Penrose suggestion as to Pre Planck era-Black holes showing up in present universe data sets discussed, with a possible candidate as to GW radiation which may provide initial CMBR data

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Abstract

What we are doing is three-fold. First, we examine the gist of the Penrose suggestion as to signals from a prior universe showing up in the CMBR. I.e. this shows up as data in the CMBR. Second, we give a suggestion as to how super massive black holes could be broken up s of a prior Universe cycle by pre big bang conditions, with say millions of pre-Planck black holes coming up out of a breakup of prior universe black holes. Three, we utilize a discussion as to Bose Einstein Condensates set as Gravitons as to composing the early universe black holes. The BEC formulation gives a number N of gravitons, linked to entropy, per black hole, which could lead to contributions to the alleged CMBR perturbations, which were identified by Penrose et.al.

Key words: Minimum scale factor, cosmological constant, space-time bubble, Penrose singularity, prior Universe black holes.

I. First what is the Penrose suggestion as to CMBR data set and pre Universe massive Black holes ?

The abstract has a clue, as part of [1] states as to what we want to explain in the CMBR, i.e. circular rings in the CMBR "data".

In [1] there is a well crafted suggestion as to V. G. Gurzadyan, R. Penrose as to an initial quote

Quote

The significance of individual low-variance circles in the true data has been disputed; yet a recent independent analysis has confirmed CCC's expectation that CMB circles have a non-Gaussian temperature distribution. Here we examine concentric sets of low-variance circular rings in the WMAP data, finding a highly non-isotropic distribution."

End of quote

Here is the nuts and bolts as to what Penrose cosmology is about. i.e. [2]

1A. There is initial inflationary expansion of the Universe, but the caveat is that matter- energy is sucked up in super massive black holes. i.e. rather than have a purported infinite expansion, and we see the following dynamic

We connect a countable sequence of open Friedmann–Lemaître–Robertson–Walker metric (FLRW) spacetimes, each representing a Big Bang followed by an infinite future expansion. Penrose noticed that the past conformal boundary of one copy of FLRW spacetime can be "attached" to the future conformal boundary of another, after an appropriate conformal rescaling. result g_{ab} reset in a conformal reset with matter from black holes collected and reset to a new value of g_{ab} at the start of cosmological expansion with matter-energy from black holes being recycled conformally to a new expansion cycle [2]

1B. Next, let us view the Penrose suggestion as to Black holes from a prior universe.

In order to see this, consider a suggestion as to black holes, being the template for a start to the present universe given by [3], and also[4] which has the Penrose suggestion of an imprint of a prior Universe black holes having an effect upon the CMBR spectrum. The CMBR spectrum is a real datum, but the worth of getting this information would be in terms of having what was said in [4] as to the "ghost" of prior universe black hole radiation . To get a glimpse of where this is going the author invites readers to look at [5] as to the cosmic maelstrom such 'signals' would have to pass through

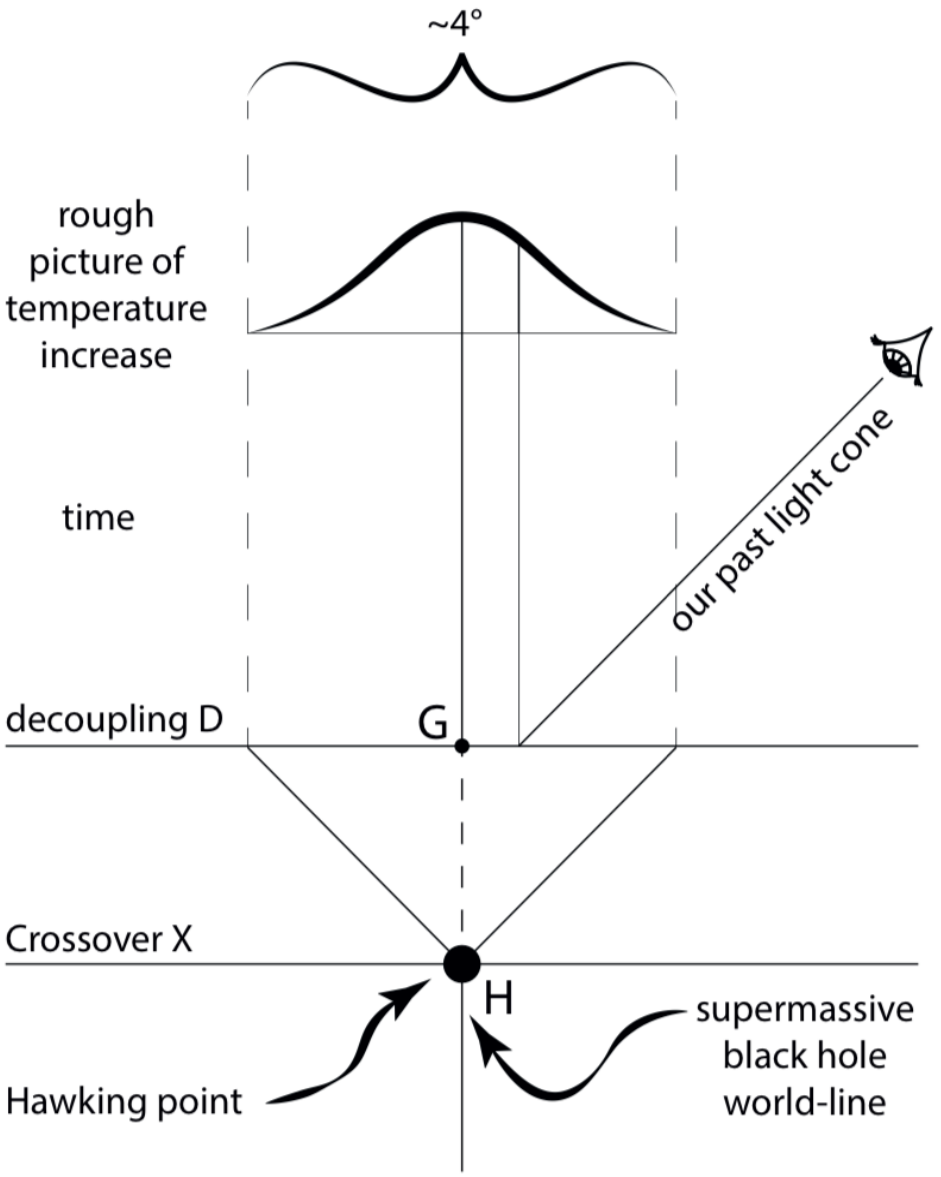

Figure 1 as given in [4] which has competing black hole radiation, and can we see this today in the CMBR?

Quote from page 2 of [4], namely

FIG. 1: A conformal diagram representing the effect of a highly energetic event occurring at the space-time point H. In CCC, H is taken to be a Hawking point, where virtually the entire Hawking radiation of a previous-Aeon supermassive black hole is concentrated at H by the conformal compression of the hole's radiating future. The horizontal

line at the bottom stands for the crossover surface dividing the previous cosmic aeon from our own and describes our conformally stretched Big Bang. In conventional inflationary cosmology, X would represent the graceful exit turn-off of inflation. In each case, the future light cone of H represents the outer causal boundary of physical effects initiated at H, and such effects can reach D only within the roughly 0.08 radian spread indicated at the top of the diagram

End of quote

II. What can we expect from the transition from a Prior universe to the Planckian regime of micro black holes? A transition from initially gigantic black holes to micro black holes.

II.A. In a word, we would likely have in the prior universe MASSIVE black hole, which would be broken up into millions (billions?) of Planck sized

In a word the GW radiation and thermal/photonic input would have to fight through a thicket of pairs of micro black holes which would be in binary configuration generating their OWN GW background.

We first will discuss this ‘binary black holes’ signal background which the Planckian early Universe stars would have to impinge upon, in order to come to our attention.

Now for the discussion of the millions (more than that) of micro sized black hole pairs which would create a generalized GW signature.

To evaluate the above in terms of our model, we need to refer to a formula given in [5][20], on page 16 of that document which reads as a change in power from rotating Planck sized black holes separated say by a Planck length.

$$\dot{E} = GW - change - in - energy = \frac{32\left(M_1 M_{\ 2}\right)^2 \left(M_1 + M_{\ 2}\right)}{5 \cdot R^2 M_{Planck}^5}$$

$$\xrightarrow[M_1 = M_{\ 2} = M_{Planck}]{} \frac{64}{5 \cdot R^2 (Planck - length)} \qquad (1)$$

$$\equiv Change - in - power - \ from - Rotating - binary - black \quad holes$$

For M about the size of a Planck sized black hole, it likely would fade out almost too quickly to be very measurable.

II.B. **We also can consider the following Gravitons as a Bose-Einstein condensate in low mass Black holes, and its relevance to signal propagation.**

This is a way to get measurable GW signals from a black hole, which have a chance of being detected.

We will be looking at [6] specifically page 181, where we have the following scaling arguments to work through, if Gravitons are BEC for small Black holes. The following are scaling value to consider, if we want BEC

Why we consider BECs and Eq. (2), i.e. if there is a break up of massive black holes into say Planck mass sized black holes, as or about the Planck era, very likely will not have a surviving signal which has a chance of being measurable in the CMBR data. I.e. the discussion of Eq. (2) below uses the device of having BEC condensation in gravitons for masses up to about 10 grams or so, and in doing so a dodge as to getting entropy counts per black hole.

That is after the black hole masses, as given in Eq. (2) are likely built up by the consolidation of two mini black holes going through an inspiral collapse, as has been modeled in GW

$$m \approx \frac{M_P}{\sqrt{N_{gravitons}}}$$

$$M_{BH} \approx \sqrt{N_{gravitons}} \cdot M_P$$

$$R_{BH} \approx \sqrt{N_{gravitons}} \cdot l_P$$

$$S_{BH} \approx k_B \cdot N_{gravitons}$$

$$T_{BH} \approx \frac{T_P}{\sqrt{N_{gravitons}}} \qquad (2)$$

Here, the first term, m, is in the effective mass of a graviton. This is my take as to how to make all this commensurate as to special relativity.

$$m \approx \frac{m_g}{\sqrt{1-\left(\frac{v_g}{c}\right)^2}} \approx \frac{M_P}{\sqrt{N_{gravitons}}} \approx 10^{-10}\, grams \quad (3)$$

$$\therefore N_{gravitons} \approx 10^{10} \quad (4)$$

With this, if say one has a 1 gram black hole, about 10^5 times larger than a Planck mass, one would be having say an entropy generated this way of about 10^10, assuming Planck normalization

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III. So, then what are the number of gravitons emitted via a spinning Planck sized black holes component binary in terms of gravitons ? [7] What does this say about an optimal BH size as to perhaps see measurable GW / Graviton generation effects

Likely from the situation in [7] for items as of about a Planck length, and involving Planck sized masses, we would see the following equation for a rotating rod, of mass M, and of velocity V, of its end, for Graviton production

$$N_g \approx \frac{32}{45} \cdot \frac{G}{\hbar c} \cdot M^2(rod) \cdot \left(\frac{V_{rod-tip}}{c} \right)^4$$

$$\propto 7.5 \times 10^{-8} \cdot \left(M(rod) \right)^2$$

$$\Rightarrow N_g \geq 1 \quad iff \quad M(rod) \geq 4 \times 10^6 \, grams \tag{5}$$

If we have an equivalent situation w.r.t. 2 black holes in a binary state, we would likely need to have approximately black holes of masses 10^5 g to 10^6 grams , i.e,. 10^10 to 10^11 times larger than Planck mass, in order to have a measurable GW/Graviton signal which would be commensurate with experimental data sets. If we had say 10^5 to 10^6 g black holes, then the value of gravitons released per second, from a BEC condensate of Gravitons for a mini black hole would me many times larger than Eq. (4) above

We don't know the exact values, but this leads to our next point, which is the stages of Black holes, before the Planckian era, to at the point of time (and space) where 1 to 10^5 gram black holes would be composed of Gravitons by BEC condensation of Gravitons, for a release in

III.A. Considering this, what can we say about the regimes of BH masses, just before the Planckian era, during the Planckian era, and right after the Planckian era?

We are assuming the following. A moderately large (10^6) or more) number of super massive black holes which would be in the center of galaxies, and which would be broken up and recycled in the CCC cosmology regime, with masses dropping from about 10^41 grams, down to about 10^-4 to 10^-5 grams, before recombination by Planck era recombination into a tier of black holes which would be at least 1 gram in mass , scaling up to 10^5 grams in mass so as to allow for BEC

generation of gravitons through entropy production as in Eq. (2) and Eq. (3) above

In doing so, we purport to use the datum given in [7] that masses of say much lower than 10^5 to 10^6 grams for black holes likely do not have much chance of producing gravitons which would be detectable in the present era. Indeed, a minimum mass of about 1 to 10 grams for a black hole would be needed for a Bose Einstein condensation via gravitons for a “light – low mass “black hole which would be able to by Eq. (2), Eq. (4) and Eq. (5) to have at least 10^10 gravitons per second generated (entropy for a BEC black hole)

III.B. We then would to a round off approximation state this hierarchy of BH behavior and size to consider a systematic break down of initially gigantic black holes, into Planck sized black holes, and then from there to

TABLE 1

Scaling of Mass of Black holes, and their purported number, if CCC cosmology (Penrose) assumed for GW radiation release (may affect the CMBR)

End of Prior Universe time frame	Mass (black hole) : super massive end of time BH 1.98910^+41 to about 10^44 grams	Number (black holes) 10^6 to 10^9 of them usually from center of galaxies
Planck era Black hole formation Assuming start of merging of micro black hole pairs	Mass (black hole) 10^-5 to 10^-4 grams (an order of magnitude of the Planck mass value)	Number (black holes) 10^40 to about 10^45, assuming that there was not too much destruction of matter-energy from the Pre Planck conditions to Planck conditions
Post Planck era black holes with the possibility of using Eq. (2) to have say 10^10 gravitons/second released per black hole	Mass (black hole) 10 grams to say 10^6 grams per black hole	Number (black holes) Due to repeated Black hole pair forming a single black hole multiple time. 10^20 to at most 10^25

IV. Why we would have the figures from III.B to consider for contributions to the CMBR and the Penrose suggestion

the formula which is for Luminosity from a black hole and in page 16 of reference [5] the text states that the two black holes emit GW with a

wave frequency 2 times the rotation frequency of the orbit of the two black holes to each other.

If we assume that we are still using this approximation above, from[5] we can see support for our choice of Planck length as the minimum separation distance between the two black holes via using Plank units normalized to 1 as yielding

$$R\left(separation\right) \simeq r_g^{eff} = \frac{\left(M_1 + M_2\right)}{\left(M_{Planck}\right)^2}$$

$$\xrightarrow[M_1 = M_2 = M_{Planck}]{M_{Planck}=1} 1 \equiv R\left(Planck - length\right) \quad (6)$$

Going to Clifford Will, [8] we see on page 252 a loss or shrinkage of the period for the rotating black hole pair defined by P

$$\dot{P} / P = \frac{dP}{dt} \cdot \frac{1}{P} = -\frac{3}{2}\frac{\dot{E}}{E} \quad (7)$$

Whereas ,with the Mechanics version of P for a sphere to be defined by, where M is a mass of a star, and we assume a binary system with two masses of equal mass M, so that , if R is the separation between the two masses[9][29] on page 188 would be

$$P = R\sqrt{\frac{2\pi^2 R}{G \cdot M}} \xrightarrow[M_1 = M_2 = M_{Planck}]{M_{Planck}=1}$$

$$R\left(Planck - length\right)\sqrt{\frac{2\pi^2 R\left(Planck - length\right)}{G \cdot M\left(Planck\right)}} \quad (8)$$

For Planck sized masses, this means that the period of the binary plank mass black hole pair would be vanishingly small,

The frequency of rotation would be half that of the GW emitted by these two Planck mass black holes which would collapse into each other. Note that the frequency we have stated for this last step, is given in Eq. (9). i.e., could we have the following quantization contribution to initial frequency?

Our final concluding point to this chapter is to review the physics of Figure 1, and then to ask, can we ascertain the GW radiation of Planck era black hole stars in a binary configuration contributing to a buildup of generating frequency getting. If

$$\Delta E\Delta t \approx \hbar \equiv \hbar\omega\Delta t \approx \hbar\omega\cdot\left(\frac{2}{3a_{\min}}\right)^{1/\gamma} \Rightarrow \omega \approx \hbar^{-1}\cdot\left(\frac{2}{3a_{\min}}\right)^{-1/\gamma} \quad (9)$$

We claim that if we take the energy as consistent with a change in value as given by Eq. (1) that this will lead to a frequency which may, if $a_{\min} \approx 10^{-25} - 10^{-20}$ (range from 10^-25 to 10^-20) lead to

$$\omega \approx \hbar^{-1}\cdot\left(\frac{3}{2}\right)^{1/\gamma}\cdot 10^{25/\gamma} \propto \left(\frac{3}{2}\right)^{1/\gamma}\cdot 10^{25/\gamma}\, Hz \quad (10)$$

Whereas note that the frequency is , say dependent upon the choice of γ and that this could be very different from the Planck frequency given below

$$\omega_P \approx 1.885\cdot 10^{43}\, Hz \quad (11)$$

We have then that if one had a redshift, of z ~ 10^25, that this would mean a present value of frequency as of about 1 Hz, whereas we can consider what would be gained by looking at the contribution near the CMBR, i.e. z~ 1100 or so for the CMBR, whereas this would mean roughly that we would be looking in the regime of the CMBR

$$\omega_{signal-from-Planck-to-CMBR} \propto \left(\frac{3}{2}\right)^{1/\gamma} \cdot 10^{(25/\gamma)} \times 10^{-3}\, Hz \qquad (12)$$

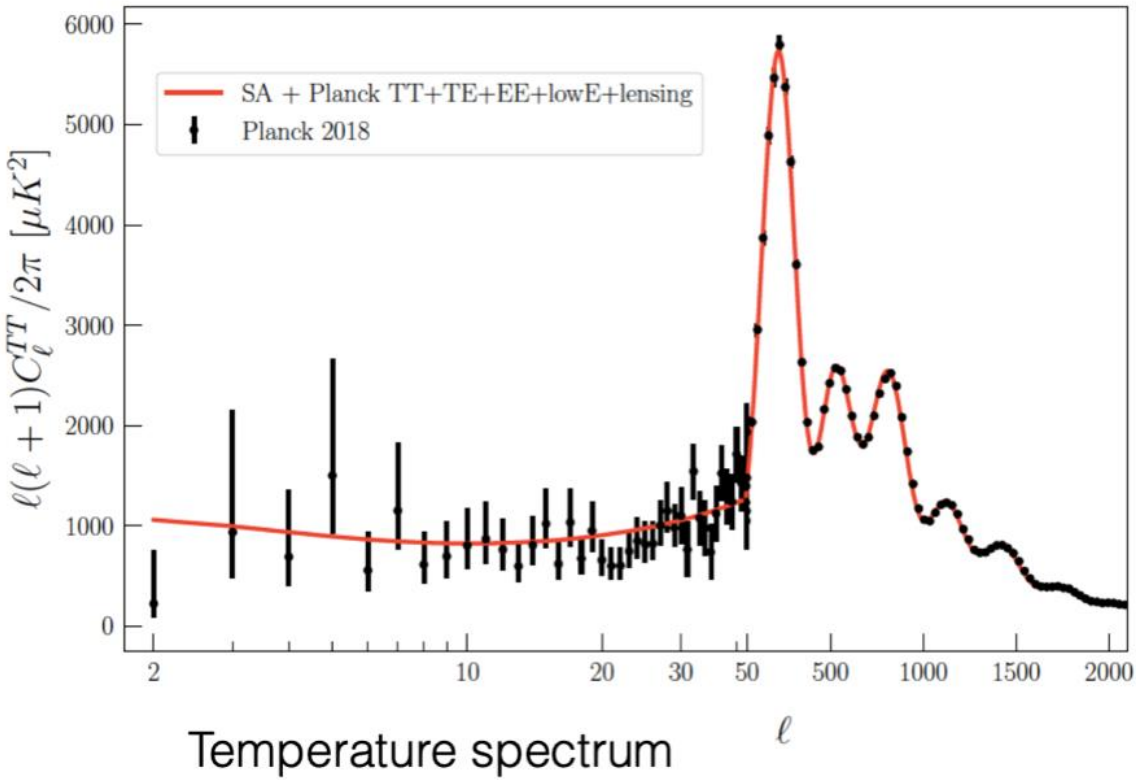
However, we have in doing this, that the duration of this frequency signal would be very minimal, i.e. due to the decay of the period, this would be going on for less than a nanosecond.

If so then we would need to refer to Eq. (2) and the value of

$$E_{BEC-Graviton} \approx \frac{k_B T_{BH}}{2} \approx \frac{k_B \times 10^{-5} \times T_P}{2}$$
$$\Rightarrow \omega_{BEC-Graviton} \propto 10^{-5} \times 10^{43}\, Hz \approx 10^{38}\, Hz$$
$$\Rightarrow \omega_{BEC-Graviton-to-CMBR} \approx 10^{38} \times 10^{-3}\, Hz \qquad (13)$$

Needless to state, that unlike the case of (12), one would likely have the duration of the signal last long enough as to imprint directly on the CMBR i.e. look at [9] and also For this I refer to the Zeldovich 4 conference Abhay Ashtekar presentation[10]

Ashtekar referred to a removal of bogus data points in the CMBR, as to the figure below, i.e. FIGURE 1



Now looking at what was discussed by [Abhay Ashtekar](#) in Zeldovich4. On September 7, 2020 [10]

In our figure 1, we copy what was done by Ashtekar, in Zelsovich4 as to what was part of anisotropic fits to the E and B polarization, as given is made easier, if there is a non singular start to the universe which I discussed in detail in [11] , and that further polarization states which may be analyzed in detail could be ascertained in [12]

If one has a nonsingular start to the universe, modeled on a muti universe generalization of Penrose CCC cosmology as is argued in [11] then the details of a break up of black holes would not be so startling, i.e. these are the details from [11] as given by the following generalization of CCC cosmology , and this is from [11]

IV.A. Looking now at the Modification of the Penrose CCC (Cosmology)

We now outline the generalization for Penrose CCC(Cosmology) just before inflation which we state we are extending Penrose's suggestion of cyclic universes, black hole evaporation, and the embedding structure our universe is contained within, This multiverse has BHs and may resolve what appears to be an impossible dichotomy. The text following is largely from [11] and has serious relevance to the final part of the conclusion. That there are N universes undergoing Penrose 'infinite expansion' (Penrose) [2] contained in a mega universe structure. Furthermore, each of the N universes has black hole evaporation, with Hawking radiation from decaying black holes. If each of the N universes is defined

by a partition function, called $\left\{\Xi_i\right\}_{i\equiv N}^{i\equiv 1}$, then there exist an information ensemble of mixed minimum information correlated about $10^7 - 10^8$ bits of information per partition function in the set $\left\{\Xi_i\right\}_{i\equiv N}^{i\equiv 1}\Big|_{before}$, so minimum information is conserved between a set of partition functions per universe [13]

$$\left\{\Xi_i\right\}_{i\equiv N}^{i\equiv 1}\Big|_{before} \equiv \left\{\Xi_i\right\}_{i\equiv N}^{i\equiv 1}\Big|_{after} \qquad (14)$$

However, there is non-uniqueness of information put into partition function $\left\{\Xi_i\right\}_{i\equiv N}^{i\equiv 1}$.Also Hawking radiation from black holes is collated

via a strange attractor collection in the mega universe structure to form a new inflationary regime for each of the N universes represented

Our idea is to use what is known as CCC cosmology [13], which can be thought of as the following. First. Have a big bang (initial expansion) by $\{\Xi_i\}_{i\equiv N}^{i\equiv 1}$. Verification of for the universe which is represented this mega structure compression and expansion of information with stated non-uniqueness of information placed in each of the N universes favors ergodic mixing of initial values for each of N universes expanding from a singularity beginning. The n_f stated value, will be using (Ng, 2008) $S_{entropy} \sim n_f$. [13] [14]. How to tie in this energy expression, as in Eq. (12) will be to look at the formation of a nontrivial gravitational measure as a new big bang for each of the N universes as by $n(E_i)\cdot$ the density of states at energy E_i for partition function [13]. **[15]**

$$\{\Xi_i\}_{i\equiv 1}^{i\equiv N} \propto \left\{ \int_0^{\infty} dE_i \cdot n(E_i) \cdot e^{-E_i} \right\}_{i\equiv 1}^{i\equiv N} . \qquad (15)$$

Each of E_i identified with Eq. (15) above, are with the iteration for N universes [13], and (Penrose, 2006) [2] Then the following holds, by asserting the following claim to the universe, as a mixed state, with black holes playing a major part, i.e.

CLAIM 1

See the below [13] representation of mixing for assorted N partition function per CCC cycle

$$\frac{1}{N}\cdot\sum_{j=1}^{N}\Xi_j\Big|_{j-before-nucleation-regime}\xrightarrow{vacuum-nucleation-tranfer}\Xi_i\Big|_{i-fixed-after-nucleation-regime} \quad (16)$$

For N number of universes, with each $\Xi_j\Big|_{j-before-nucleation-regime}$ for j = 1 to N being the partition function of each universe just before the blend into the RHS of Eq.(16) above for our present universe. Also, each independent universes as given by $\Xi_j\Big|_{j-before-nucleation-regime}$ is constructed by the absorption of one to ten million black holes taking in energy**. I.e. (Penrose)**

[2]. Furthermore, the main point is done in [11] in terms of general ergodic mixing [13]

Claim 2

$$\Xi_j\Big|_{j-before-nucleation-regime}\approx\sum_{k=1}^{Max}\tilde{\Xi}_k\Big|_{black-holes-jth-universe} \quad (17)$$

What is done in **Claim 1 and 2 [11]** is to come up as to how a multi-dimensional representation of black hole physics enables continual mixing of spacetime largely as a way to avoid the Anthropic principle[11], as to a preferred set of initial conditions

V. Conclusion, i.e. if one has a nonsingular start of expansion of the universe and Ergodic mixing of initial conditions of space-time from other universes, how does this relate to the breaking up of BHs from table 1 ?

In [11] to do away with the Anthropic principle, the following references in terms of Ergodic mixing of the Partition function of the Universe was

utilized, as far as a multiverse. But there is one final piece. Assume that we have

$$\omega_{Earth-orbit} \leq 10^{-25}\,\omega_{initial-era} \qquad (18)$$

We will be of course assuming an equivalence between a graviton count and information, as given by [17], and we can in future work compare this with the Rosen[19] value of energy for a mini universe of(from a Schrodinger equation) with ground state mass of $m = \sqrt{\pi} M_{Planck}$ and an energy of

$$E_{\hat{n}} = \frac{-Gm^5}{2\pi^2 \hbar^2 \hat{n}^2} \qquad \textbf{(19)}$$

Our preliminary supposition is that Eq. (19) could represent the initial energy of a Pre Planckian Universe and that Eq. (20) would be thermally based energy dumped into the space-time bubble assumed to be in [11], i.e.

$$E(universe) = 10^{41} \times E_{BEC-Graviton} \approx 10^{41} \times \left(\frac{k_B T_{BH}}{2} \approx \frac{k_B \times 10^{-5} \times T_P}{2} \right) \textbf{(20)}$$

be the thermal energy dumped in due to the use of Cyclic Conformal cosmology. Here we specify that initially it would have that the value of Eq. (20) would exactly counter balance the energy given in a negative form by Rosen as of Eq. (19).

Now use the following approximation of the Universe, initially having the entropy of a black hole, i.e, we are using Ng Infinite

Quantum statistics, [20], while Area denotes the surface area of the regime of space-time.

$$S_{Universe} \propto S_{BH} \cong \frac{A(area)}{4 \cdot \ell^2_{Planck}} \approx \frac{9n_Q}{4} \approx n_{graviton} \qquad \textbf{(21)}$$

This way of noting entropy and the signals of the prior Universe Black holes being generated secondarily is a surface area which is commensurate with the utilization of Eq. (2) for BEC condensation by Gravitons for Early Universe black holes. This is in tandem with the quantum fluctuations as seen in Figure 2 below. Also see Appendix A below, as well as the physics, of [18],[19], and [20]

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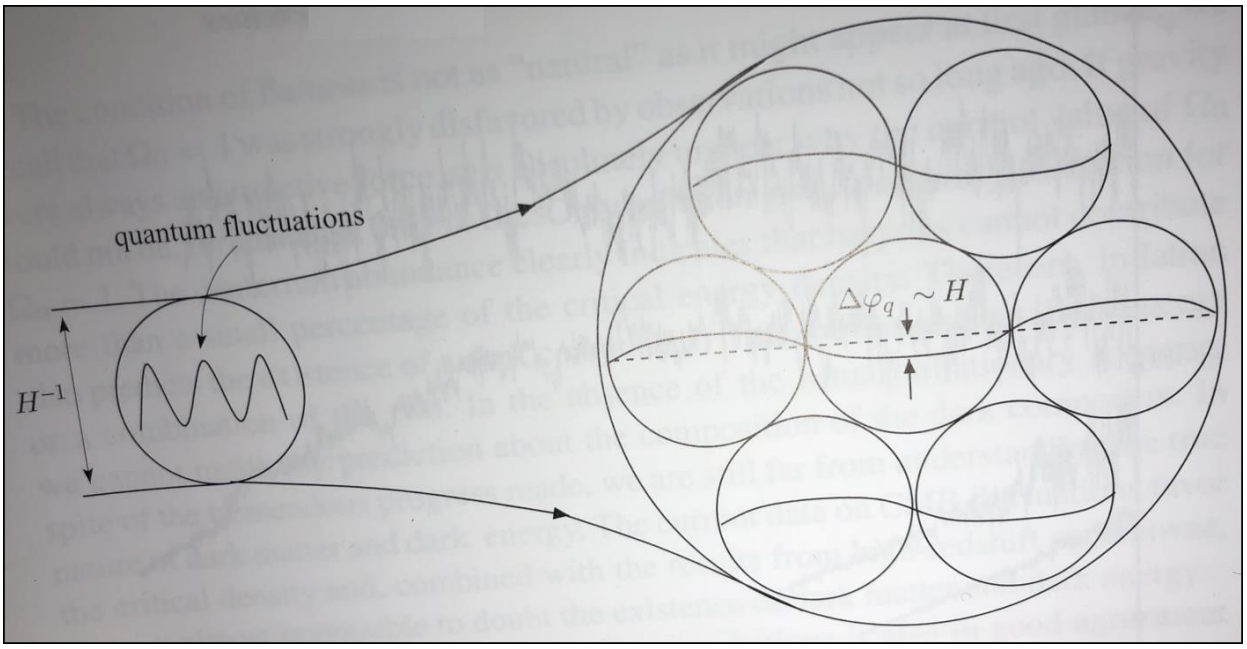


Figure 2 which is from reference [11] , [15]

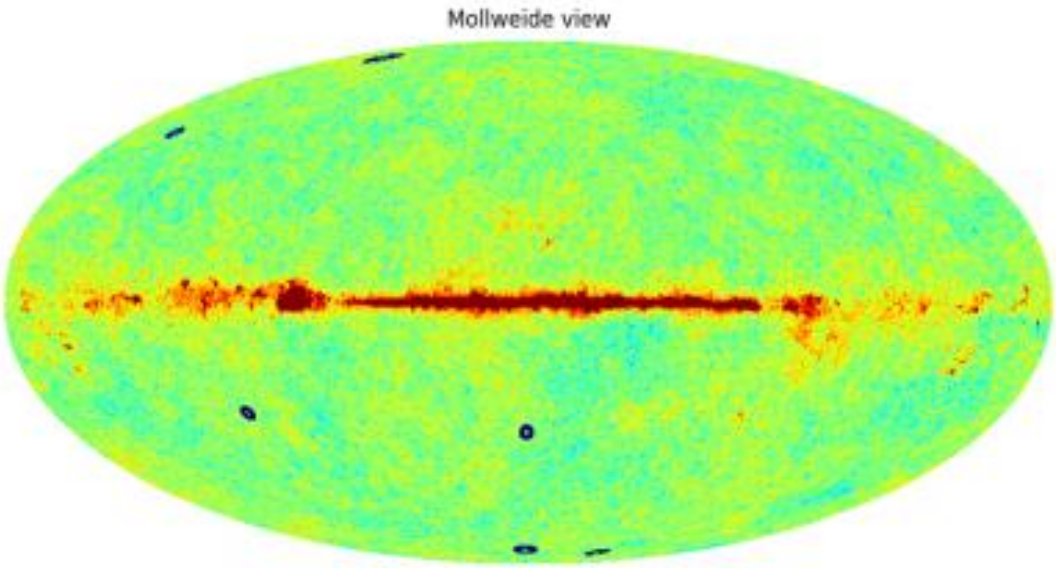
The bubble nucleation, plus the details of cosmology as presented in [21] leading to

Quote

For thirty years Oxford Mathematician Roger Penrose has challenged one of the key planks of Cosmology, namely the concept of Inflation, now over 40 years old, according to which our universe expanded at an enormous rate immediately after the Big Bang. Instead, fifteen years ago, Penrose proposed a counter-concept of C*onformal Cyclic Cosmology* by which Inflation is moved to before the Big Bang and which introduces the idea of preceding aeons. The concept has been disputed by most physicists, but Roger and colleagues believe that new evidence has come to light which requires closer inspection and argument - the research is published today in the Monthly Notices of the Royal Astronomical Society (MNRAS).

Recent analysis of the Cosmic Microwave Background (CMB) by Roger, Daniel An, Krzysztof Meissner and Pawel Nurowski has revealed, both in the Planck and WMAP satellite data (at 99.98% confidence), a powerful signal that had never been noticed previously, namely numerous circular spots $\sim 8 \sim 8$ times the diameter of the full moon. The brightest six (Figure 1) are $\sim 30 \sim 30$ times the average CMB temperature variations seen at precisely the same locations in the Planck and WMAP data. These spots were

overlooked previously owing to a belief that the very early exponentially expanding *inflationary* phase of standard cosmology should have obliterated any such features.



End of quote

We submit that judicious application of Eq. (2) plus Table 1 above will lead to this phenomenon.

Appendix A. Examining how many gravitons might be produced by initially Planck sized black holes

From [5] Alexander D. Dolgov, Damian Ejlli inform us that a mass of a primordial black hole is

$$M\left(early-black-hole\right)\approx 4\times 10^{38}\cdot\left(\frac{t(\,formation)}{\mathrm{Sec}}\right)\cdot g(grams) \quad (1)$$

A Planck mass is of the value 10^-5 grams, i.e. almost , is then obtainable when

$$t(\,formation) \approx 10^{-43}\,\mathrm{Sec}$$

$$\Rightarrow M\left(early-black-hole\right) \approx 10^{-5}\,g(grams) \qquad (2)$$

Note

$$t(\,formation) \approx 10^{-43}\,\mathrm{Sec} \geq 5.39 \times 10^{-44}\,s = Planck-time$$

leads to almost a Planck Mass

$$2.176434(24)\times 10^{-5}\,_{\mathrm{g}} = M\left(Planck-mass\right) \qquad (3)$$

The mechanism of how Plank sized black holes could generate GW comes from, as given in [5] initial friction in the early universe environment, leading to coupling of early primordial binary black hole systems which in turn would collapse and form larger black holes, i.e. in fact the argument in [20] is stated in page 15 as follows

Quote

For PBH masses below a few grams dynamical friction would be an efficient mechanism of PBH cooling leading to frequent binary formation. Moreover, dynamical friction could result in the collapse of small PBHs into much larger BH with the mass of the order of Mb (18). This process would be accompanied by a burst of GW emission

End of quote

What is called Mb in this situation is given by, in [5] on page 4

Quote

As we see in what follows, generation of gravitational waves would be especially efficient from such high density clusters of primordial black holes. Let us assume that the spectrum of perturbations is the flat Harrison-Zeldovich one and that a perturbation with some wavelength λ

crossed horizon at moment t in. The mass inside horizon at this moment was:

$$Mb(t\ in) = m2\ P\ lt\ in. \quad (4)$$

It is the mass of the would-be high-density cluster of PBHs

End of quote

We then from here have the mechanism of black hole formation comes from binary pair formation of small black holes which collapse into a larger set of black holes. This chain of BH pair production and collapse would then lead to an accretion procedure along the lines of Eq. (21). Eventually these black hole clusters would form the mega black holes as seen in the center of spiral galaxies.

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