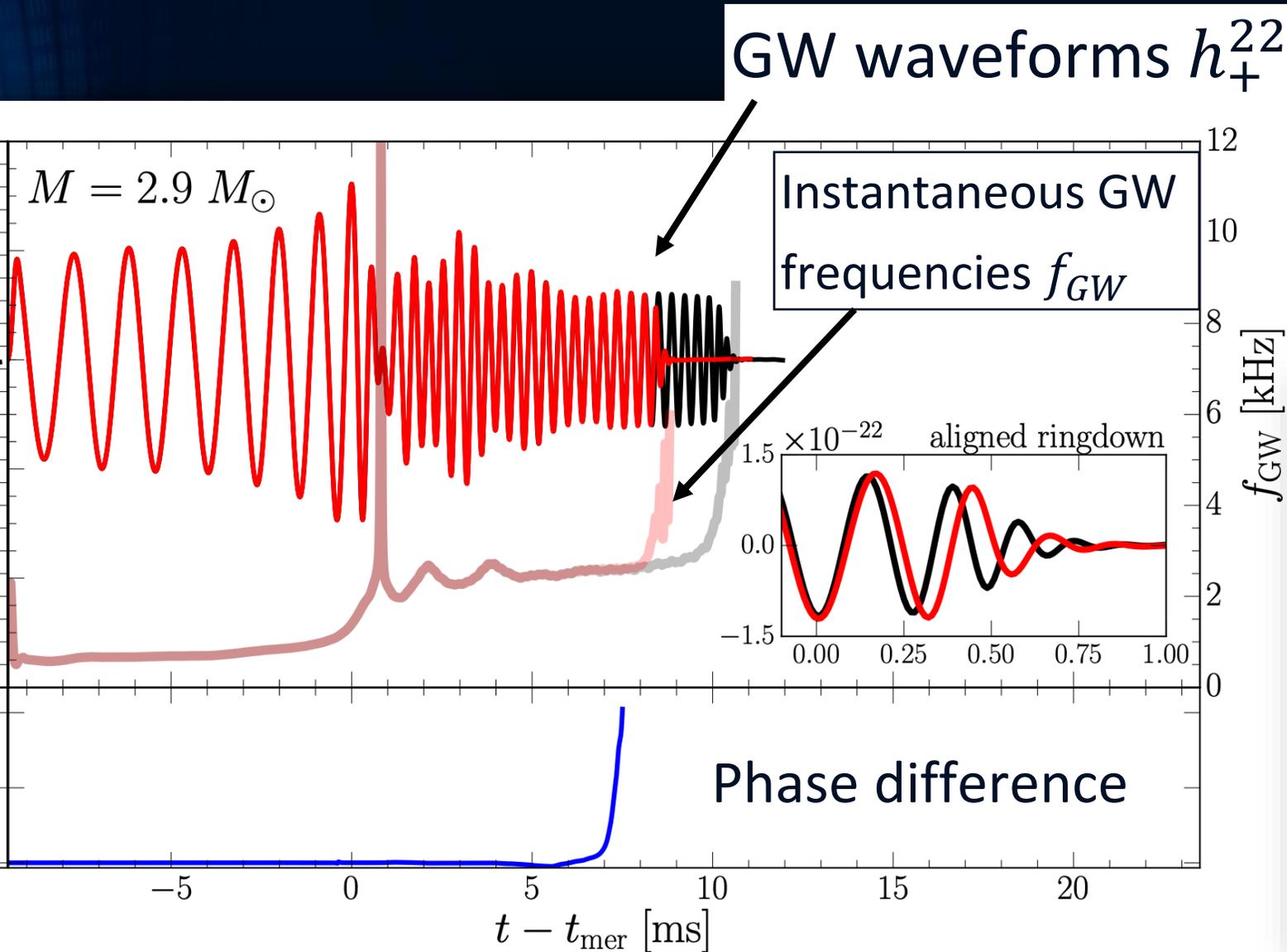
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  - Signatures within the late inspiral phase (premerger signals)
    - Constraining twin stars with GW170817; G Montana, L Tolós, M Hanauske, L Rezzolla; Physical Review D 99 (10), 103009 (2019)
  - Signatures within the post-merger phase evolution
    - **Phase-transition triggered collapse scenario**  
Signatures of quark-hadron phase transitions in general-relativistic neutron-star mergers; ER Most, LJ Papenfort, V Dexheimer, M Hanauske, S Schramm, H Stöcker, L. Rezzolla; Physical review letters 122 (6), 061101 (2019)
    - **Delayed phase transition scenario**  
Postmerger Gravitational-Wave Signatures of Phase Transitions in Binary Mergers; LR Weih, M Hanauske, L Rezzolla; Physical Review Letters 124 (17), 171103 (2020)
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# Signatures within the post-merger phase

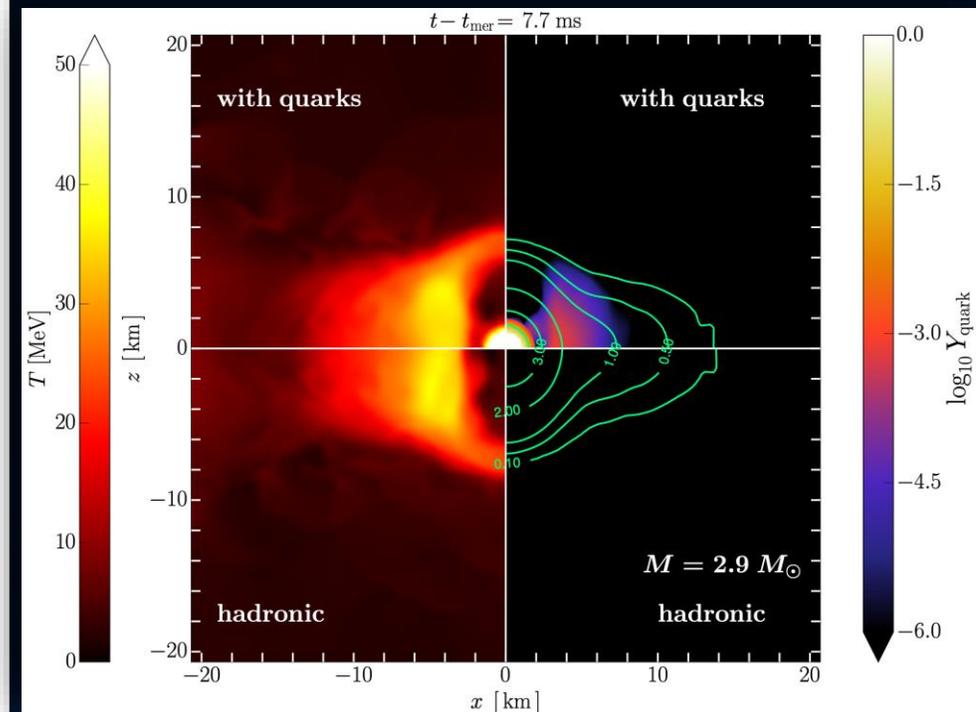
## Phase-transition triggered collapse scenario



ER Most et.al., PRL 122 (6), 061101 (2019)

EOS based on Chiral Mean Field (CMF) model, based on a nonlinear SU(3) sigma model with (red) and without (black) phase transition.

Phase transition leads to a very hot and dense quark core that, when it collapses to a black hole, produces a ringdown signal different from the hadronic one.

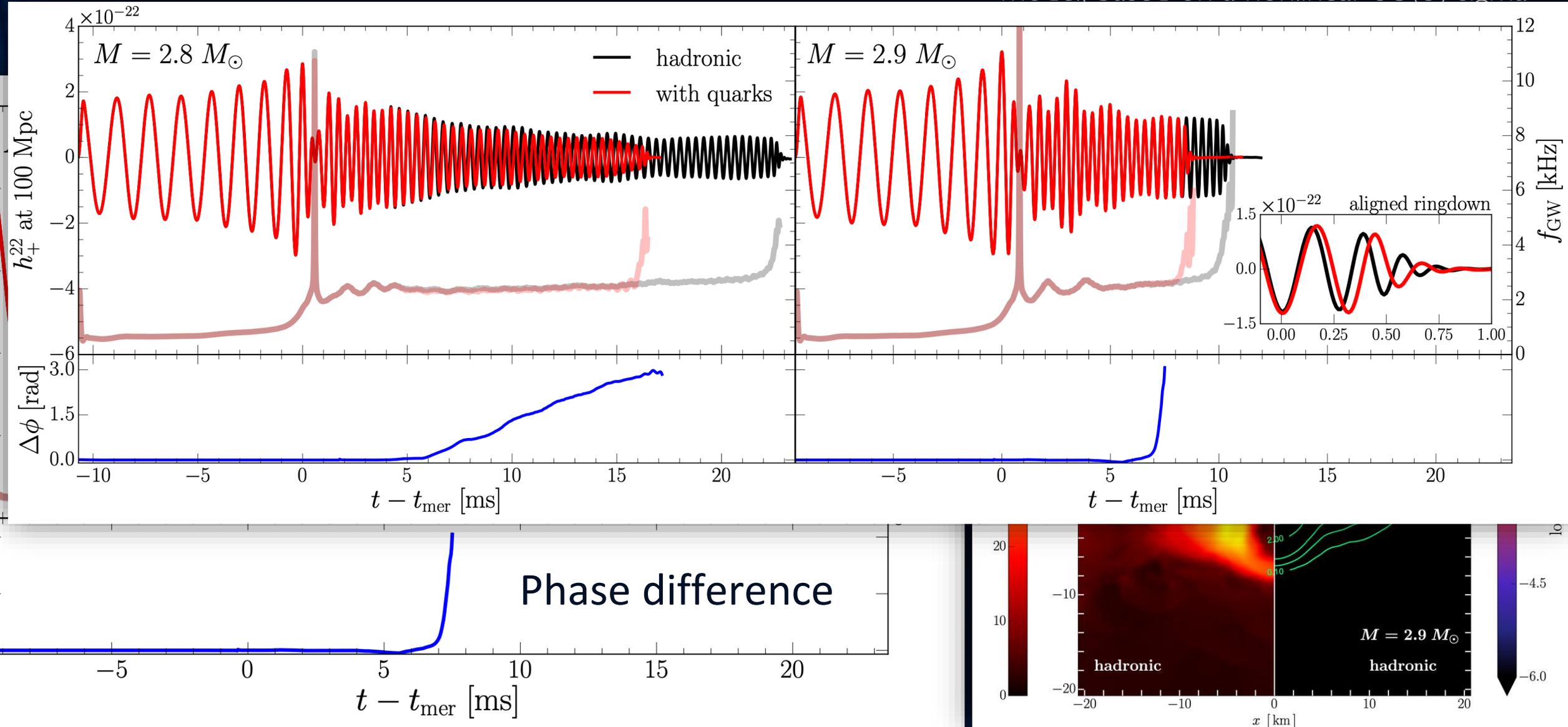


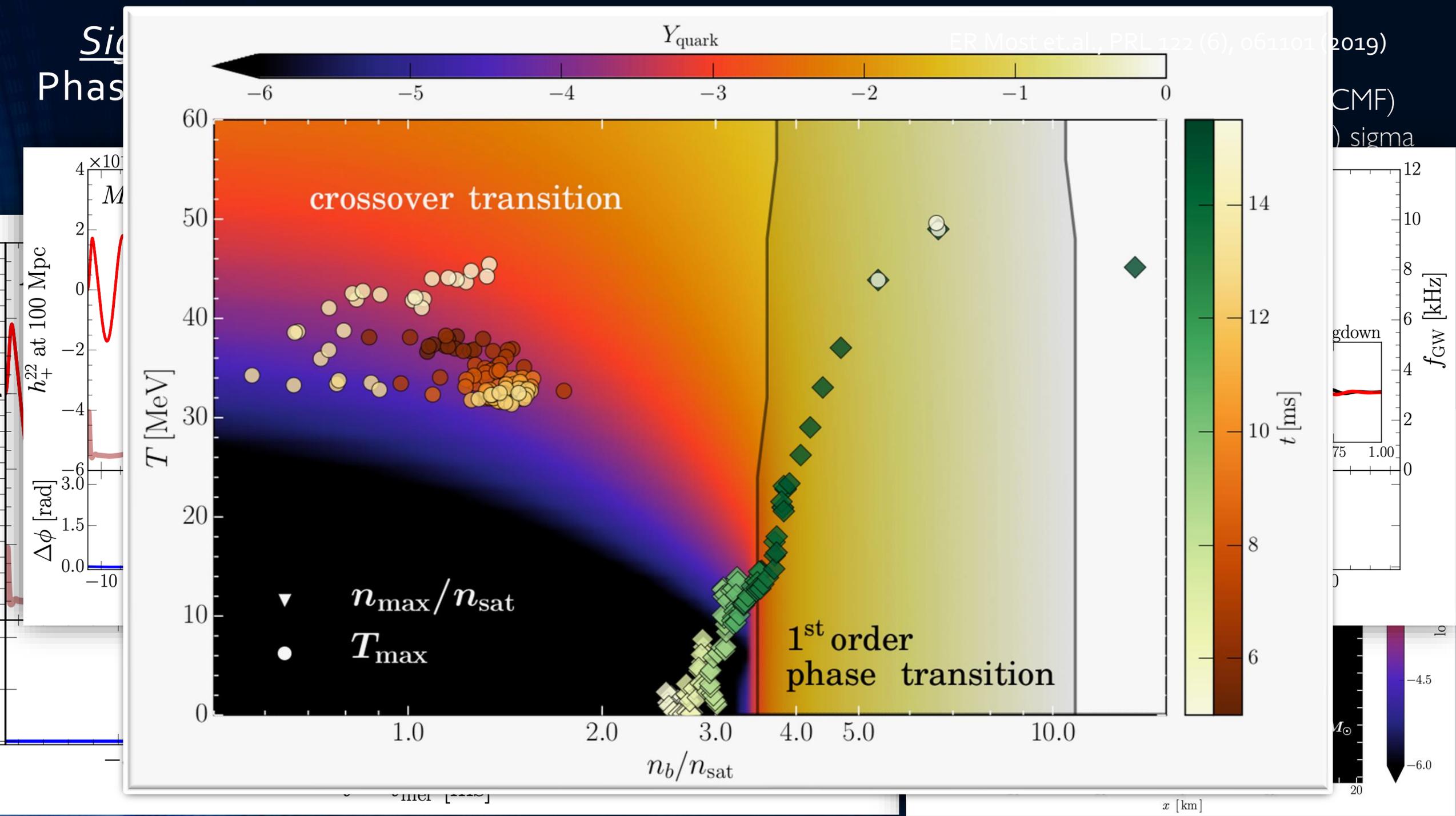
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EOS based on Chiral Mean Field (CMF) model, based on a nonlinear SU(3) sigma





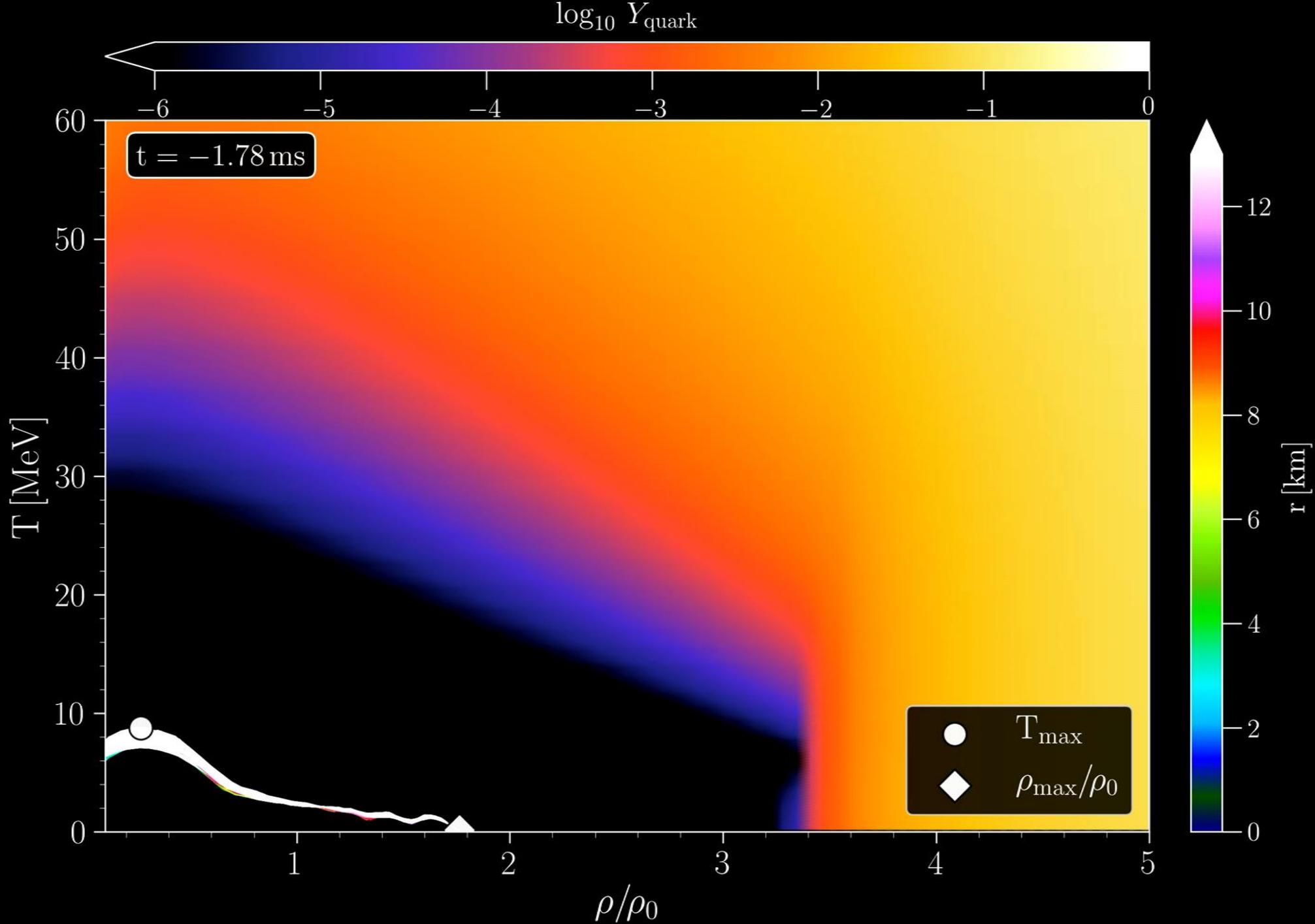
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*Signatures of quark-hadron phase transitions in general-relativistic neutron-star mergers*

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Physical review letters 122 (6), 061101 (2019)

Density-Temperature-Composition dependent EOS within the CMF<sub>0</sub> model. Simulation of total mass  $M=2.8 M_{\text{solar}}$



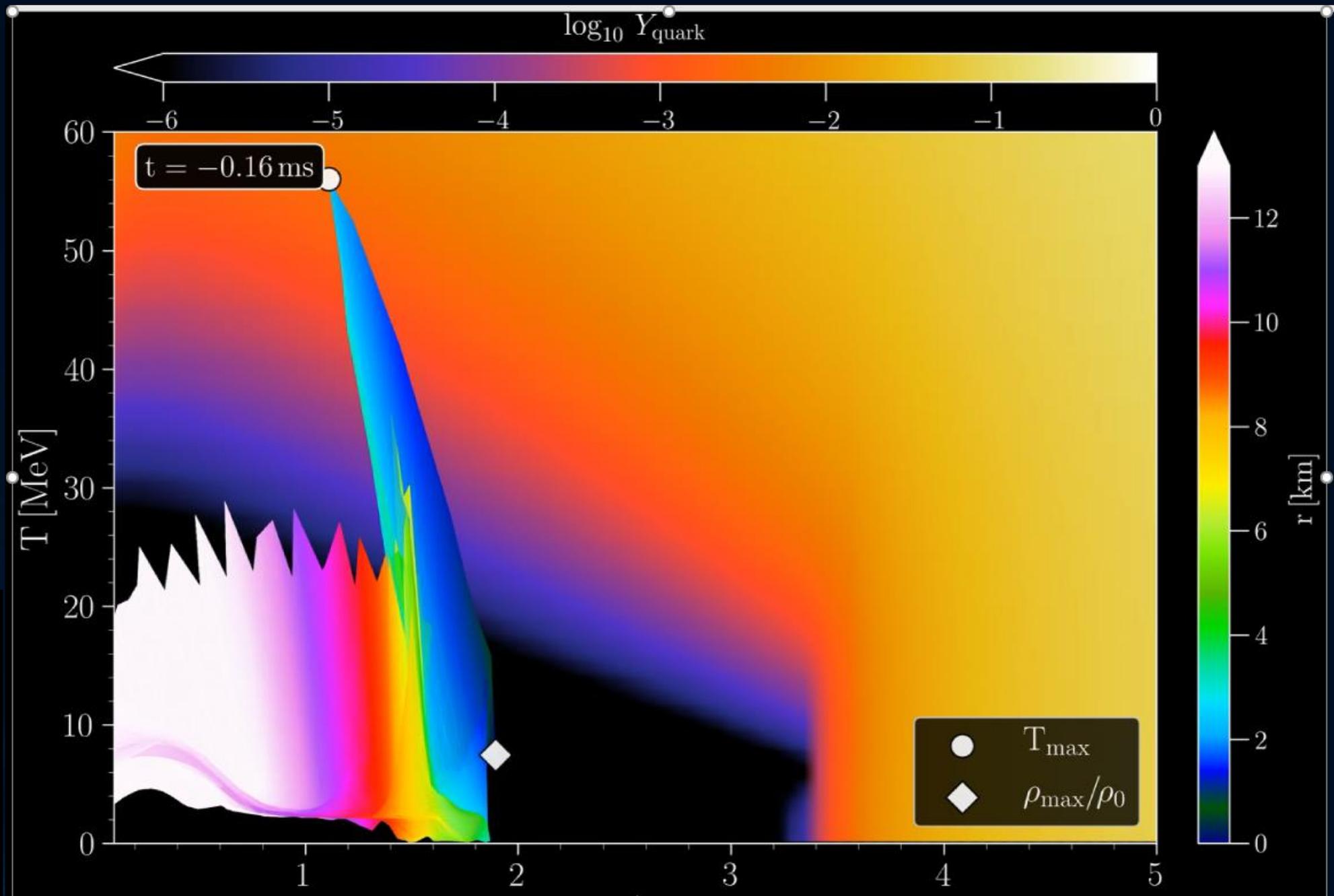
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Physical review letters 122 (6), 061101 (2019)

Density-Temperature-Composition dependent EOS within the CMF0 model. Simulation of total mass  $M=2.8 M_{\text{solar}}$



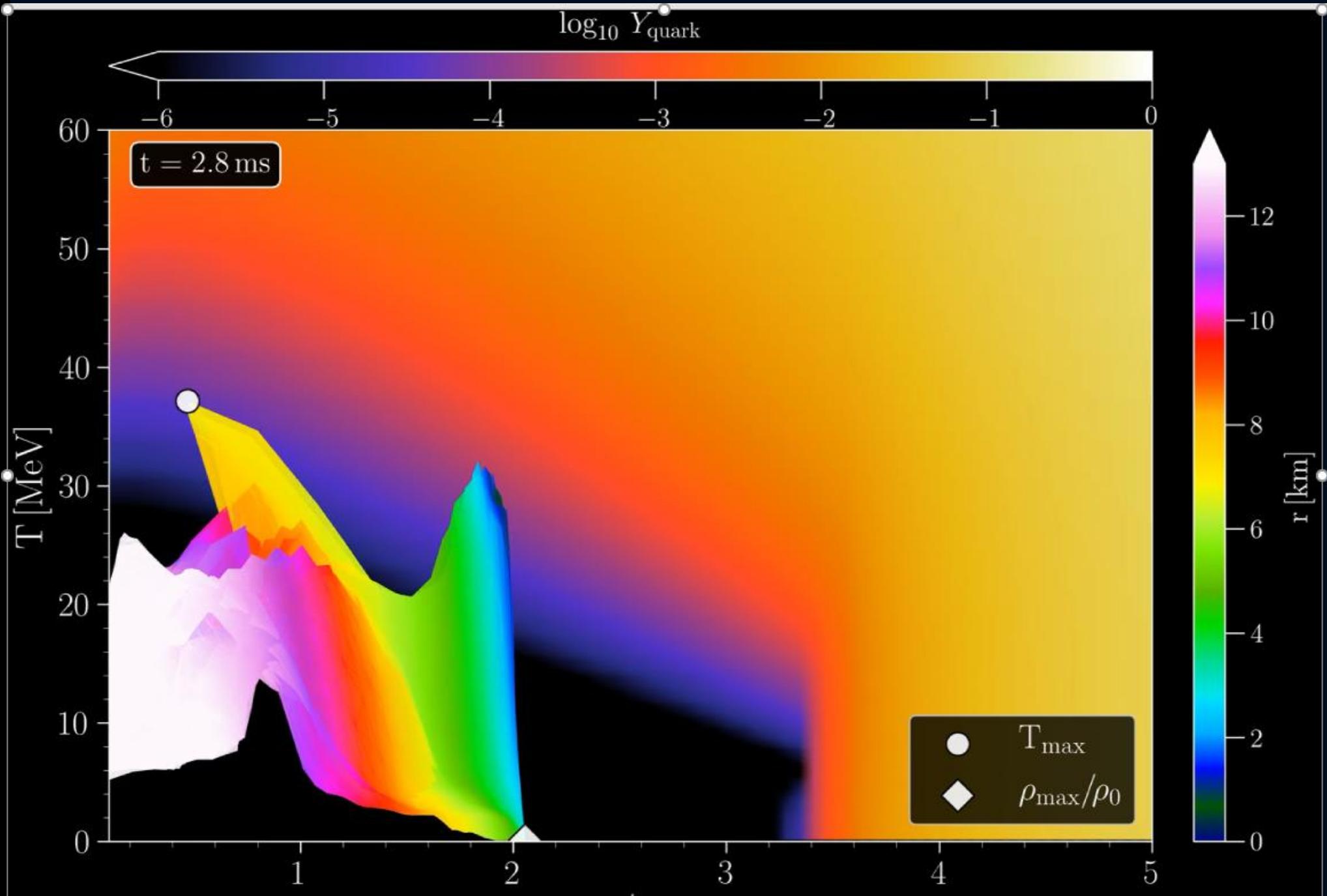
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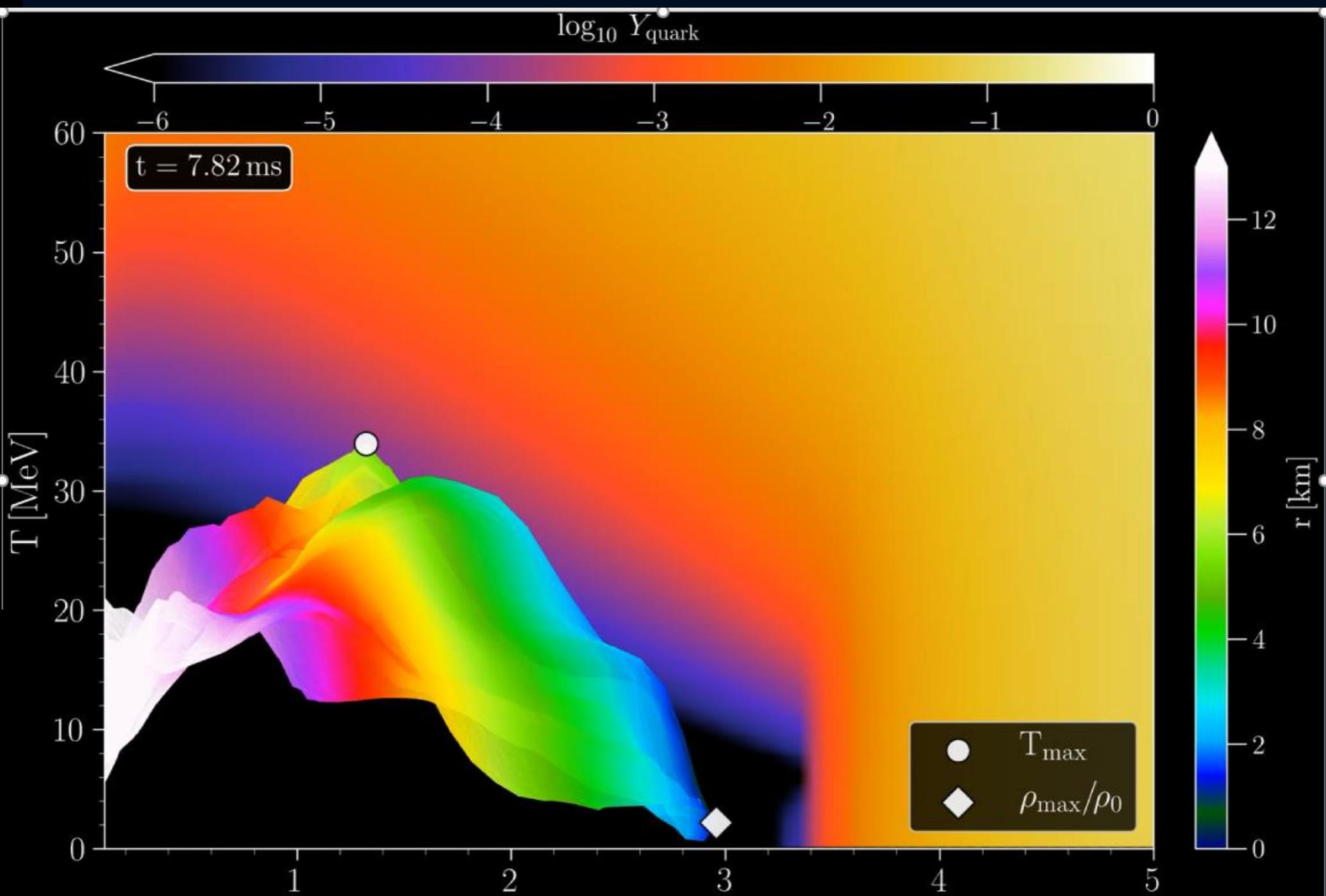
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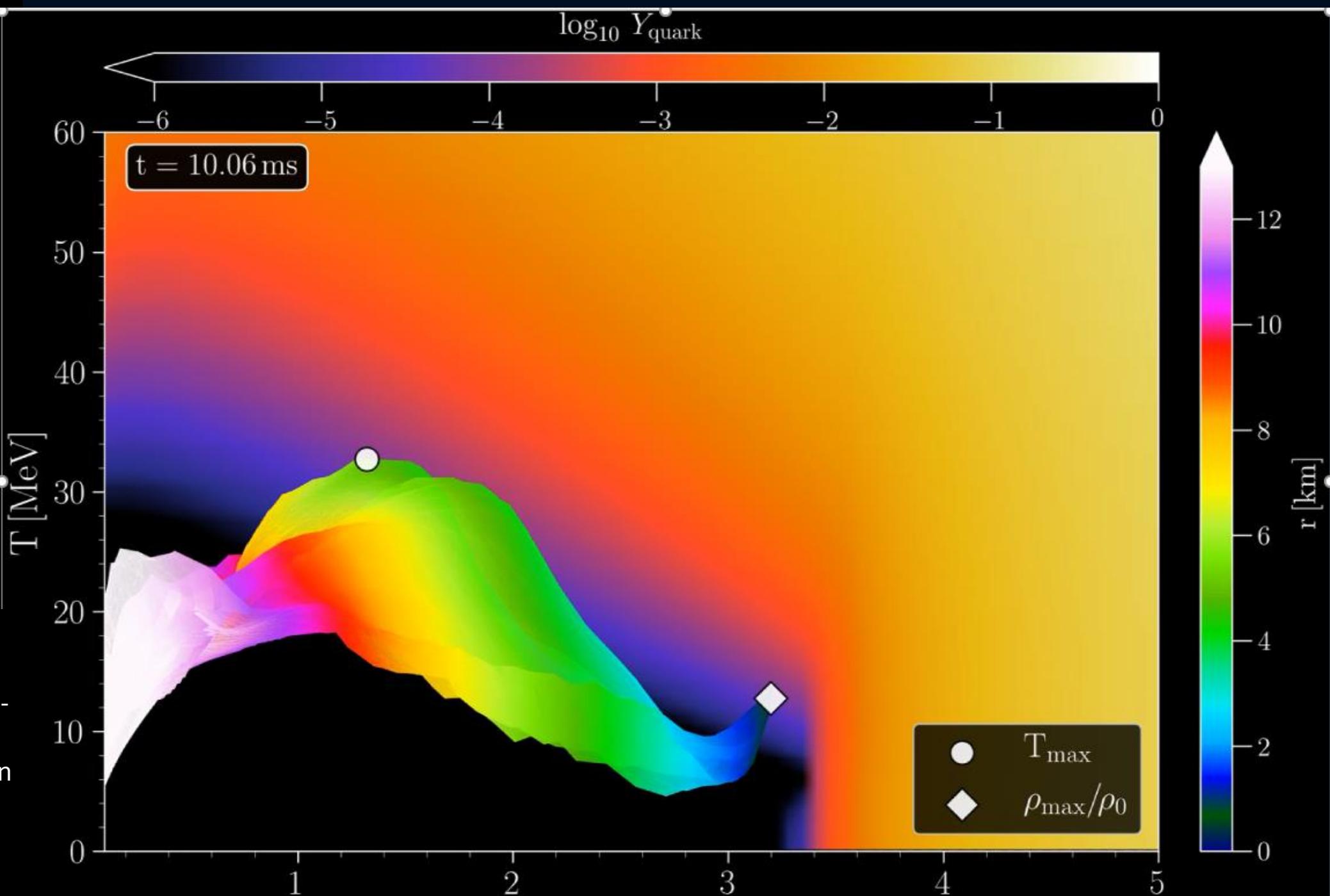
# Phase-transition triggered collapse scenario

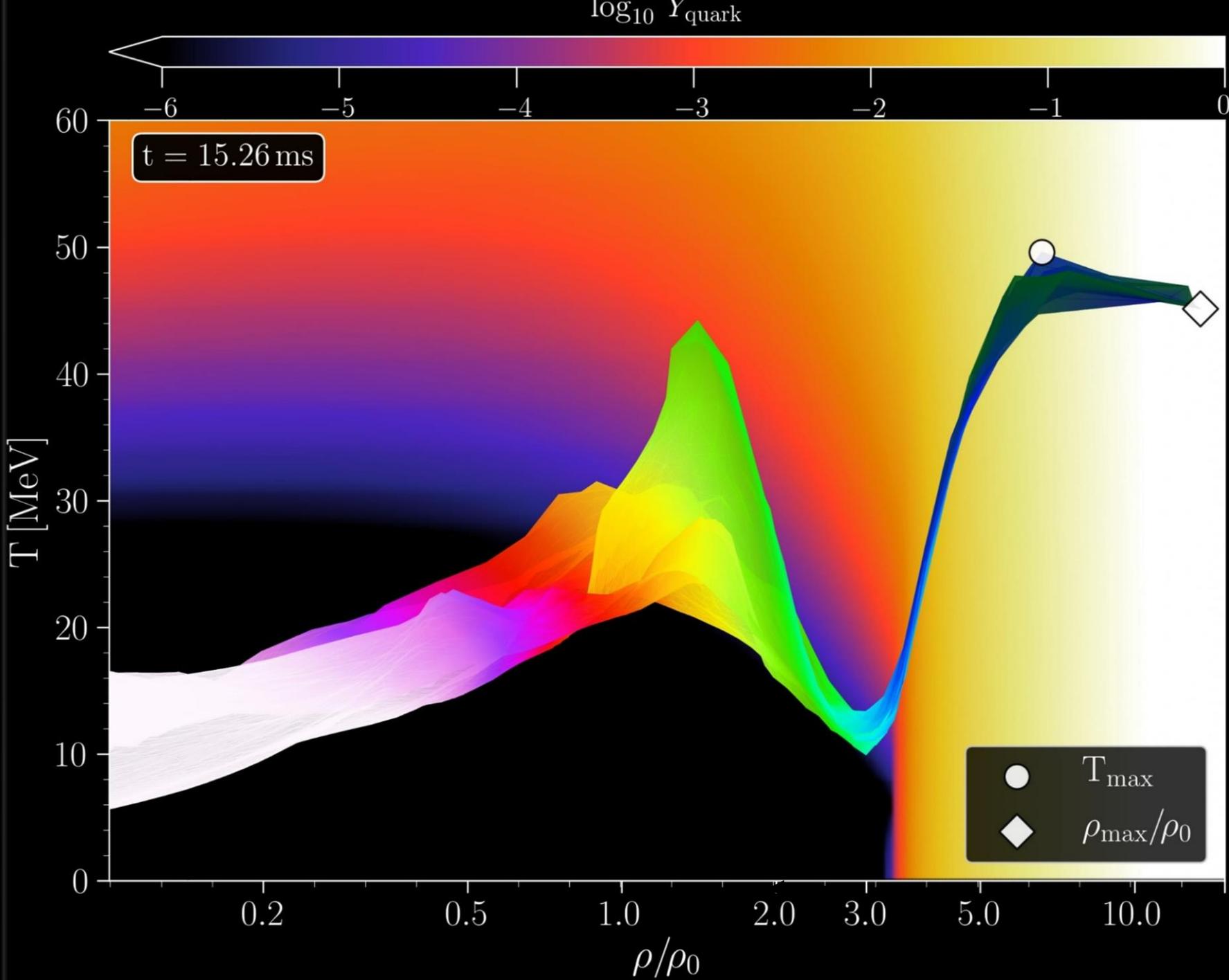
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# The Strange Bird Plot

ER Most, LJ Papenfort, V  
Dexheimer, M Hanauske, S  
Schramm, H Stöcker and L.  
Rezzolla,  
*Signatures of quark-hadron phase  
transitions in general-relativistic  
neutron-star mergers*  
Physical review letters  
122 (6), 061101 (2019)

E. Most, J. Papenfort,  
V. Dexheimer, M. Hanauske,  
H. Stöcker and L. Rezzolla,  
*On the deconfinement phase  
transition in neutron-star mergers*  
The European Physical Journal A  
56 (2), 1-11 (2020)

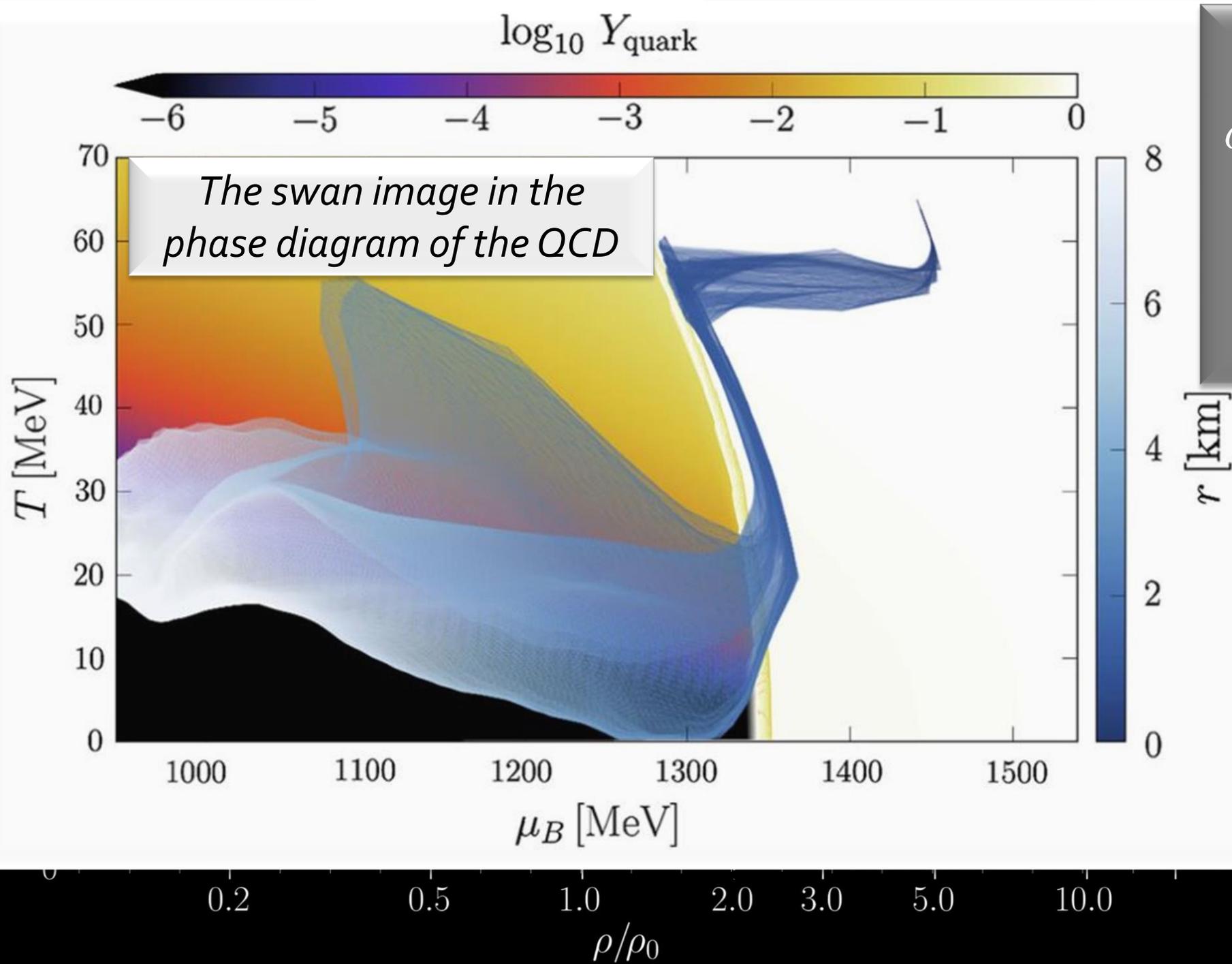
A. Motorenko, M. Hanauske,  
L. Weih, J. Steinheimer and  
H. Stöcker, *MAGIC: Matter in  
Astrophysics, Gravitational Waves,  
and Ion Collisions. 原子核物理评  
论*, 37(3), 272-282 (2020)

## Talk on Thursday

*On the properties of metastable  
hypermassive hybrid stars*

*Parallel session*

*Neutron stars: Dense matter in compact  
stars, 08.07.2021, 18:10*



E. Most, J. Papenfort,  
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*On the deconfinement phase  
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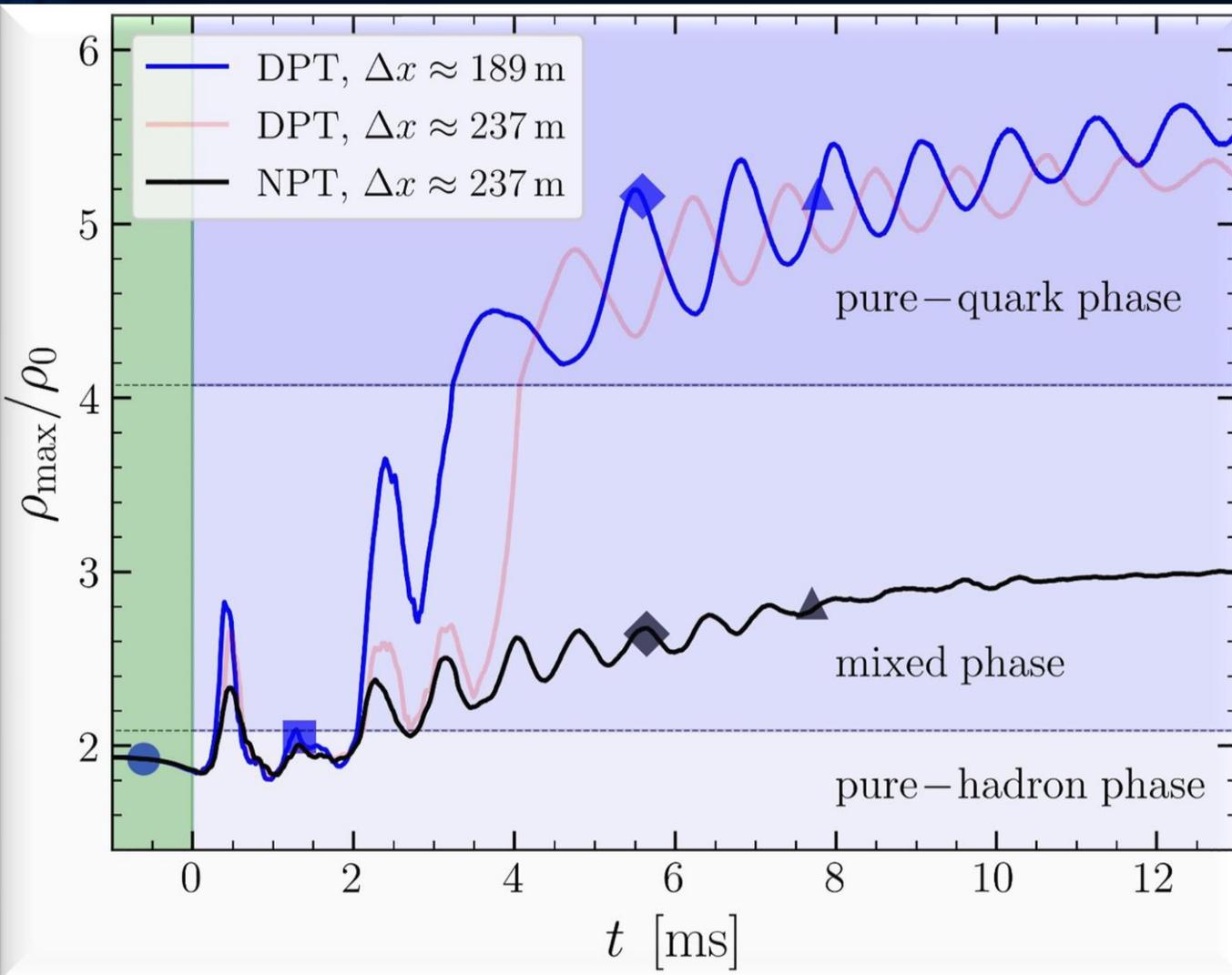
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# Signatures within the post-merger phase evolution

## DPT: Delayed phase transition scenario

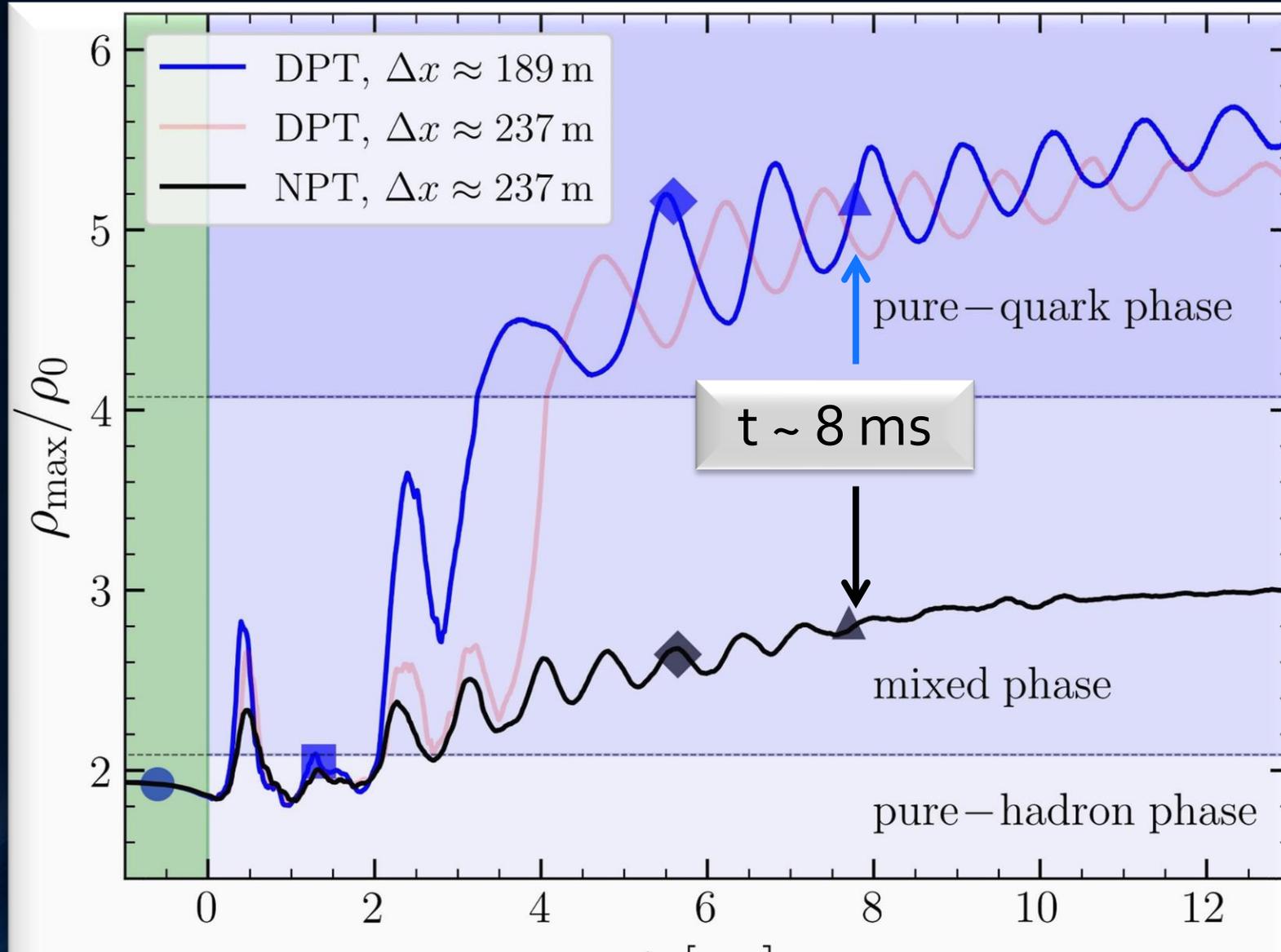
Postmerger Gravitational-Wave Signatures of Phase Transitions in Binary Mergers; LR Weih, M Hanauske, L Rezzolla; Physical Review Letters 124 (17), 171103 (2020)



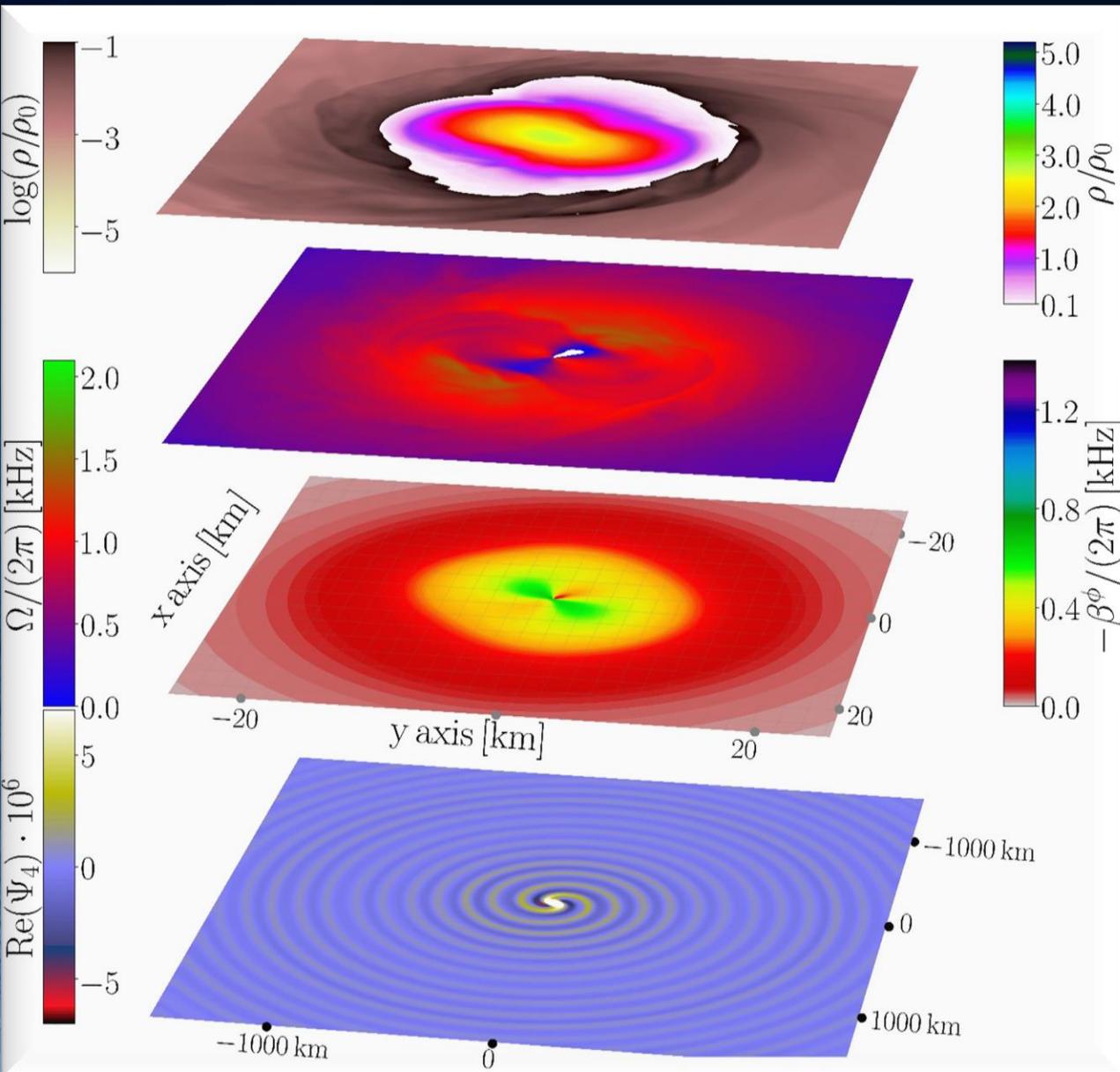
Maximum value of the rest-mass density vs time for three binary neutron star simulations. Black curve without a phase transition (NPT) and blue/red with a Gibbs-like hadron-quark phase transition (DPT: standard/low resolution). Blue-shaded regions mark the different phases of the EOS (mixed phase and pure-quark phase).

# Without Phase Transition

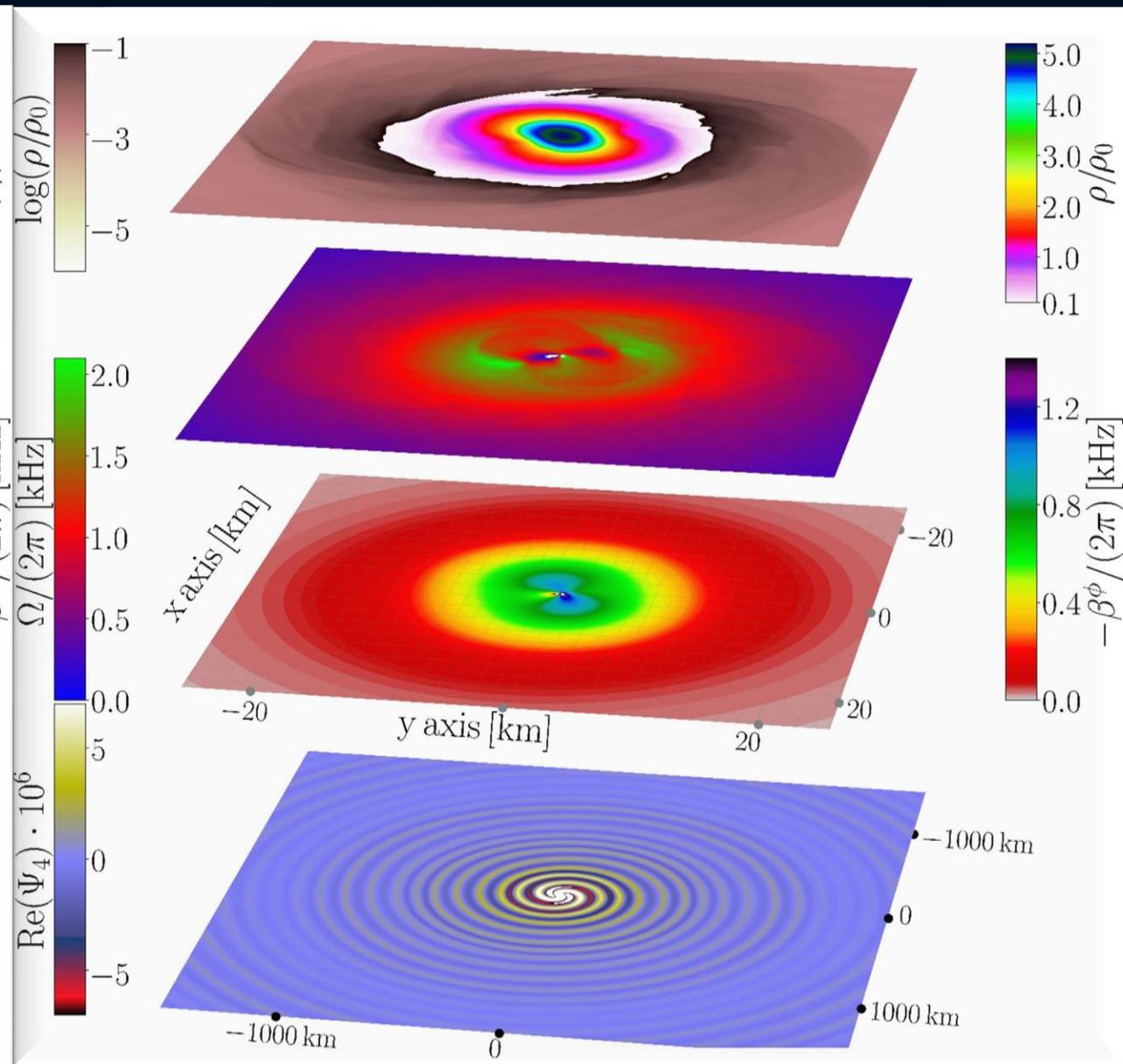
# With Phase Transition

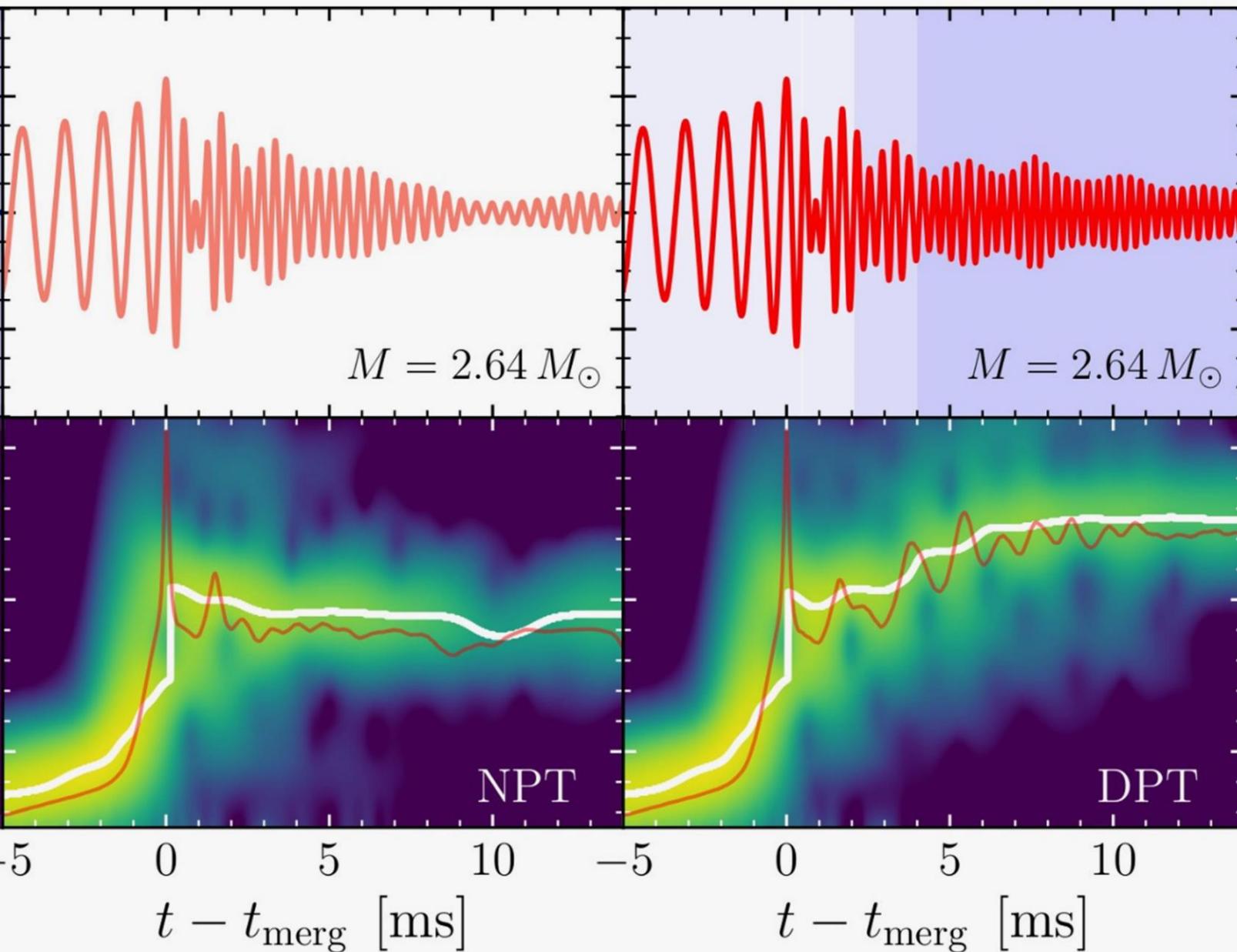


# Without Phase Transition



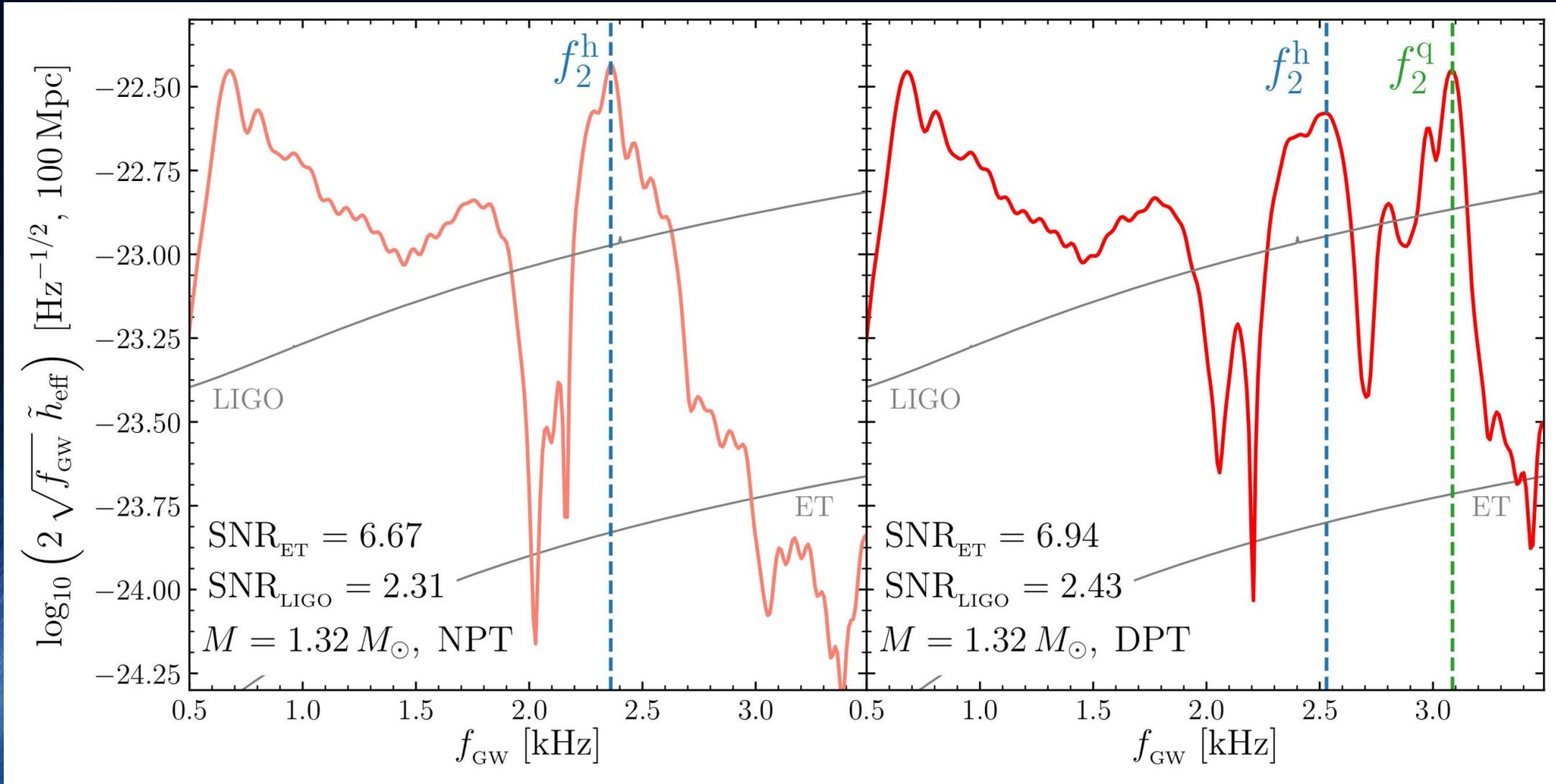
# With Phase Transition



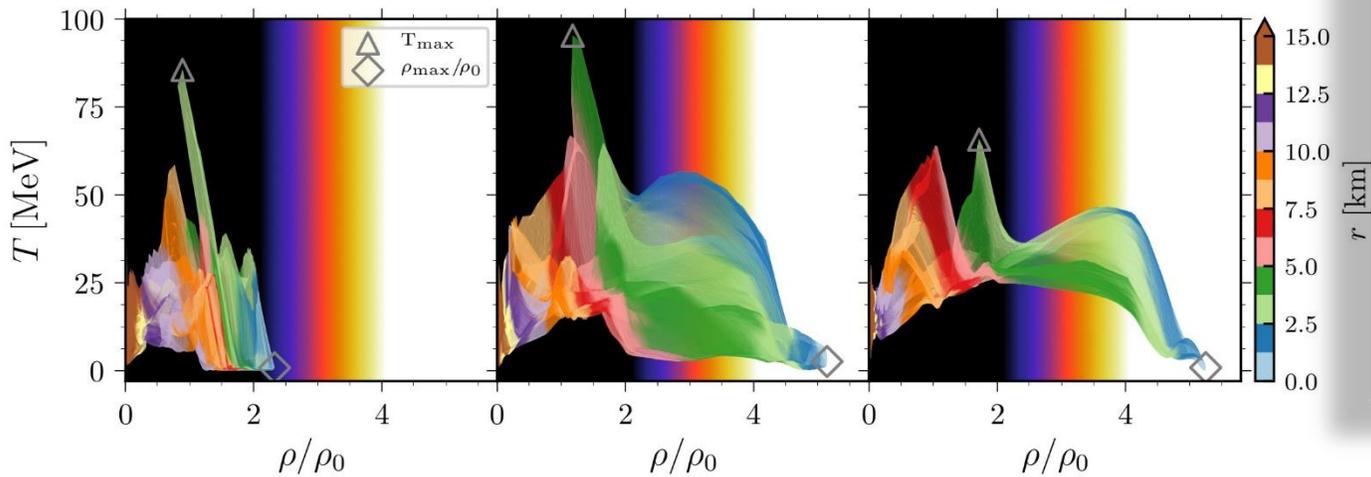
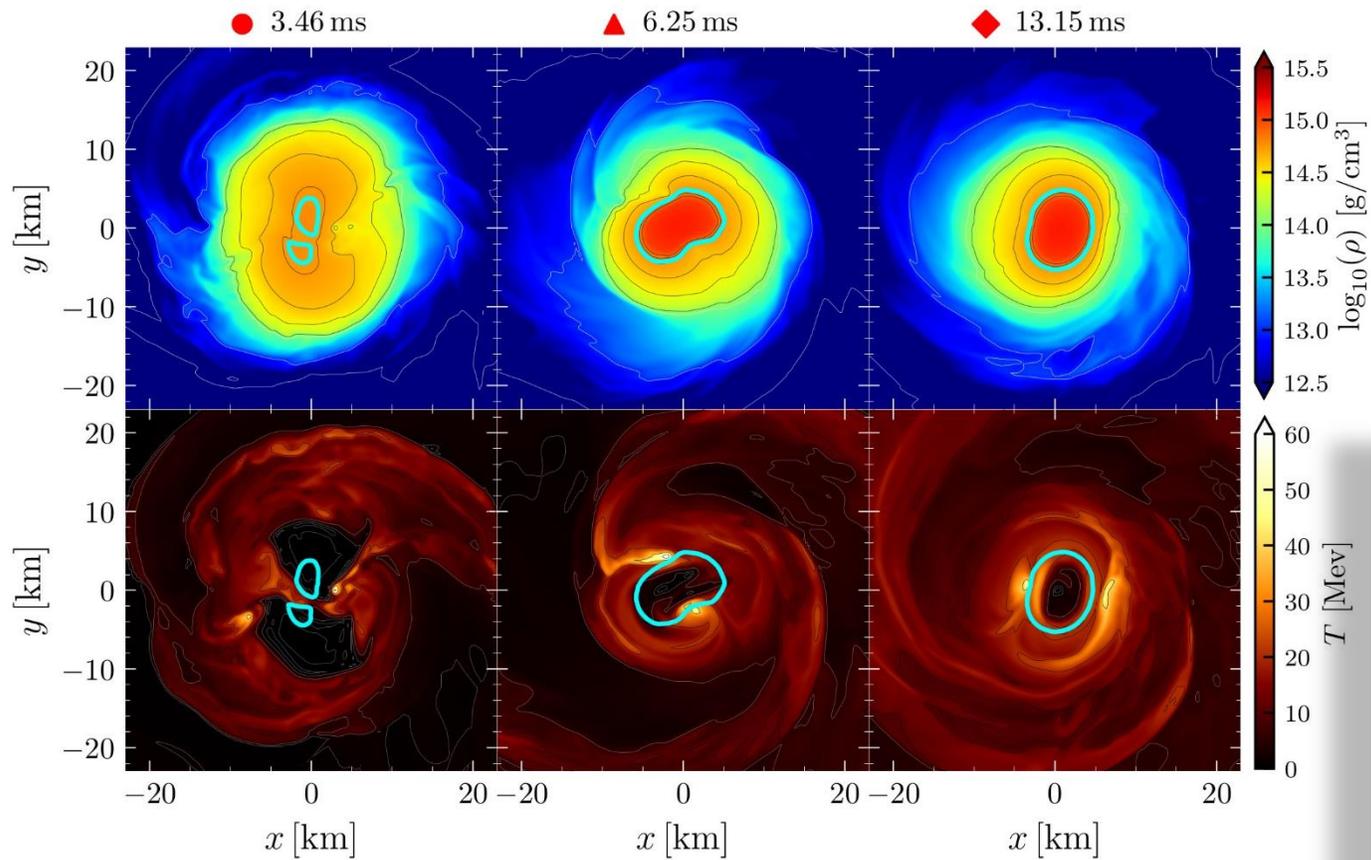


Strain  $h_+$  (top) and its spectrogram (bottom) for the binary neutron star simulation of the delayed phase transition scenario. In the top panel the different shadings mark the times when the HMHS core enters the mixed and pure quark phases. In the bottom panels, the white lines trace the maximum of the spectrograms, while the red lines show the instantaneous gravitational-wave frequency.

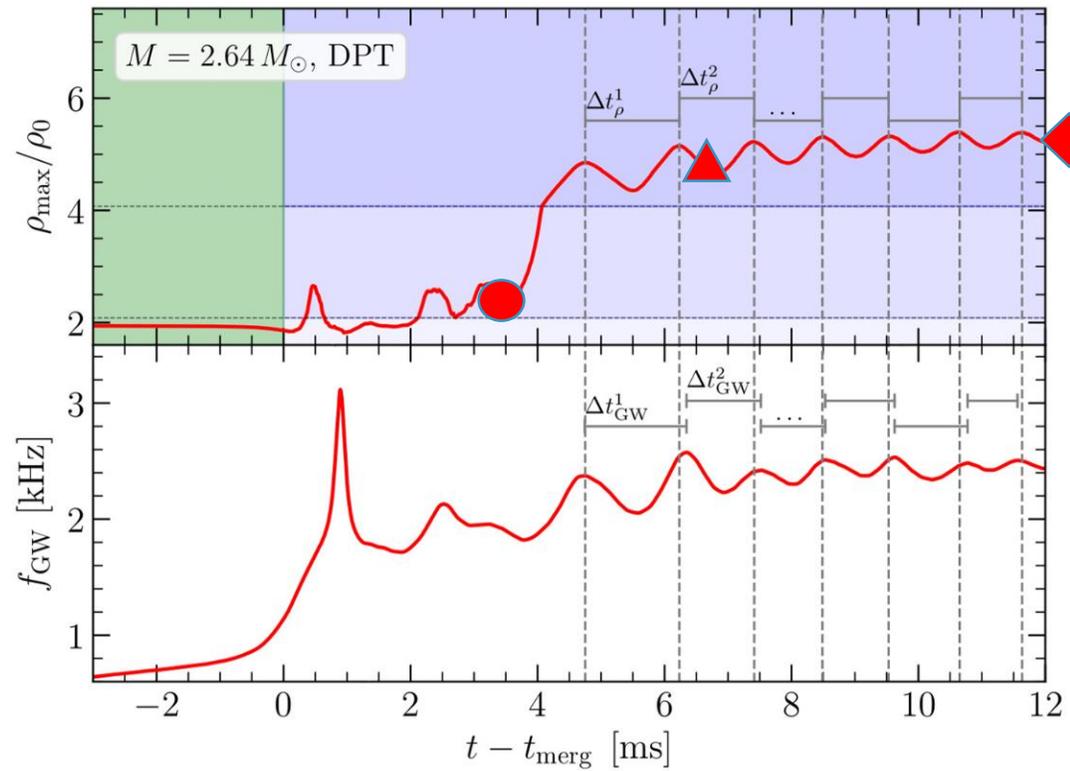
# How to detect the hadron-quark phase transition with gravitational waves



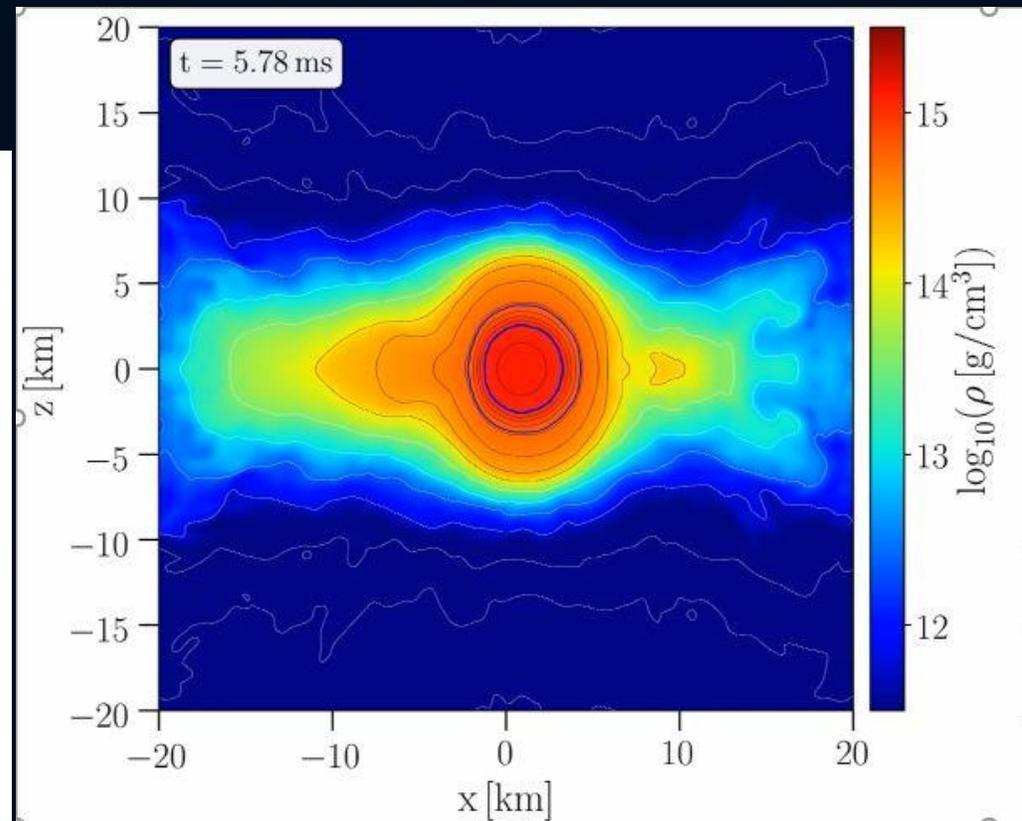
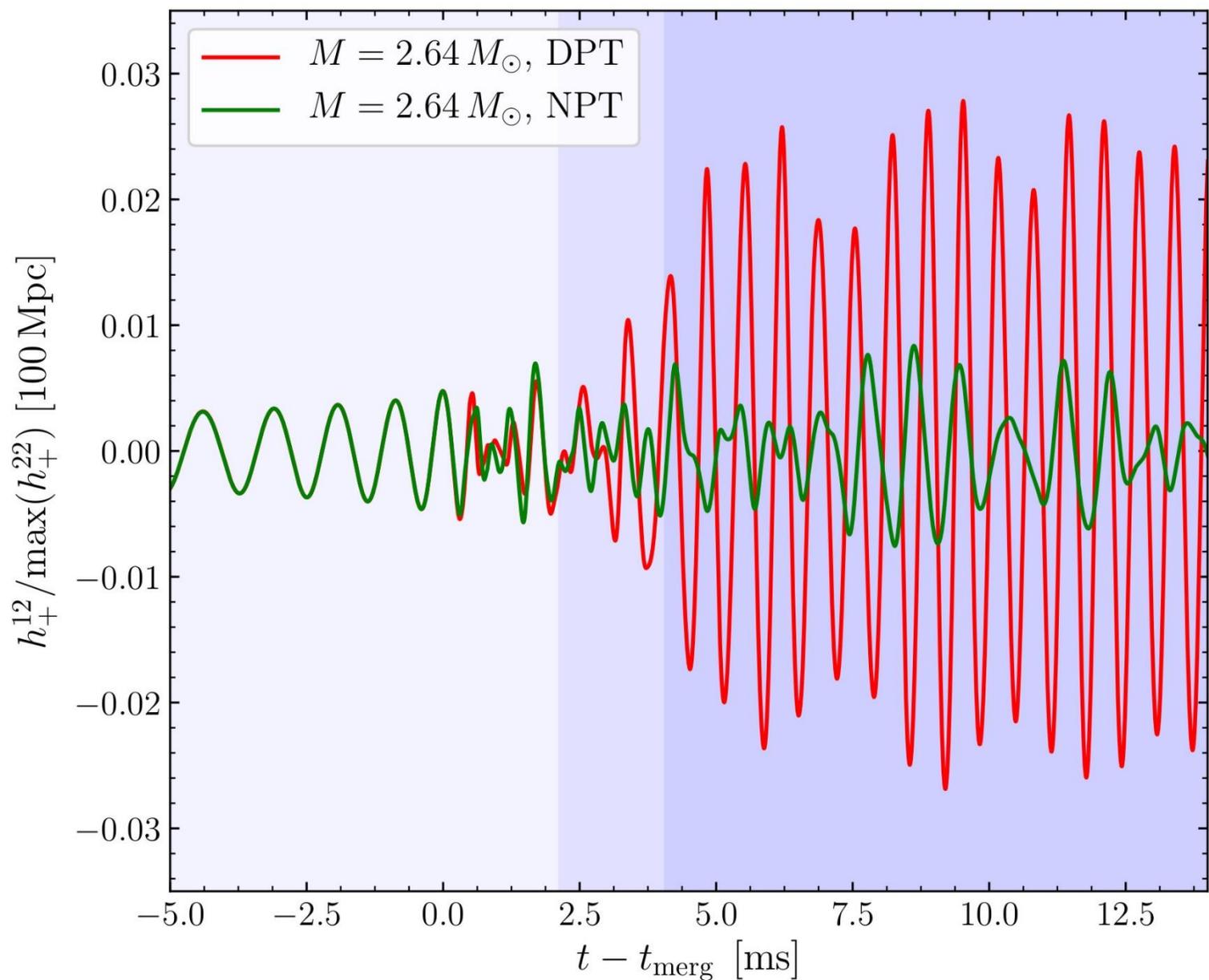
Total gravitational wave spectrum (left NPT, right DPT), PRL 124, 171103 (2020)



M. Hanauske, L. Weih, H. Stöcker  
and L. Rezzolla  
*Metastable hypermassive hybrid stars as  
neutron-star merger remnants*  
The European Physical Journal Special  
Topics: 1-8 (2021)



# Difference in the $h_+^{12}$ – gravitational wave mode



Due to the large  $m=1$  mode of the emitted gravitational wave in the DPT case, a qualitative difference to the NPT scenario might be observable in future by focusing on the  $h_+^{12}$  – gravitational wave mode during the post-merger evolution.

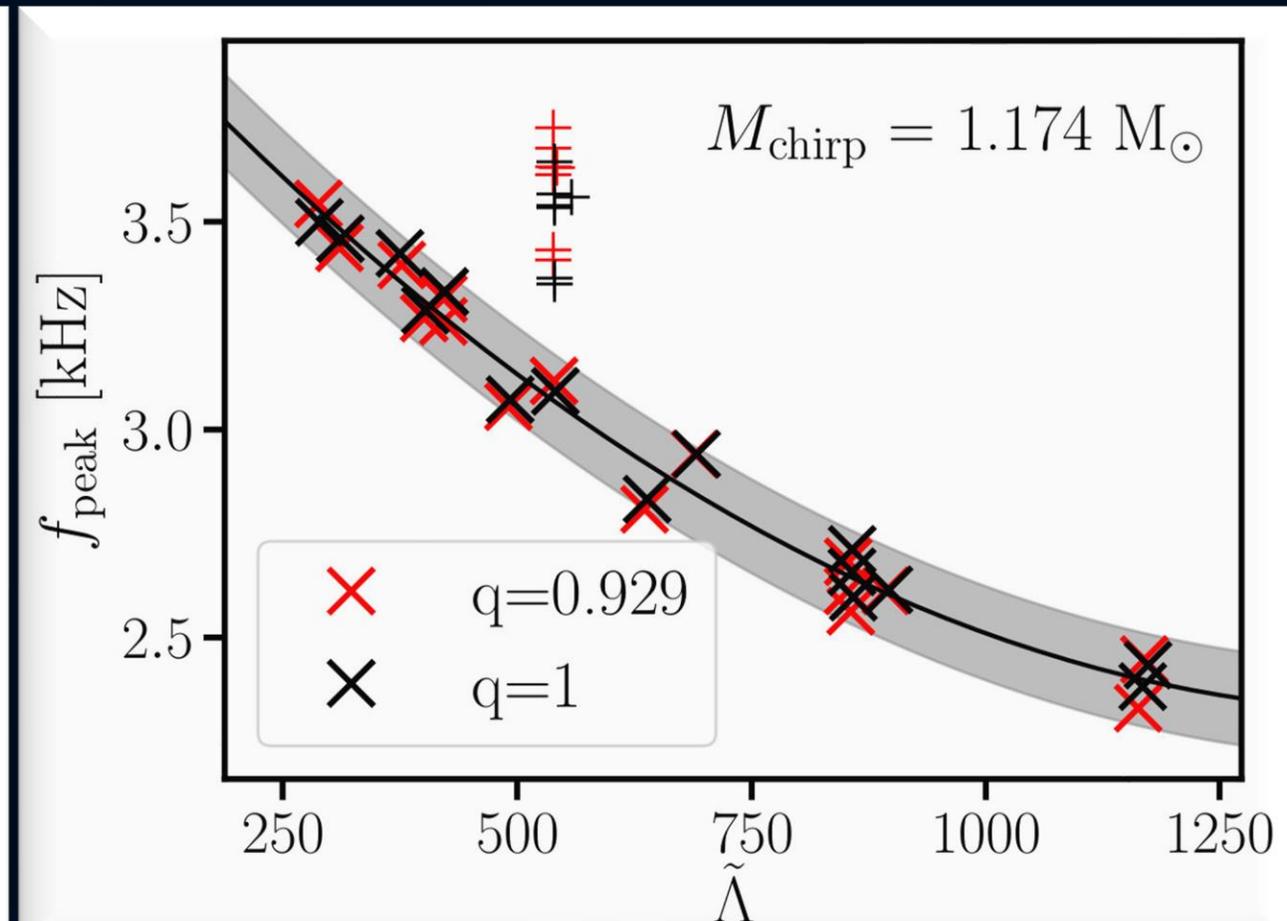
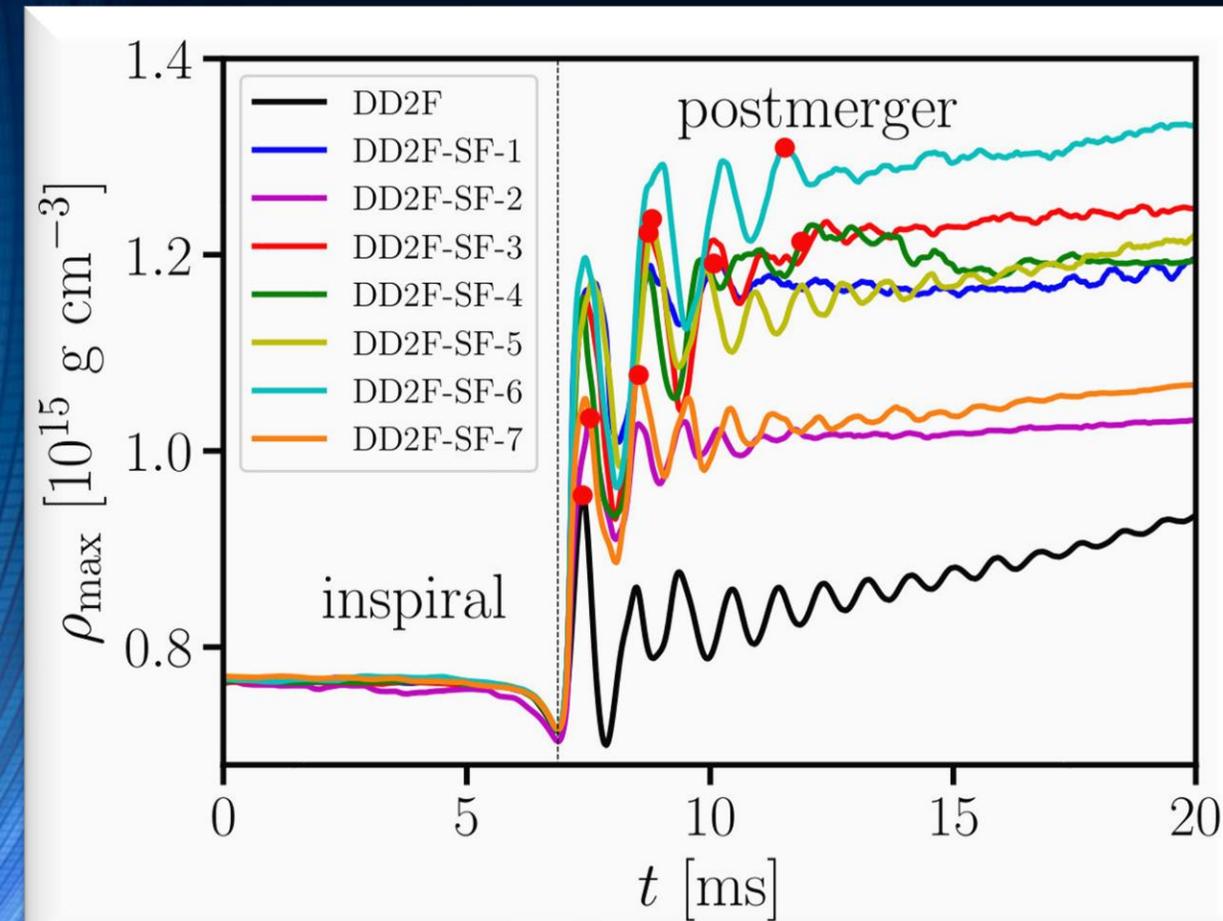
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# Signatures within the post-merger phase evolution

## Prompt phase transition scenario

Identifying a first-order phase transition in neutron-star mergers through gravitational waves; A Bauswein, NUF Bastian, DB Blaschke, K Chatziioannou, JA Clark, JA Clark, T Fischer, M Oertel; Physical review letters 122 (6), o61102 (2019)



# Gravitational-wave signatures of the hadron-quark phase transition in binary compact star mergers

## Two brand new articles

Aviral Prakash, David Radice,  
Domenico Logoteta, Albino Perego,  
Vsevolod Nedora, Ignazio Bombaci,  
Rahul Kashyap, Sebastiano Bernuzzi,  
Andrea Endrizzi.  
*Signatures of deconfined quark phases  
in binary neutron star mergers.*  
*arXiv:2106.07885 (2021).*

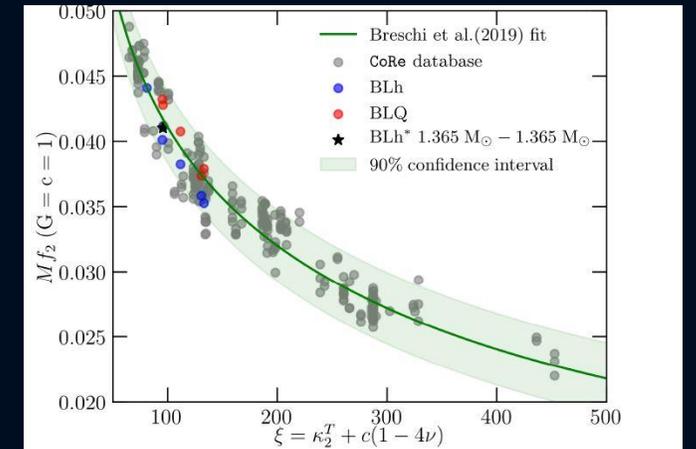
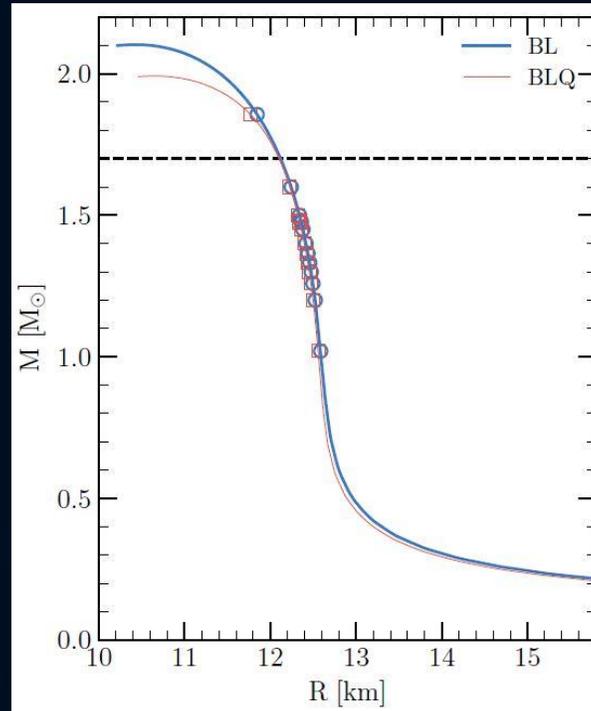
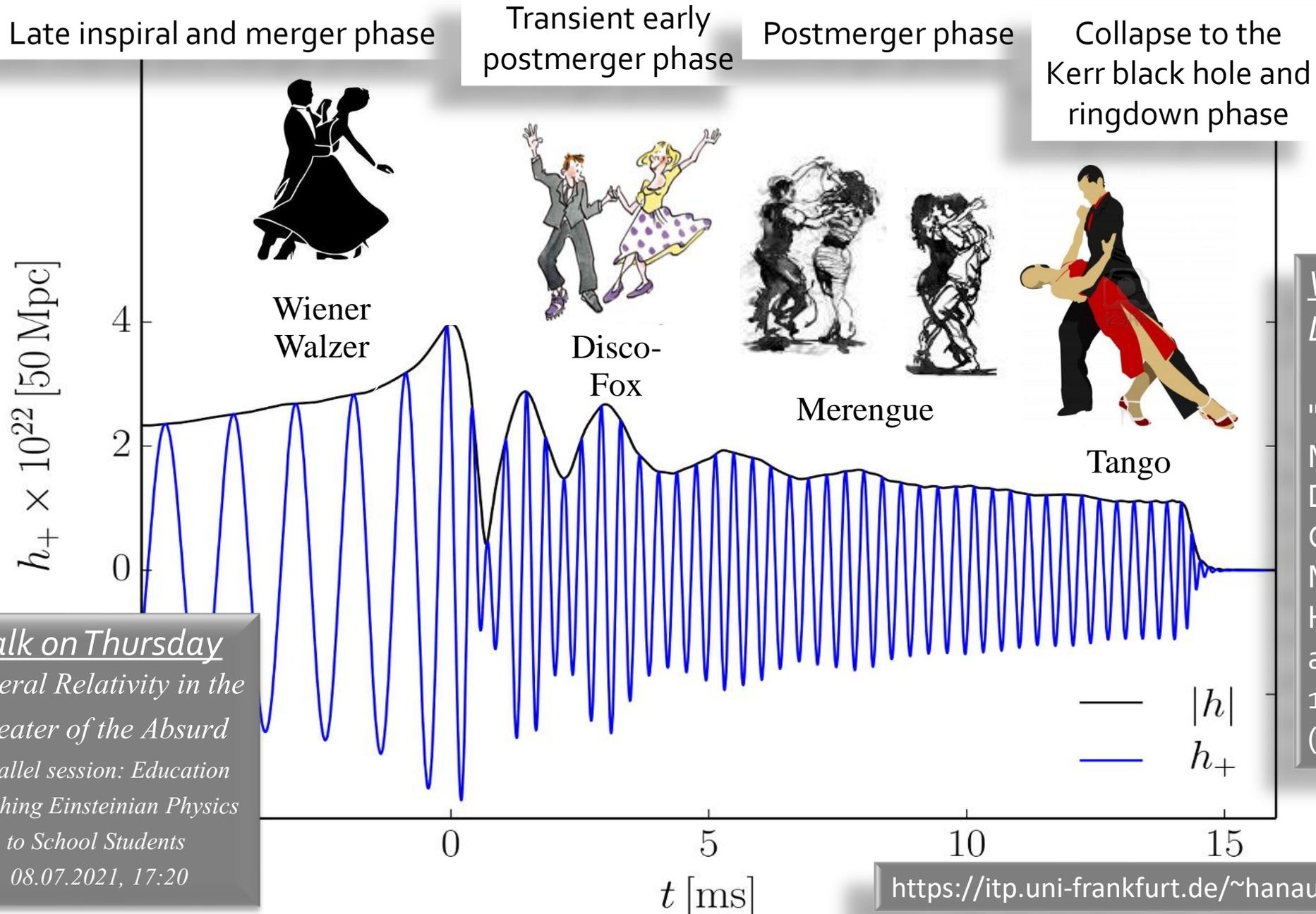


FIG. 10. Correlations between the total mass-scaled post-merger peak frequency  $Mf_2$  and the tidal parameter  $\xi$ . Also shown is the fit from the quasi universal relation presented in [25] along with its 90% confidence interval. The grey points correspond to simulations catalogued in the CoRe database [84]. It can be seen that deviations in  $f_2$  (red circles) by virtue of phase transitions are not large enough to violate the quasi-universal relation.

Liebling, Steven L., Carlos Palenzuela, and Luis Lehner.  
*Effects of high density phase transitions on neutron star dynamics.*  
*Classical and Quantum Gravity* 38.11 (2021): 115007.

# The different Phases of a Binary Compact Star Merger Event



*Why exactly these dances?  
Details in*

"Binary Compact Star Mergers and the Phase Diagram of Quantum Chromodynamics", Matthias Hanauske and Horst Stöcker, Discoveries at the Frontiers of Science, 107-132; Springer, Cham (2020)

*Talk on Thursday  
General Relativity in the  
Theater of the Absurd  
Parallel session: Education  
Teaching Einsteinian Physics  
to School Students  
08.07.2021, 17:20*