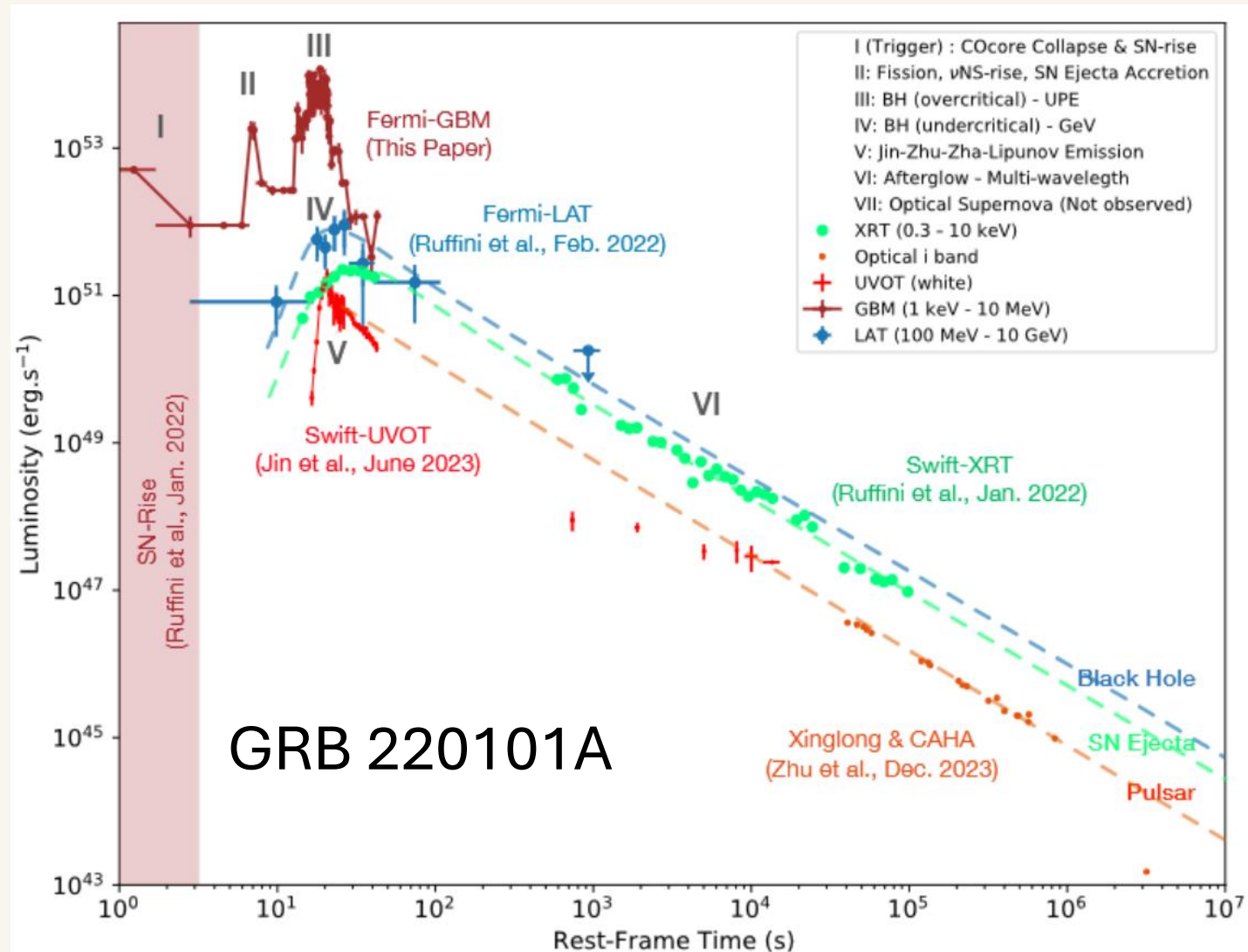




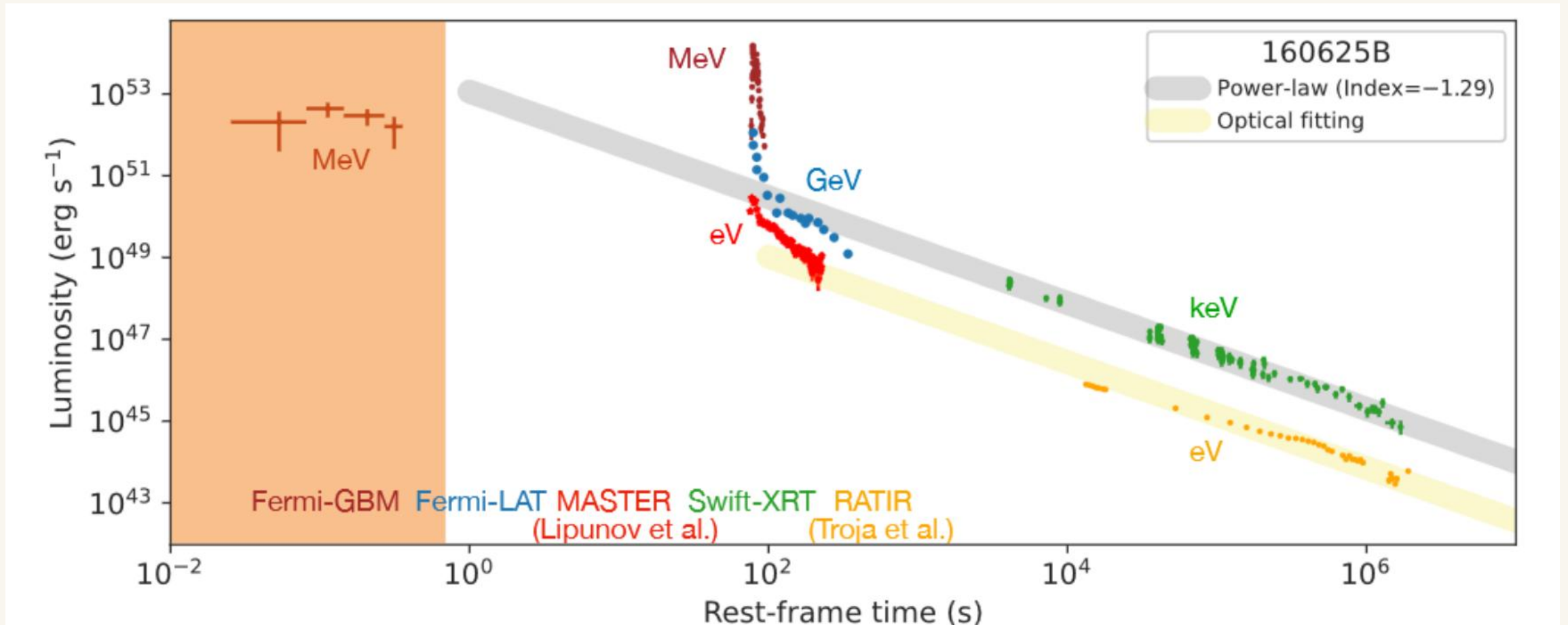
Estimating Black Hole Mass from GeV spindown

Ridha Fathima Mohideen Malik
7th Galileo - Xu-Guangqui meeting
July 10, 2025

BdHN model



GRB 160625B



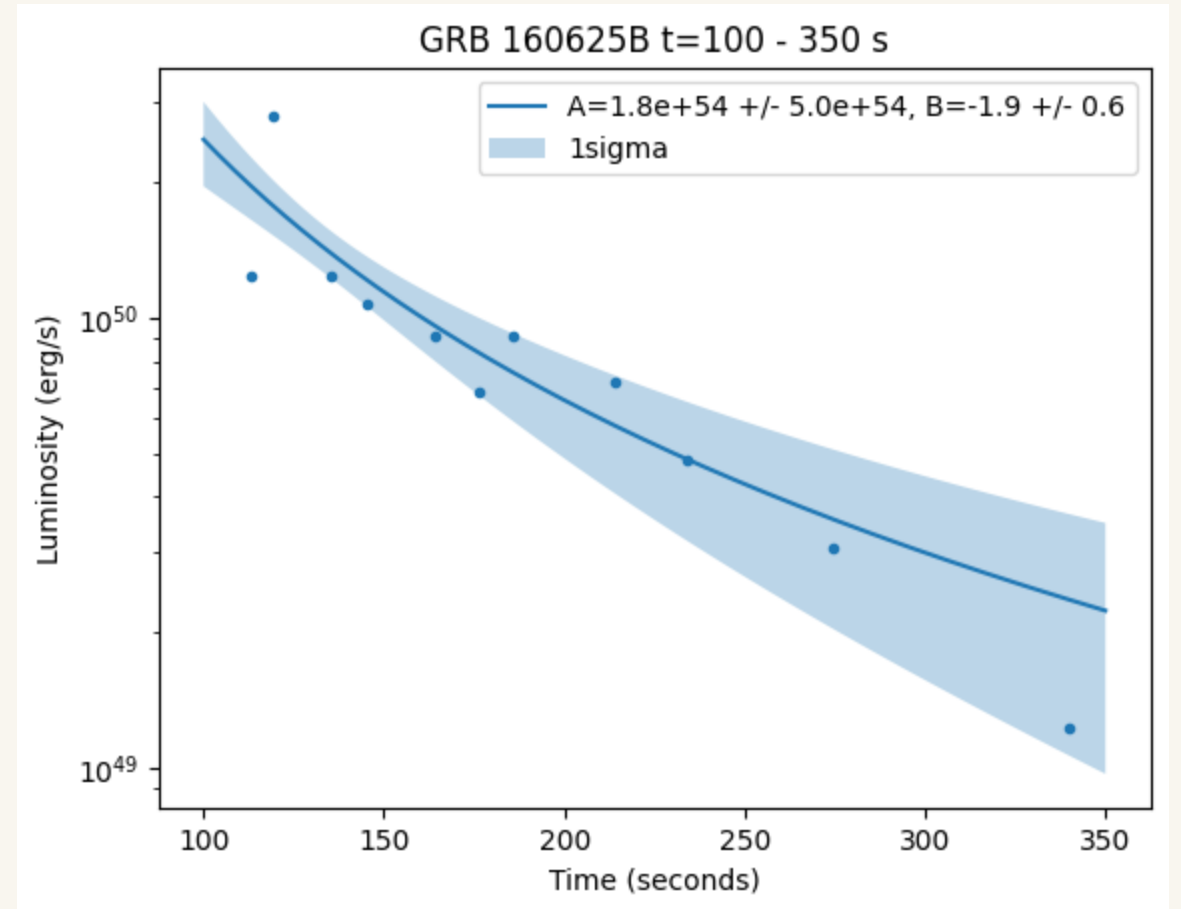
Lower bound for initial mass

$$L_{GeV} = A t_0^\beta$$

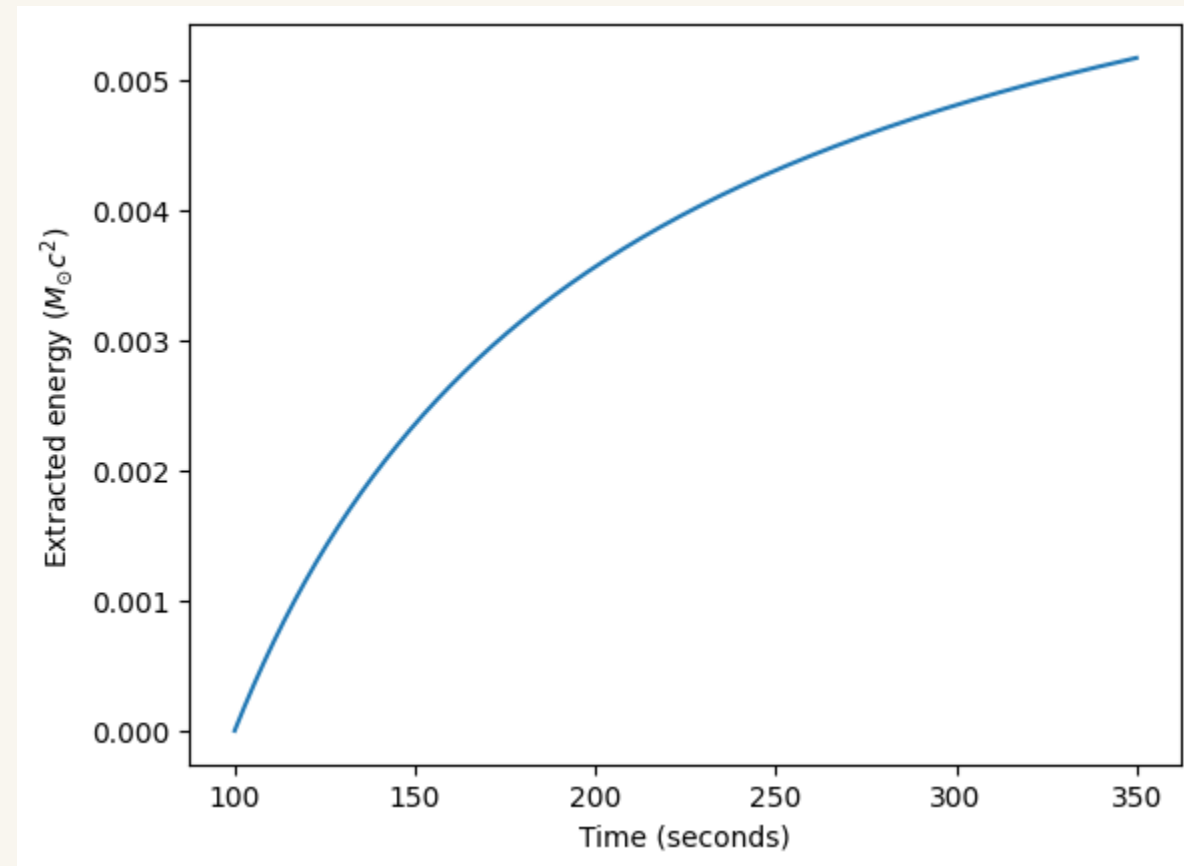
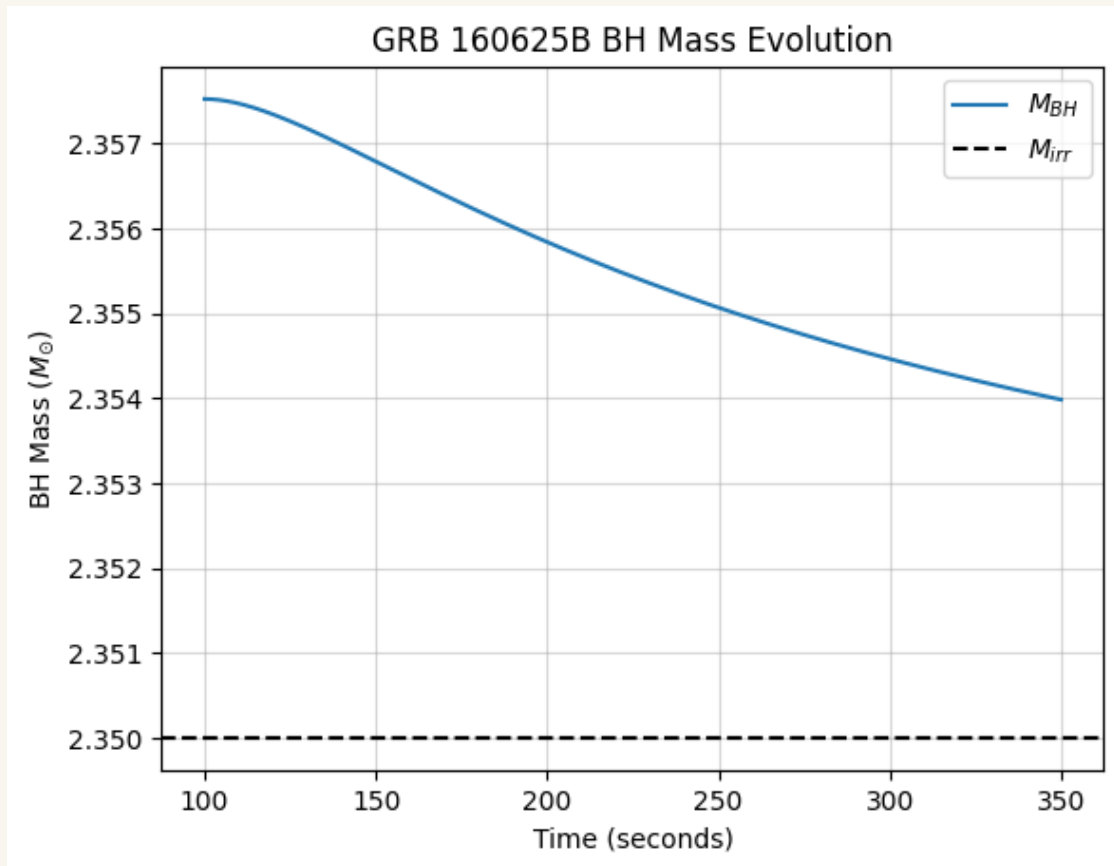
$$E_{GeV} = \int L_{GeV} dt = A \frac{t_0^{1+\beta}}{|1+\beta|}$$

$$\tilde{E}_{GeV} = E_{GeV}(1 - \cos\theta)$$

$$M_{BH,0} = M_{GeV} + M_{irr}$$



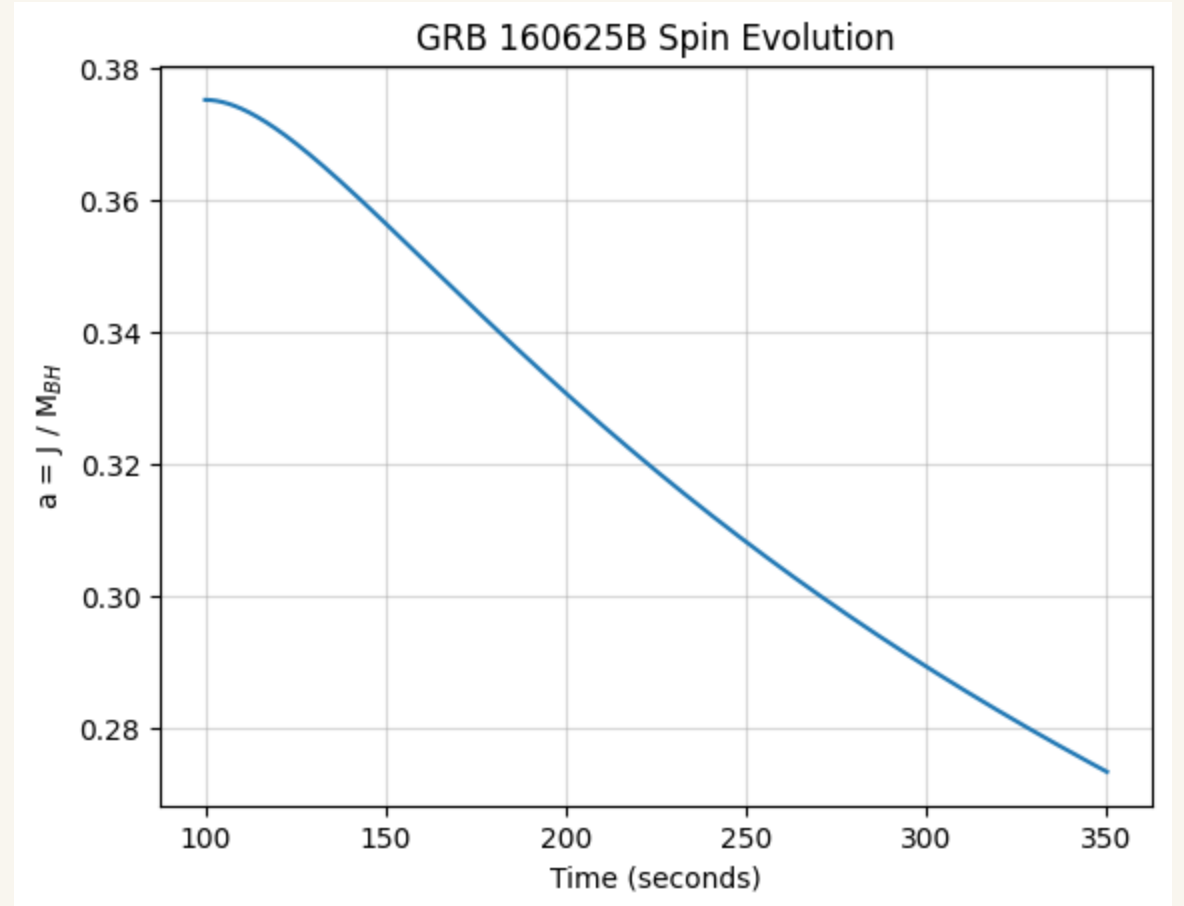
$$M_{BH} = \overset{2.36 M_{\odot}}{M_{BH,0}} - \overset{2.35 M_{\odot}}{M_{irr}} - M_{ext}$$



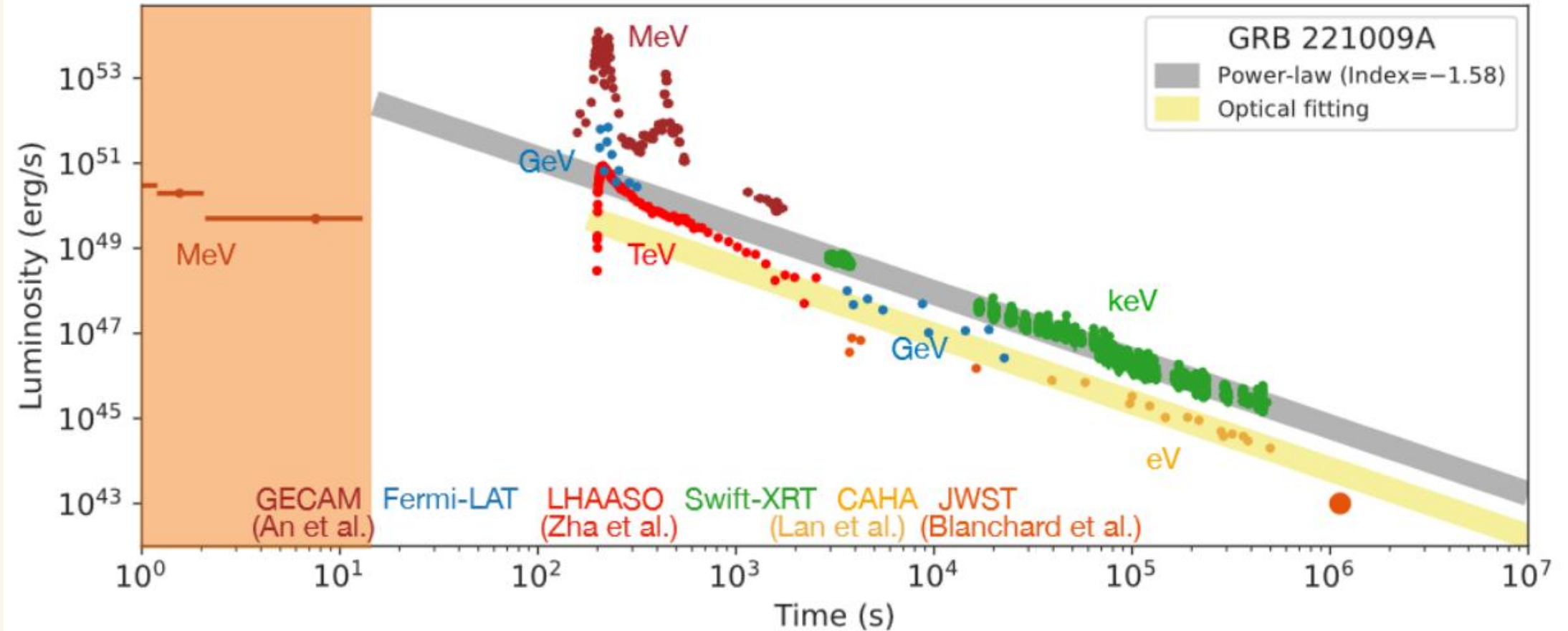
Spin evolution

$$M_{BH}^2 = M_{irr}^2 + \frac{a^2 M_{BH}^2}{4 M_{irr}^2}$$

$$a = 2M_{irr} \sqrt{1 - \left(\frac{M_{irr}}{M_{BH}}\right)^2}$$



GRB 221009A – Ultra Long BOAT



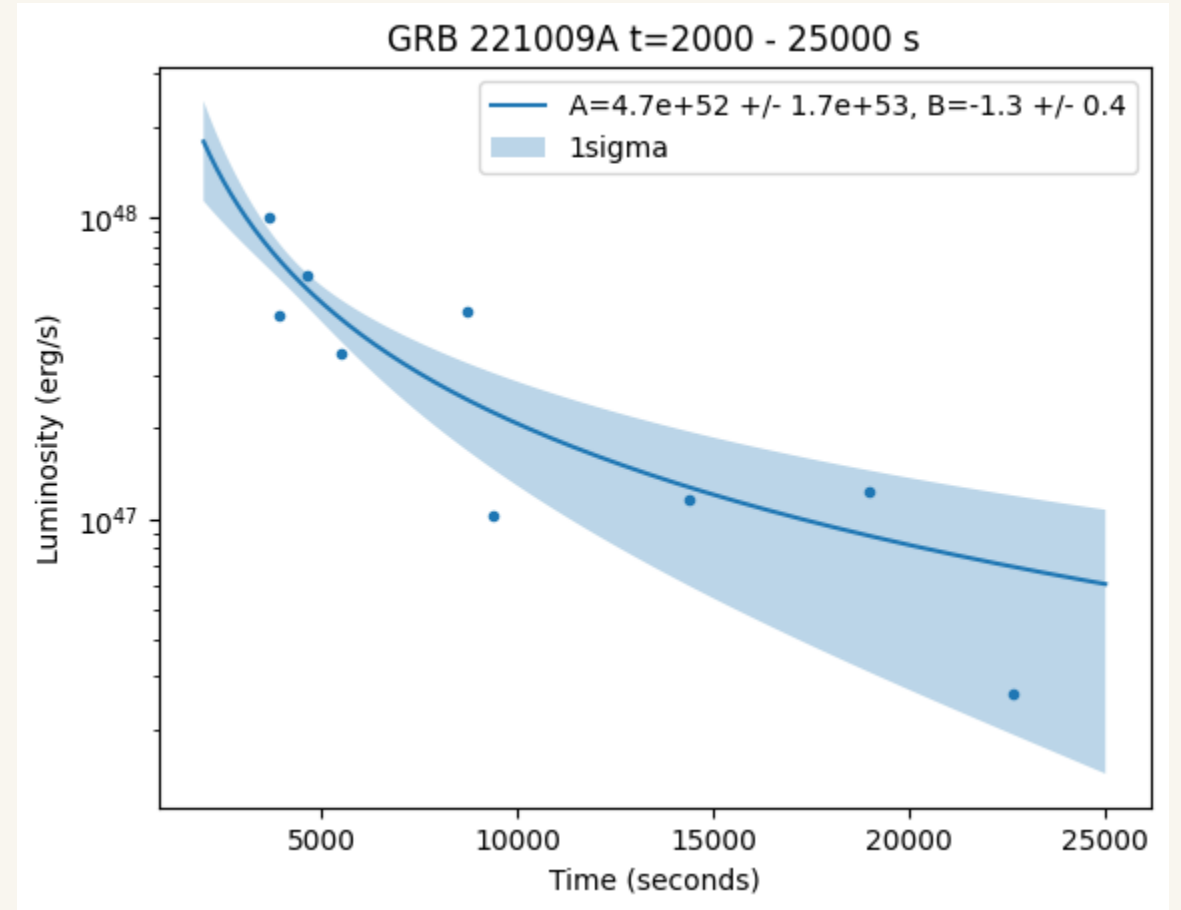
Lower bound for initial mass

$$L_{GeV} = At_0^\beta$$

$$E_{GeV} = \int L_{GeV} dt = A \frac{t_0^{1+\beta}}{|1+\beta|}$$

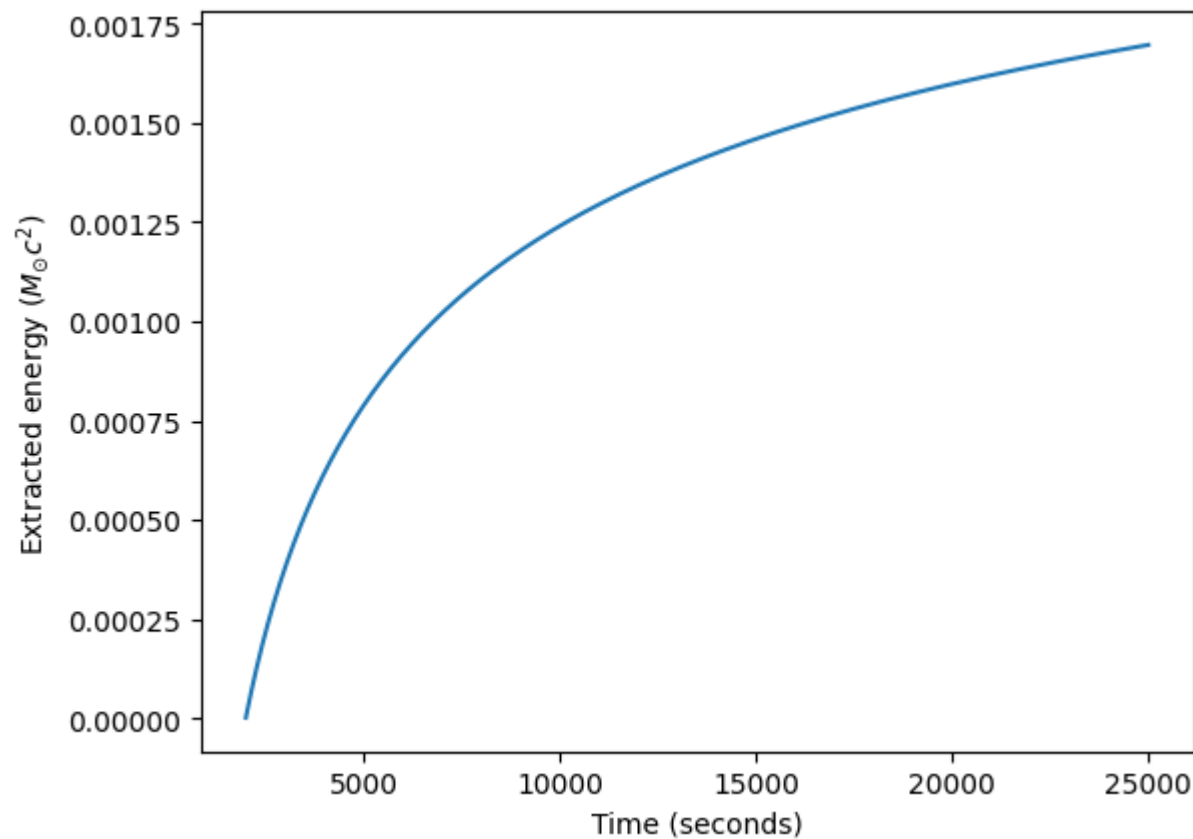
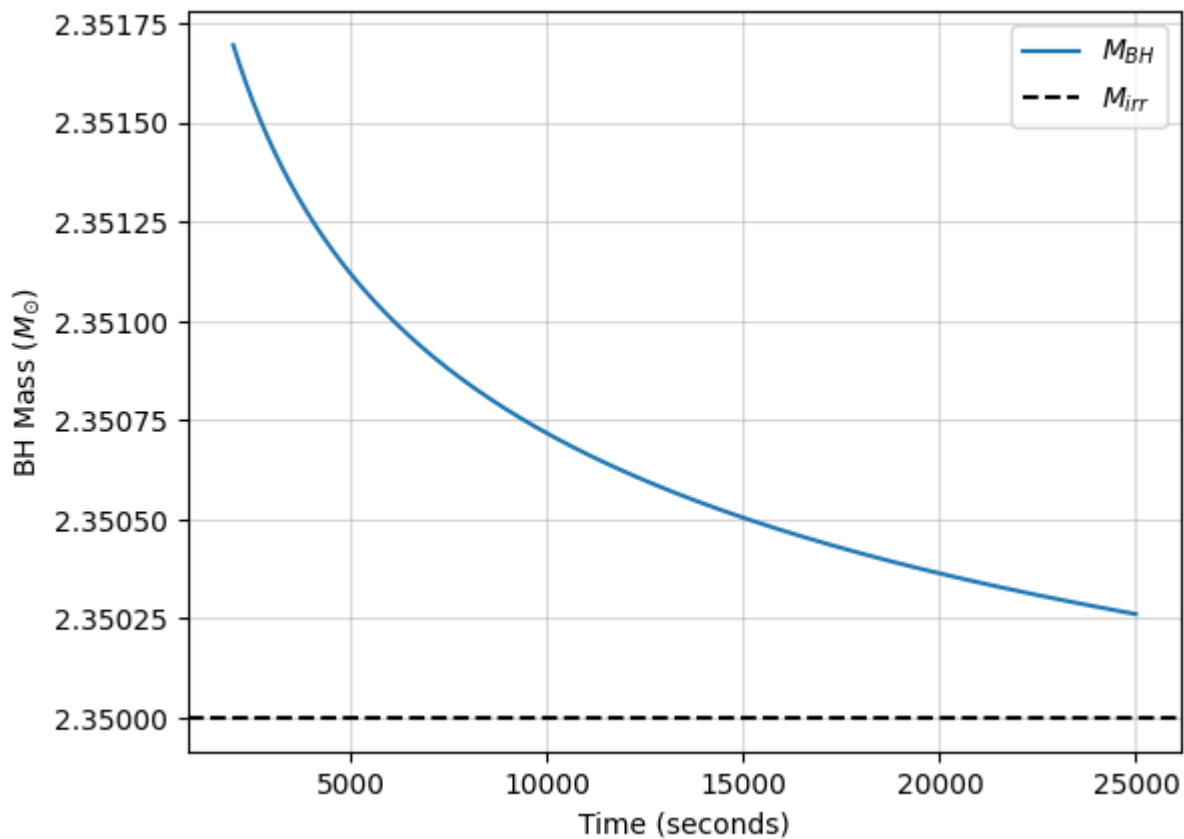
$$\tilde{E}_{GeV} = E_{GeV}(1 - \cos\theta)$$

$$M_{BH,0} = M_{GeV} + M_{irr}$$



$$M_{BH} = \overset{2.358 M_{\odot}}{\underbrace{M_{BH,0}}} - \overset{2.350 M_{\odot}}{\underbrace{M_{irr}}} - M_{ext}$$

GRB 221009A BH Mass Evolution



Spin evolution

$$M_{BH}^2 = M_{irr}^2 + \frac{a^2 M_{BH}^2}{4 M_{irr}^2}$$

$$a = 2M_{irr} \sqrt{1 - \left(\frac{M_{irr}}{M_{BH}}\right)^2}$$



Summary

GRB	Initial BH mass ($M_{\odot}$)	At the end of GeV emission ($M_{\odot}$)	Initial a	At the end of GeV emission
160625B	2.3575	2.3540	0.38	0.27
221009A	2.3517	2.3503	0.18	0.07
220101A	?	?	?	?