

17th Marcel Grossmann Meeting

7-12 July 2024



On the origin of the spectral
features observed in the cosmic ray
spectrum

Sarah Recchia

INAF Brera (Merate)

Overview

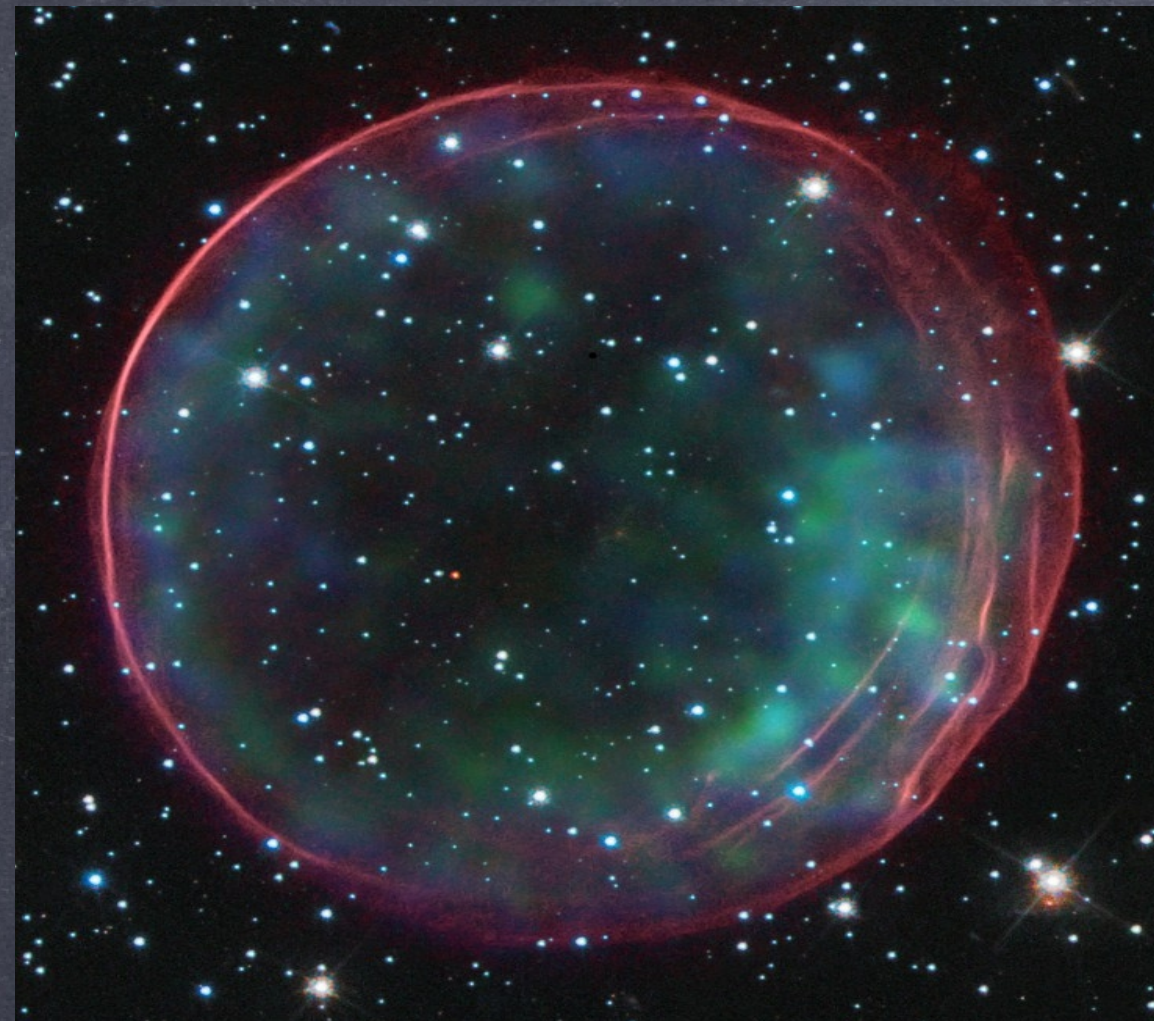
Recchia & Gabici (2023)

- Spectral features in the CR data - new results
- GeV - PeV
- how to interpret features - propagation, sources ... ?
- CRs up to \sim TeV - propagation and grammage CRs
- multi TV - PV range - sources and maximum energy
- microphysics of CR transport ? Galactic PeVatrons?

Breaks in the CR spectrum

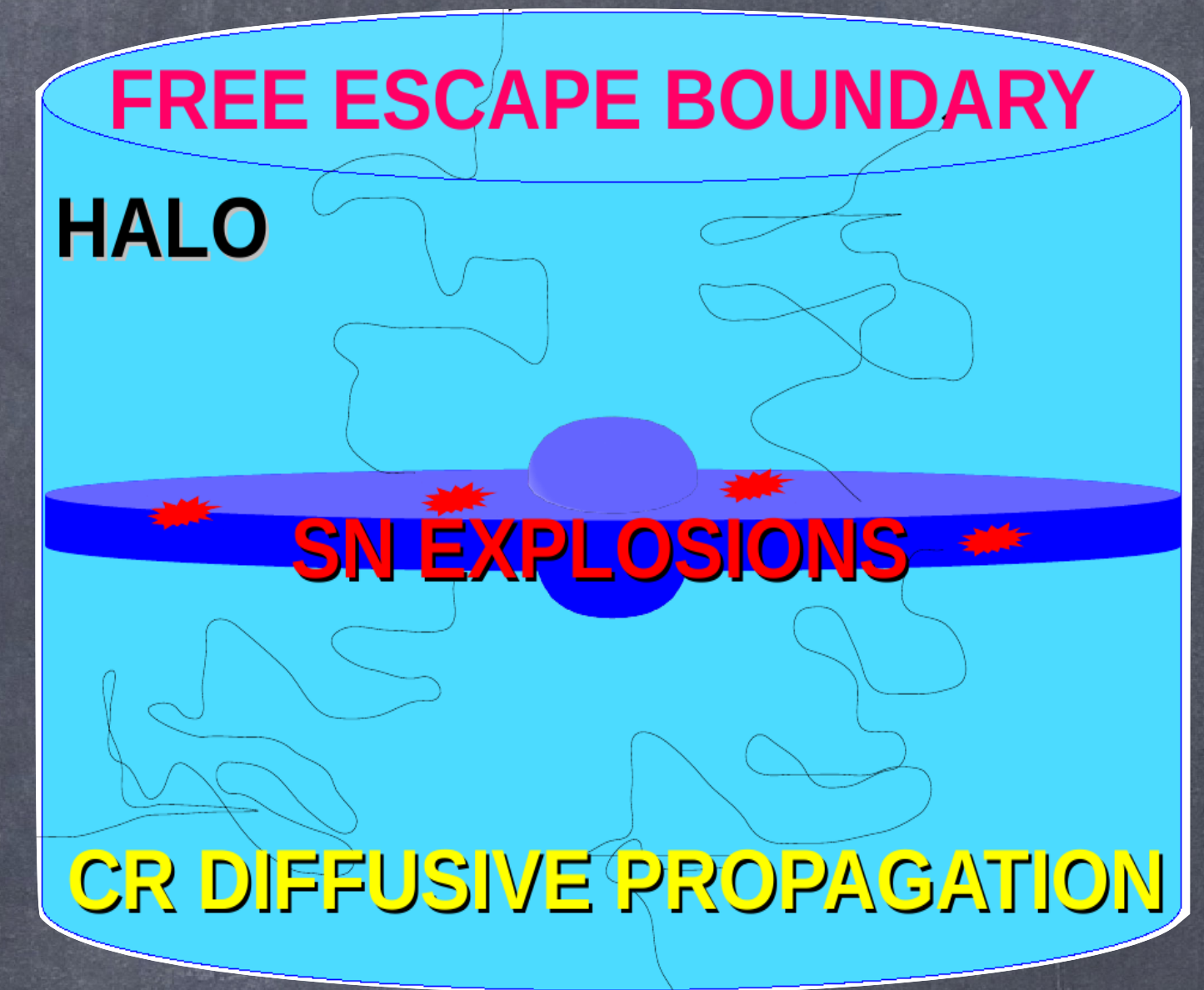
CRs in a nutshell - SNR paradigm

~ 10% of SNR power



Equilibrium

$$N_{\text{CR}} \propto Q_{\text{CR}}/D \propto E^{-2.7}$$



diffusive shock acceleration

- power-law spectrum $Q_{\text{CR}} \propto E^{-2}$
- rigidity dependent $R \propto p/Z$
- protons to the knee? $\approx 3 \text{ PeV}$

Galactic propagation

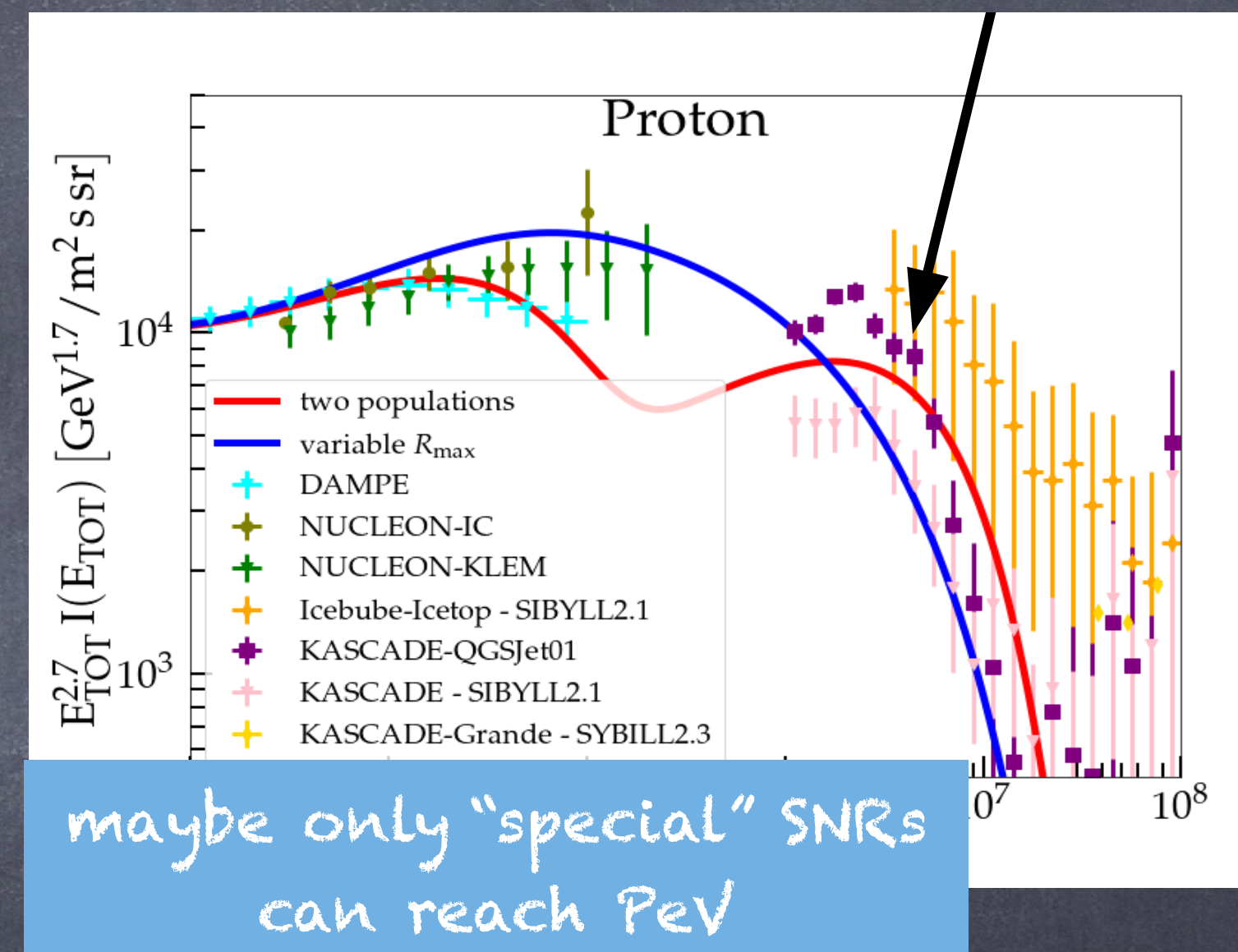
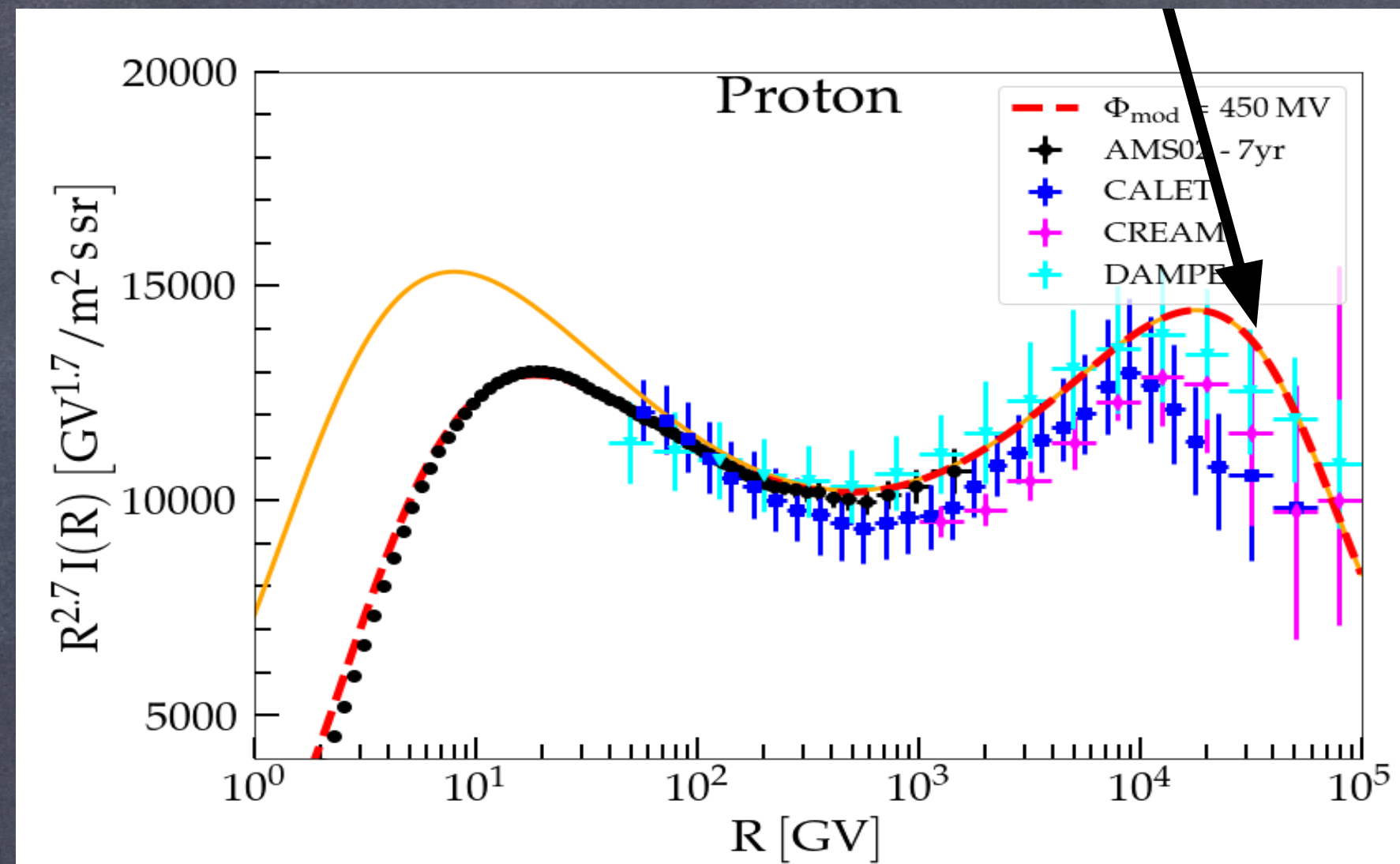
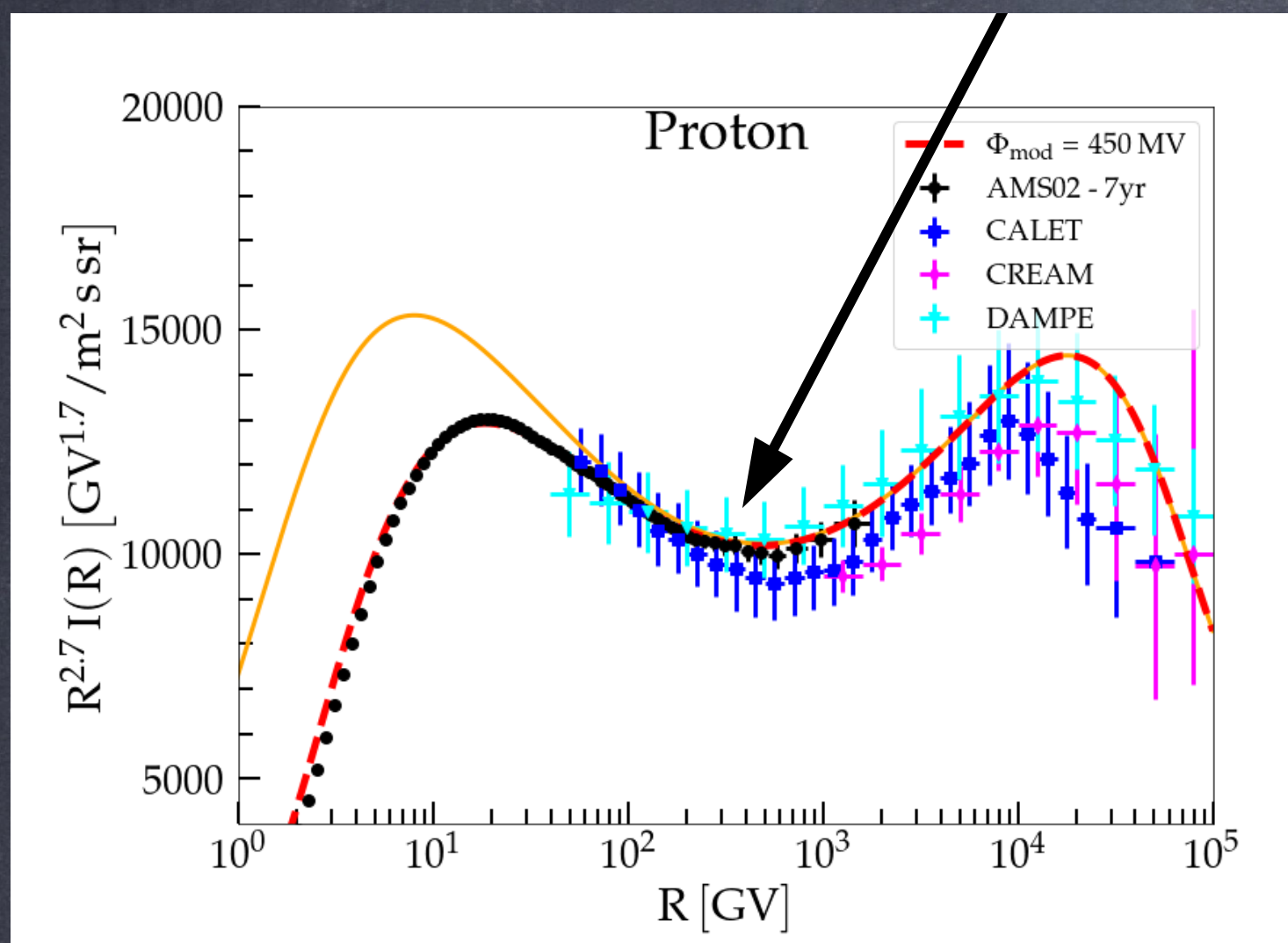
- B/C, unstable isotopes...
- grammage, energy-dependent escape
- $D(E) \propto E^{0.3-0.7}$, $H \sim \text{few kpc}$

Breaks in GV-PV range

~ 300 GV

"Dampe" ~ 15 TV

"Knee" ~ 3 PV

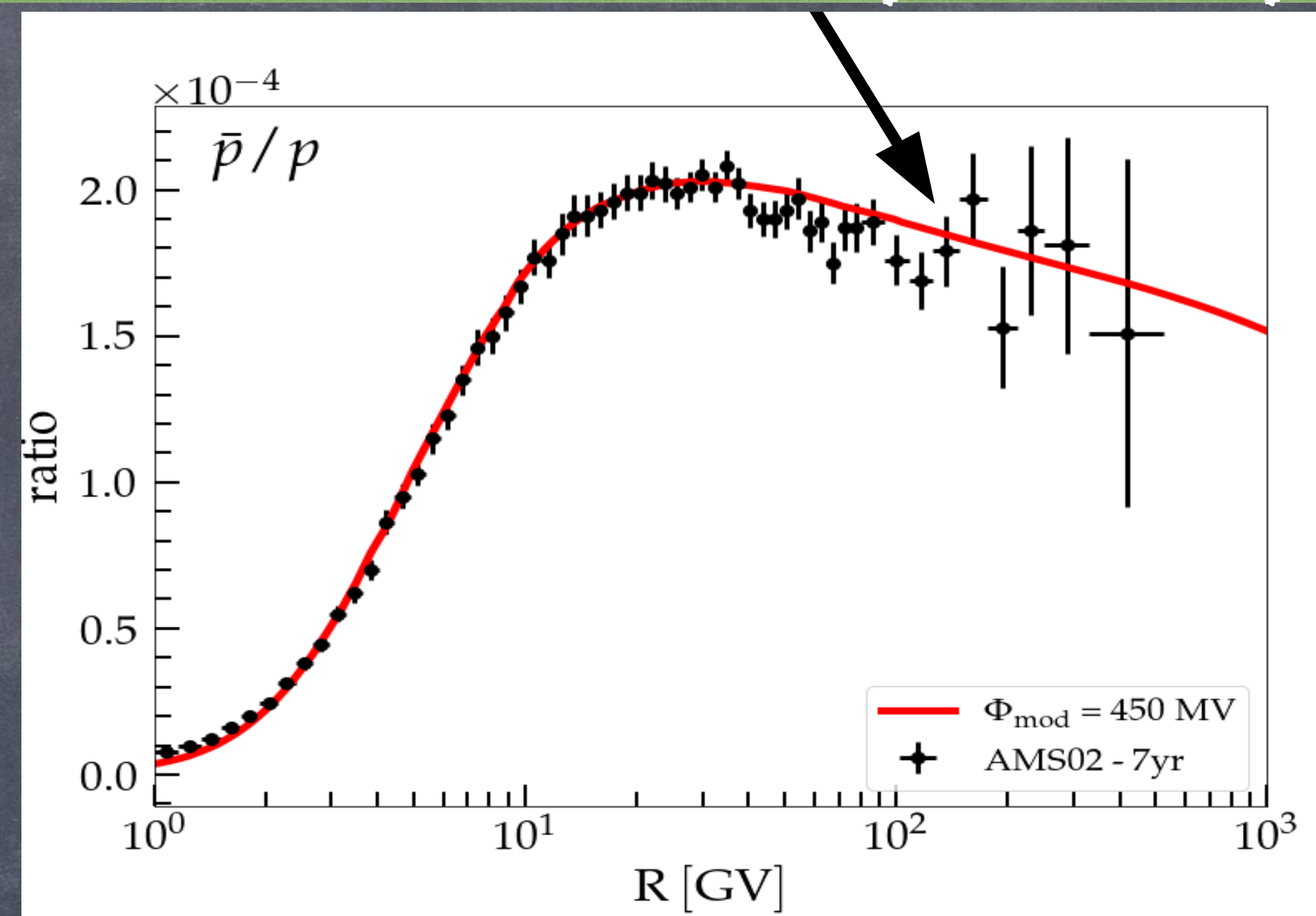
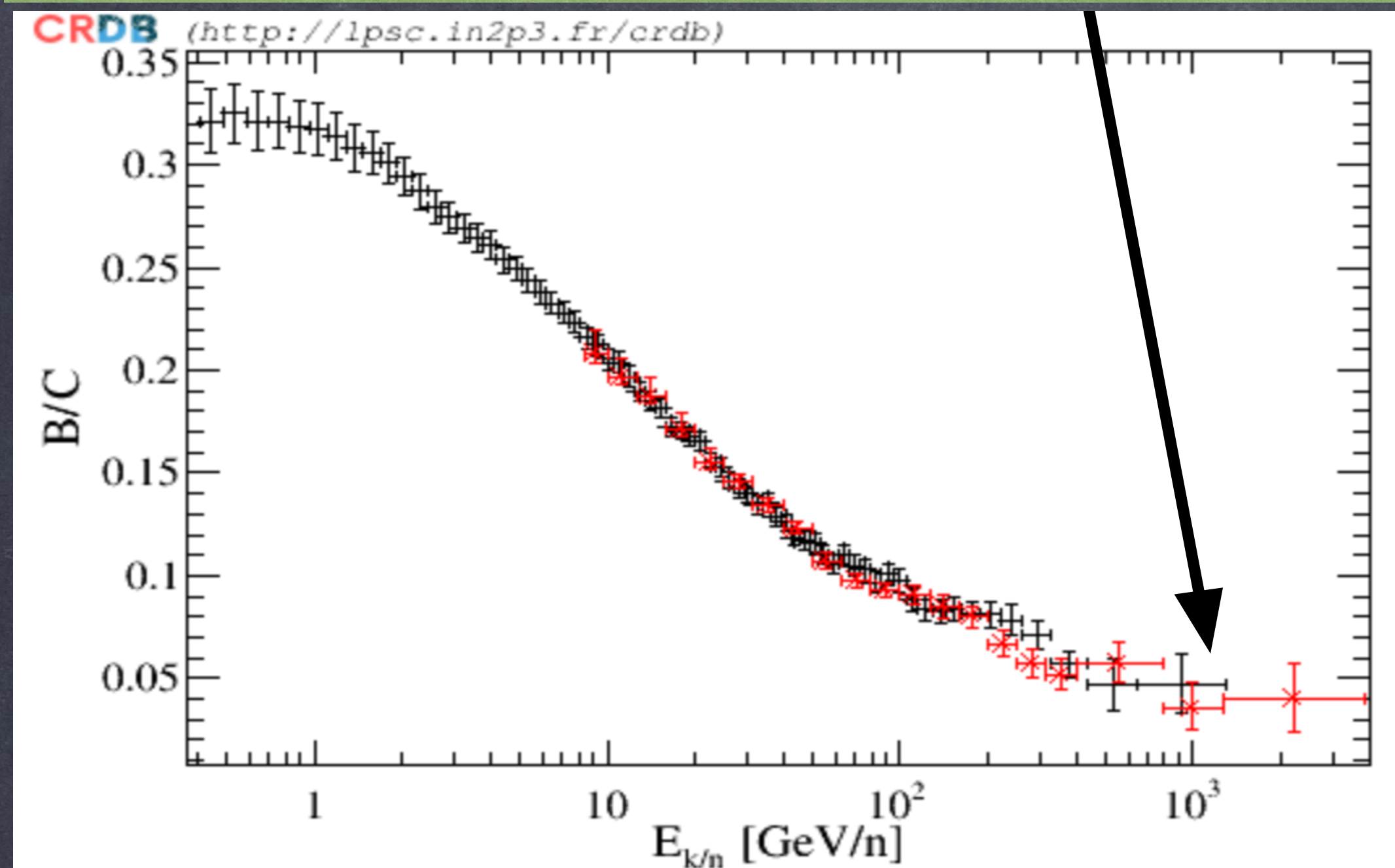


- hardening by ~ 0.1
- confirmed in secondary nuclei, by ~ 0.2
- change in propagation

- local source? (most popular in literature)
- "special" sources
- features of acceleration?
- change in propagation?

- most SNRs accelerate up to ~ 3xZ PeV ?
- overlap of E_max of different species
- difficult for current theories

Hardening of B/C at $\sim \text{TeV/n}$ \nsubseteq pbar/p



- explained by flatter $D(R)$ above $\sim 300 \text{ GV}$?
- where is the grammage accumulated? role of sources?
- secondaries produced at/nearby accelerators?
- effect of sources is unavoidable but not clear if enough

Tomassetti $\&$ Donato (2012)

Bresci et al. 2019

Mertsch et al. (2021)

D'Angelo et al. (2016)

Recchia et al. (2022)

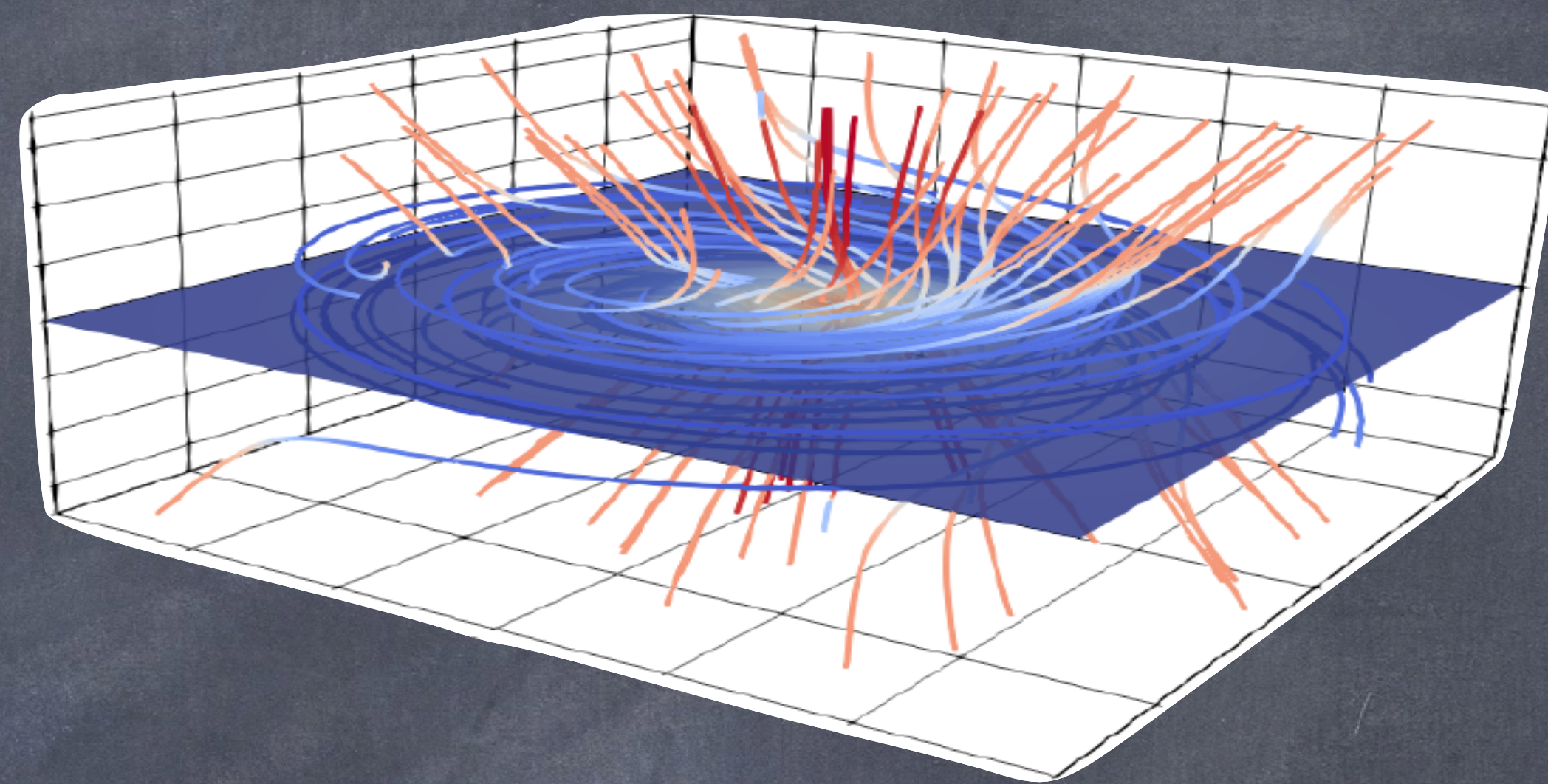
Alternative framework
CR data ~ GV - PV

Alternative framework - CR data \sim GV - PV

Recchia & Gabici (2023)

CR propagation in disk

- weak scattering along B
(along Galactic plane)
damping/anisotropic cascade
- energy-independent perp. transport
- typical diffusion $D(E)$
in Galactic halo
- role of disk emerges above \sim TV

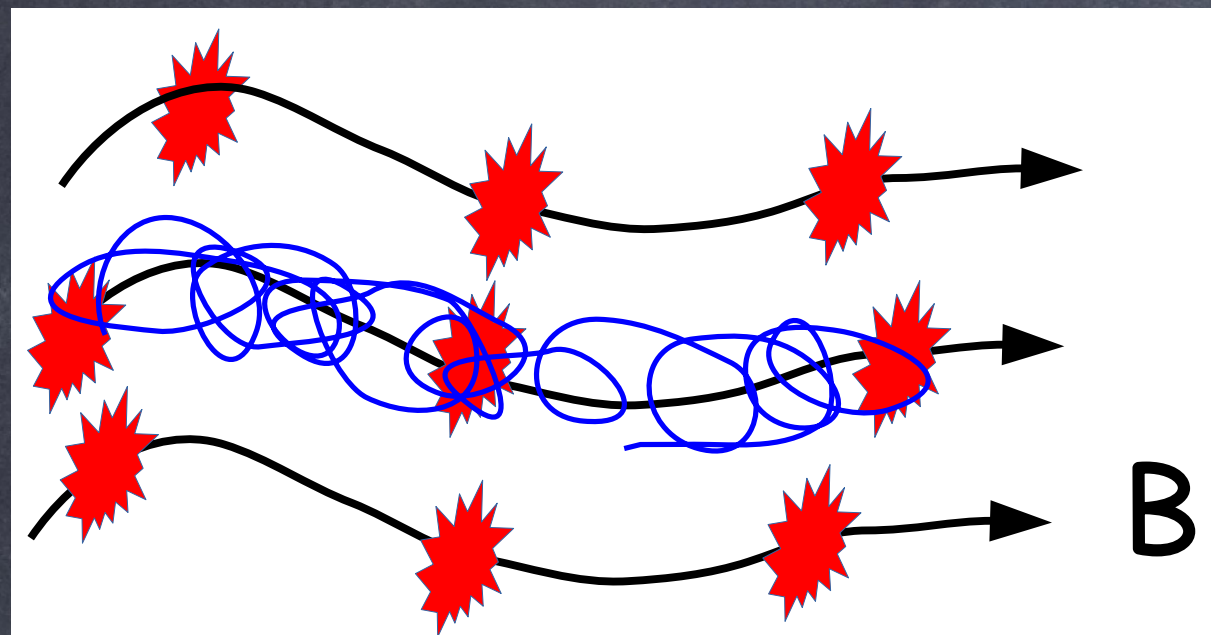


E_{max} of "typical" SNRs

- "Damped break"
 E_{max} of typical SNRs (\sim 50 TV)
- "special" sources can reach the
"knee" (\sim 10-15% luminosity)
- easier with current theories

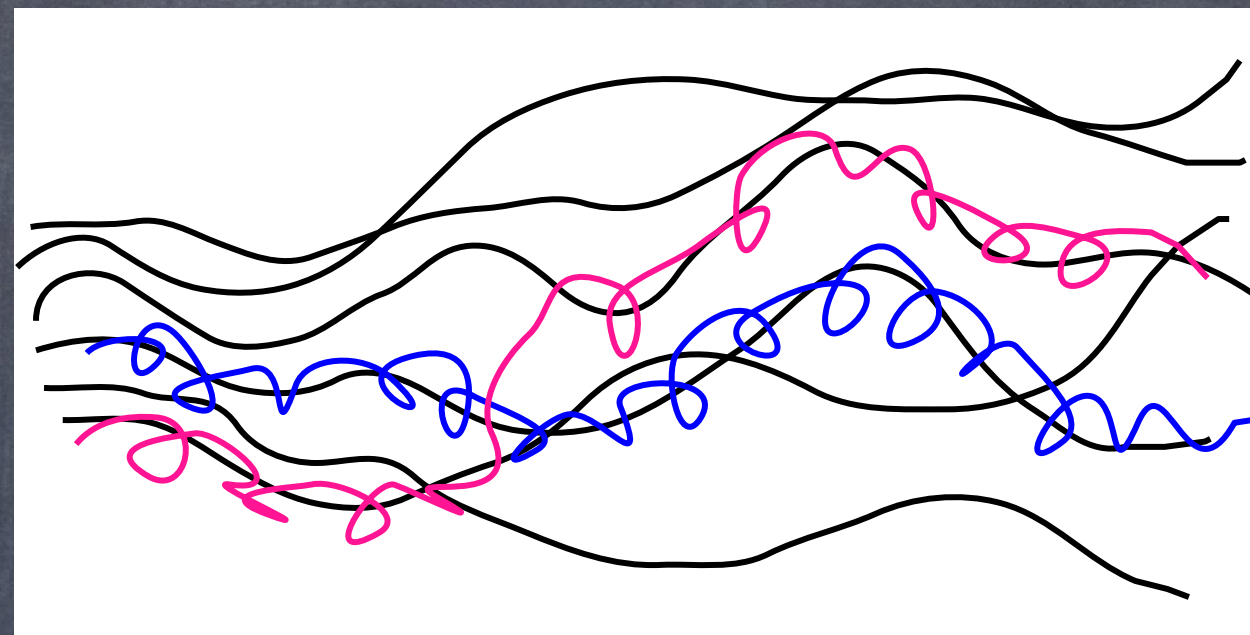
CR transport in (very) short

parallel diffusion



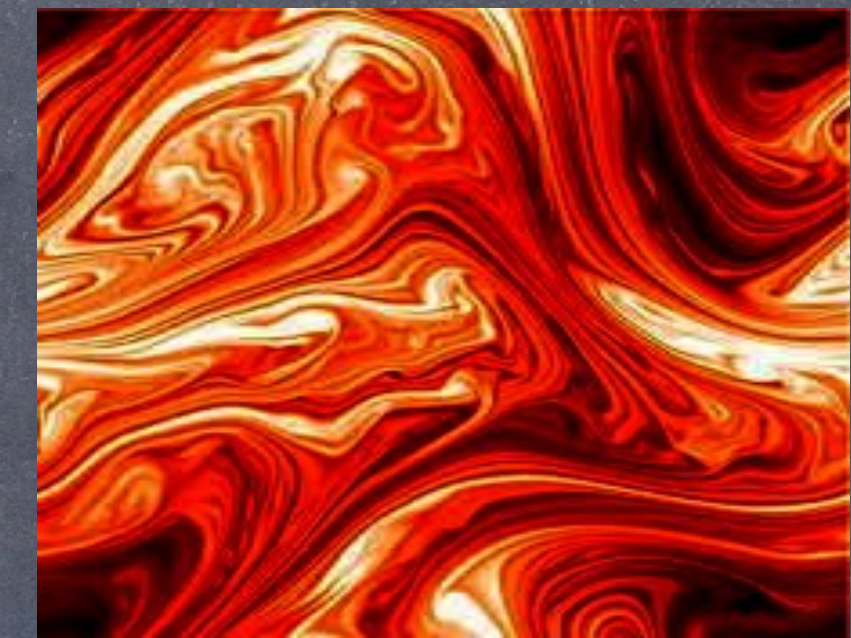
- CR gyromotion
- scattering off waves
- $k \sim 1/r_L$ (resonance)
- scattering mean free path λ_{mfp}
- $D_{\parallel}(E) \propto \lambda_{\text{mfp}}$

perp. transport



- field line random walk
- CR jump between lines
- large-scale perp diffusion
- $D_{\perp}(E) \lesssim D_{\parallel}(E)$

MHD turbulence



- source injection (10s pc)
- cascade to $k \sim 1/r_L$?
- damping?
- Produced by CRs?

Perpendicular diffusion: weak scattering limit

Rechester & Rosenbluth 1978

Chandran 2000

Snodin et al. (2022)

Pezzi & Blasi (2024)

• weak scattering ALONG field lines

▶ scattering along B is inefficient (damping, "wrong" cascade...)

▶ large D_{\parallel} \longrightarrow $\lambda_{\text{mfp}} \gtrsim L_{\text{coh}}$

▶ within L_{coh} , $z(t) \sim vt$

• diffusive motion of field lines

▶ D_m [length] \longrightarrow field line diffusion coefficient

▶ large scale turbulence ($\gg r_L$)

▶ D_{\perp} becomes energy-independent

$$D_m v \approx 3 \times 10^{28} \left(\frac{D_m}{\text{pc}} \right) \text{cm}^2/\text{s},$$

Alternative framework
CR data ~ GV - PV

Model of CR transport in the disk-halo

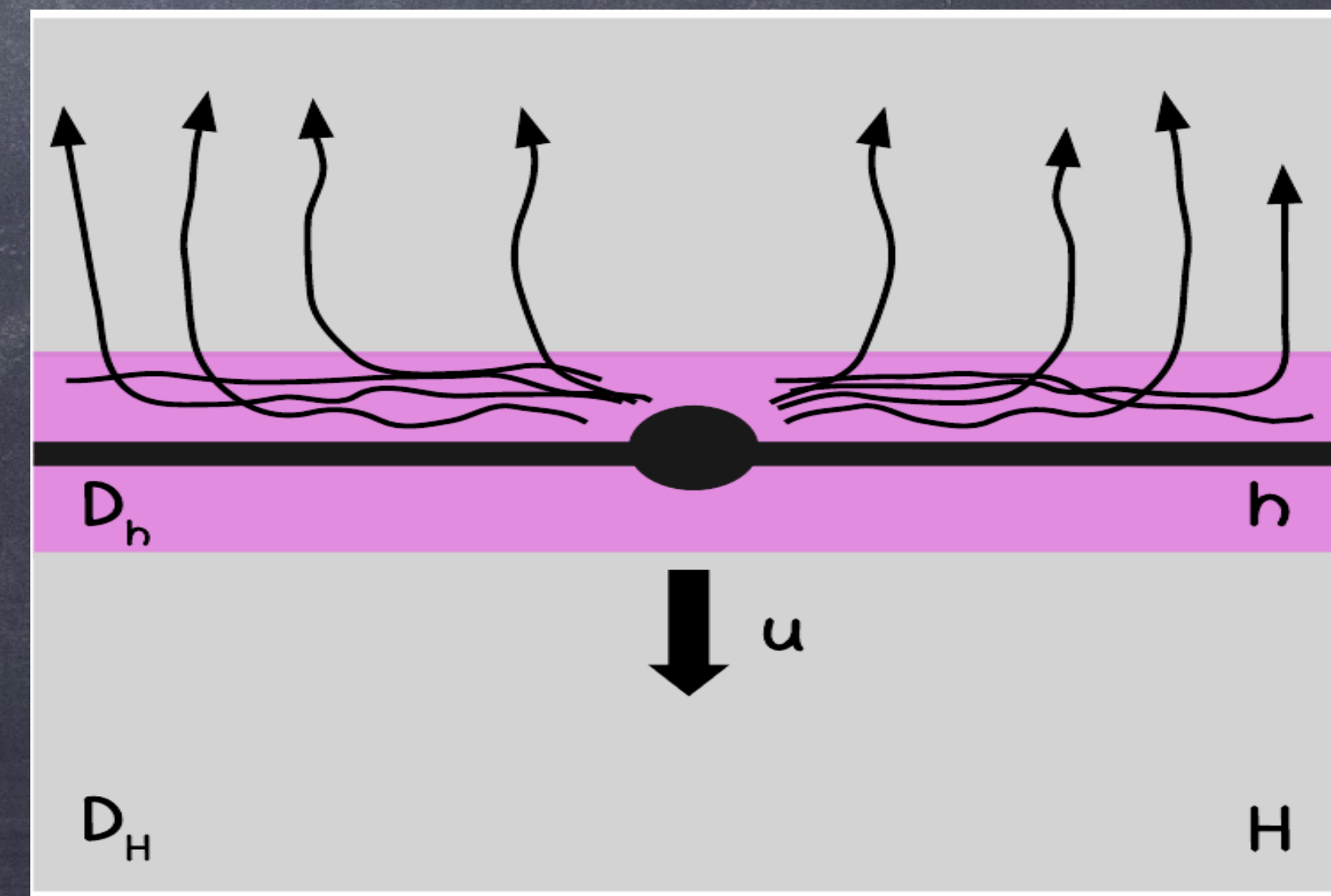
Galactic disk

- ▶ field lines mostly along the GP
- ▶ weak scattering along BO (along GP)
- ▶ injection/spallation in thin gaseous disk

$$D_m v \approx 3 \times 10^{28} \left(\frac{D_m}{\text{pc}} \right) \text{cm}^2/\text{s},$$

Galactic halo

- ▶ $D(E) \sim 10^{28} \text{cm}^2/\text{s} E^{0.7}$
- ▶ advection away from disk
- ▶ size $H \sim 4 \text{kpc}$



Analytic solution of the CR transport

flux of stable nuclei vs E_{kin}/n

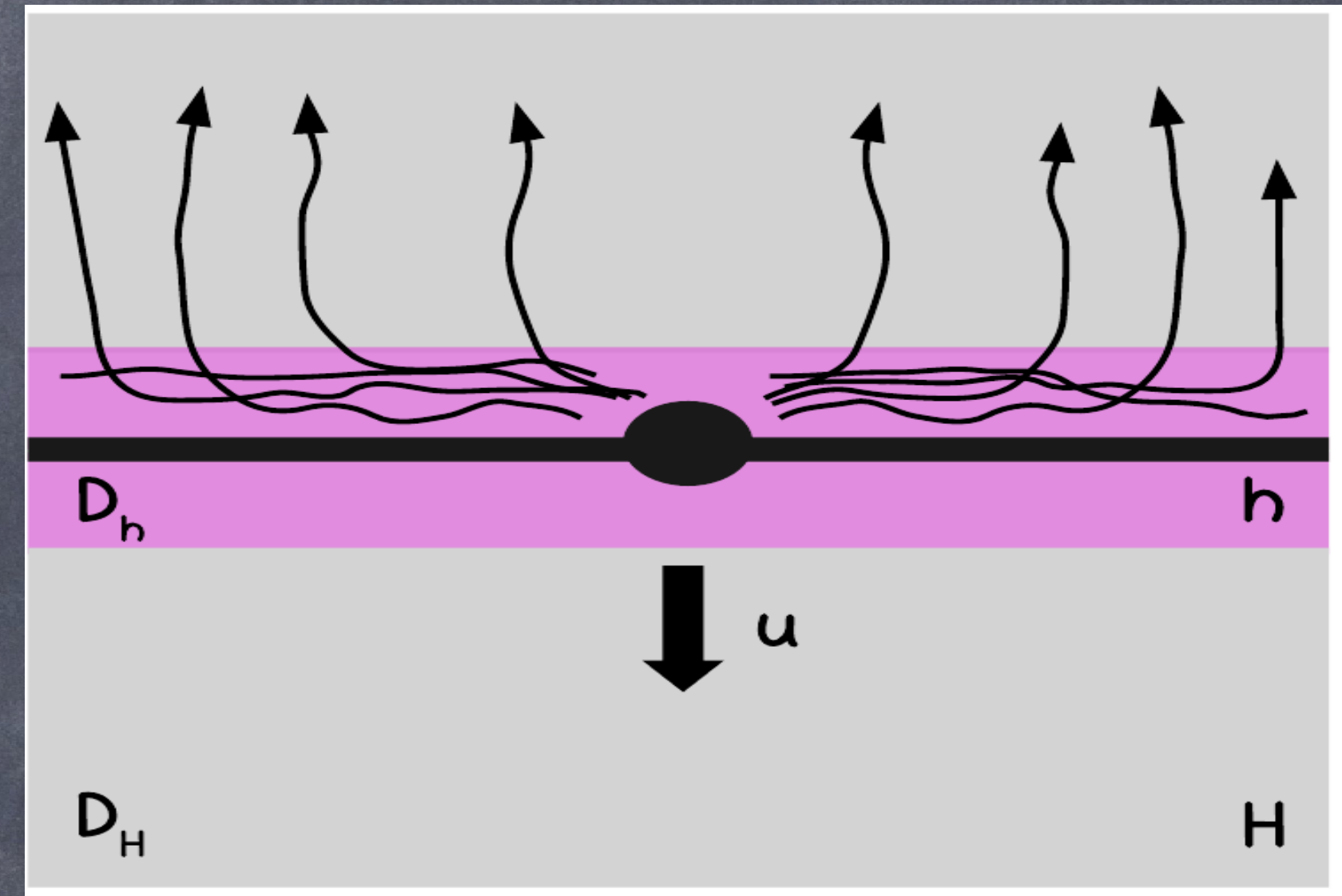
$$I_{\alpha 0}(E_k) = \frac{\tau_{\alpha}^{hH}}{1 + n_d \frac{h_d}{h} v(E_k) \sigma_{\alpha} \tau_{\alpha}^{hH}} \times \left[\frac{1}{2h} Q_{\alpha,src} + n_d \frac{h_d}{h} Q_{\alpha,spall} \right]$$

$$\begin{cases} Q_{\alpha,src} \equiv c A p^2 q_{0\alpha} \end{cases}$$

inj. sources

$$\begin{cases} Q_{\alpha,spall} \equiv \sum_{\beta > \alpha} v(E_k) \sigma_{\beta\alpha}(E_k) I_{\beta}(E_k) \end{cases}$$

inj. spallation



$$\tau_{\alpha}^{hH} \equiv \frac{h^2}{D_h} + \frac{hH}{D_H} \frac{1 - \exp^{-\frac{uH}{D_H}}}{\frac{uH}{D_H}}$$

residence time
in disk

$$X_{\alpha}(E_k) = \left(n_d \frac{h_d}{h} \right) \mu v(E_k) \tau_{\alpha}^{hH},$$

grammage

$$\frac{n_s}{n_p} \sim \frac{\sigma_s X}{\mu m_p}$$

$$X = \mu m_p c n_d \tau_d$$

Analytic solution of the CR transport

residence time in disk

$$\tau_{\alpha}^{hH} \equiv \frac{h^2}{D_h} + \frac{hH}{D_H} \frac{1 - \exp^{-\frac{uH}{D_H}}}{\frac{uH}{D_H}}$$

smooth transition

$$R^* = \left[80 \frac{H}{4 \text{ kpc}} \frac{h}{150 \text{ pc}} \frac{D_m}{\text{pc}} \frac{10^{28} \text{ cm}^2/\text{s}}{D_0} \right]^{1/\delta} \text{ GV.}$$

$\approx 6 \text{ TV}$	$(\delta = 0.5)$
$\approx 2 \text{ TV}$	$(\delta = 0.6)$
$\approx 500 \text{ GV}$	$(\delta = 0.7)$
$\approx 200 \text{ GV}$	$(\delta = 0.8)$

diffusion in disk
constant in E

repeated crossings of disk
induced by diffusion in halo
decreases with E due to $D_H \sim E^{0.7}$

Analytic solution of the CR transport

residence time in disk

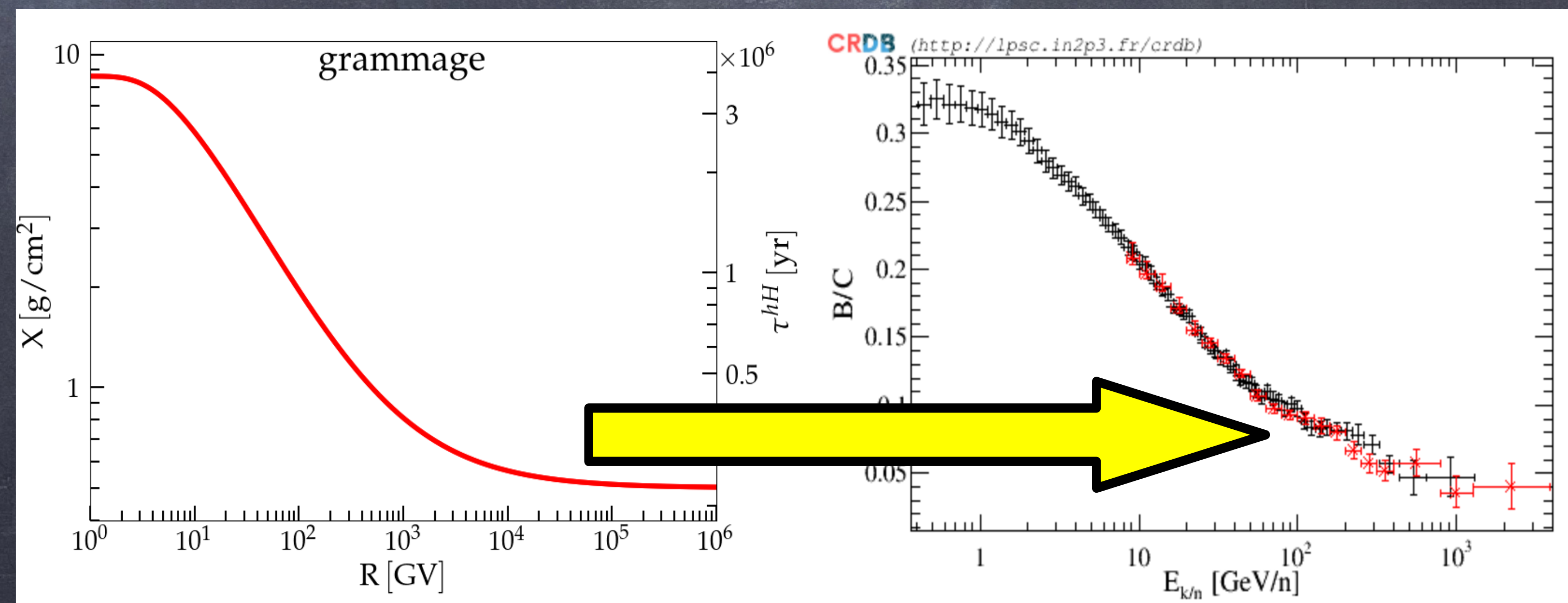
$$\tau_{\alpha}^{hH} \equiv \frac{h^2}{D_h} + \frac{hH}{D_H} \frac{1 - \exp^{-\frac{uH}{D_H}}}{\frac{uH}{D_H}}$$

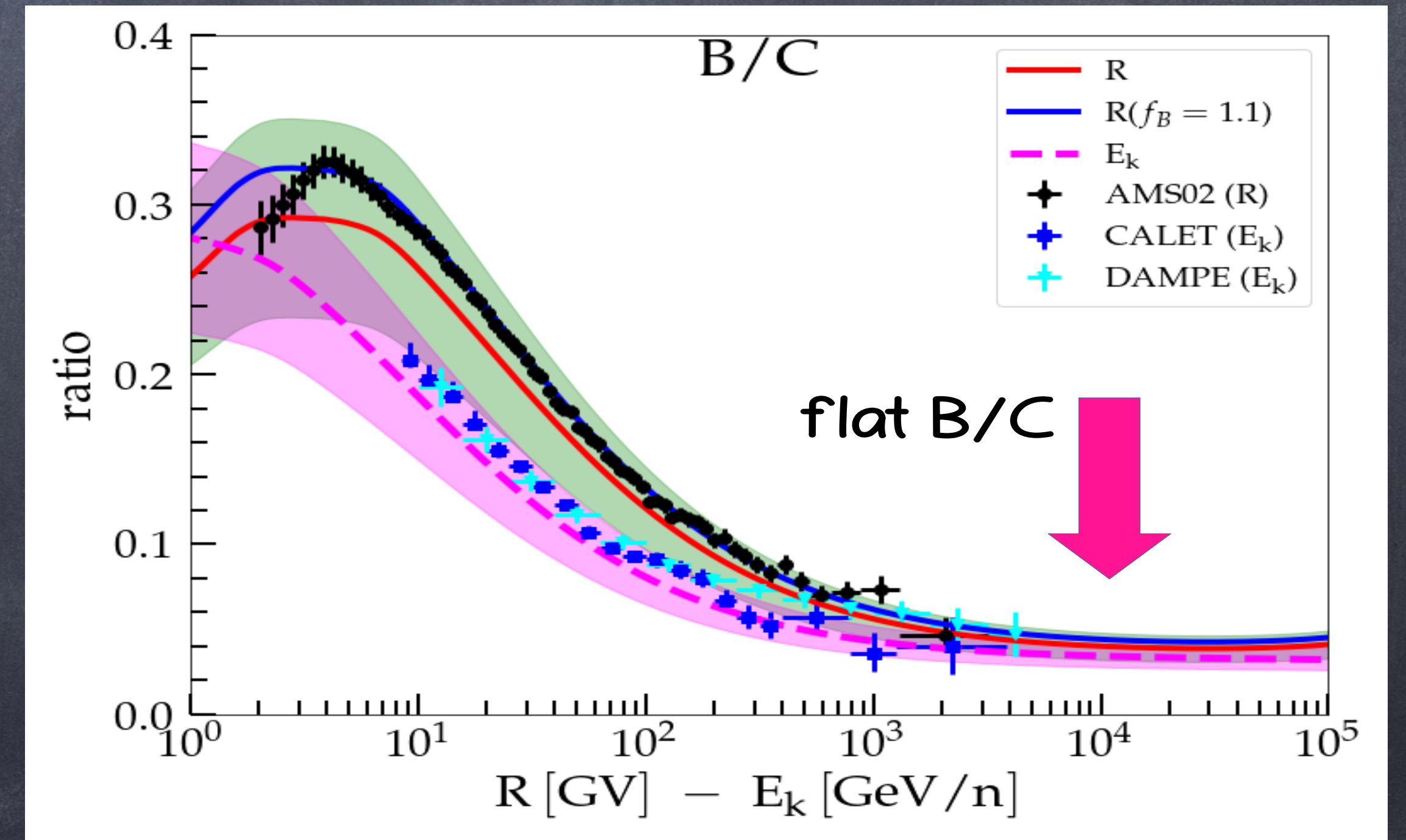
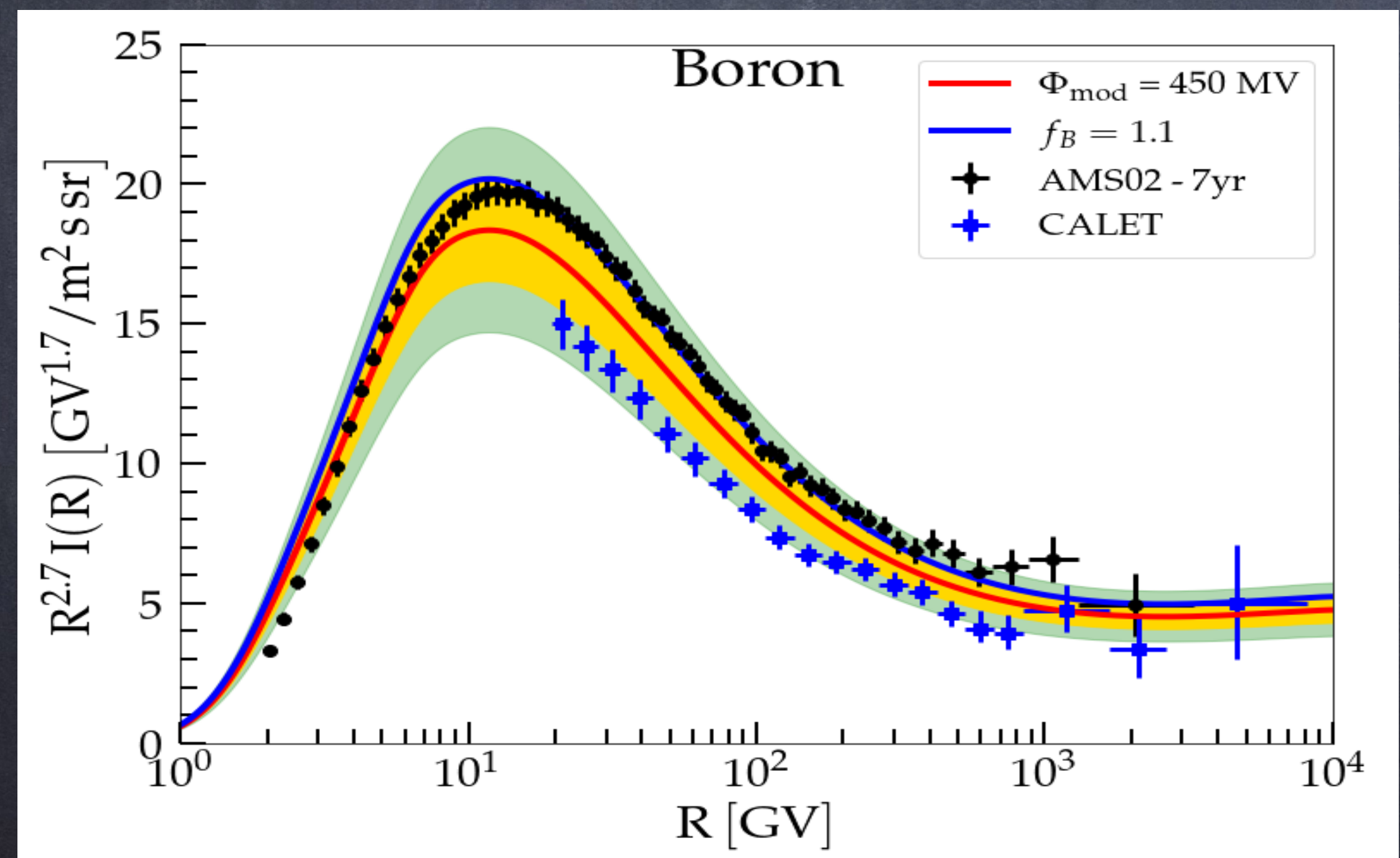
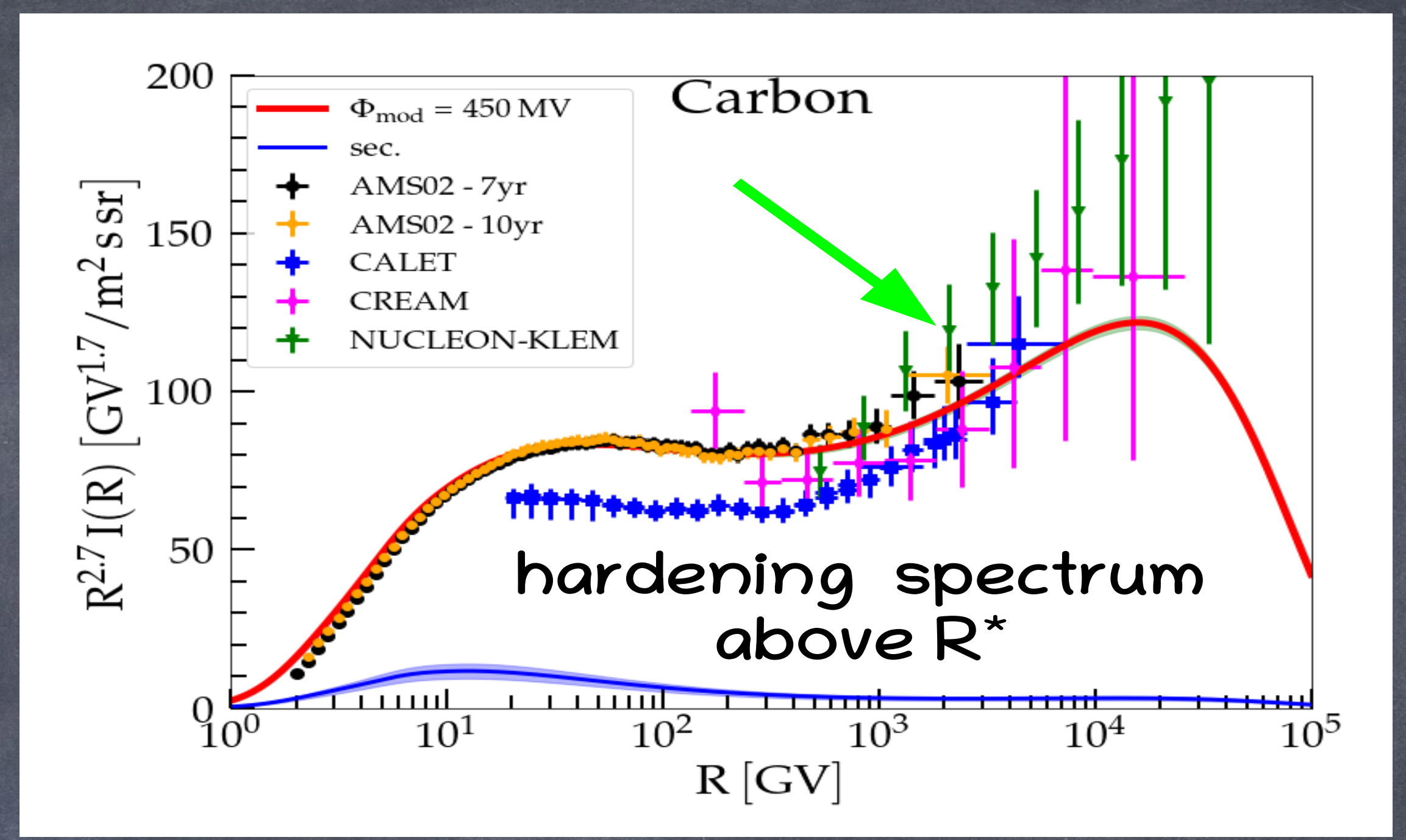
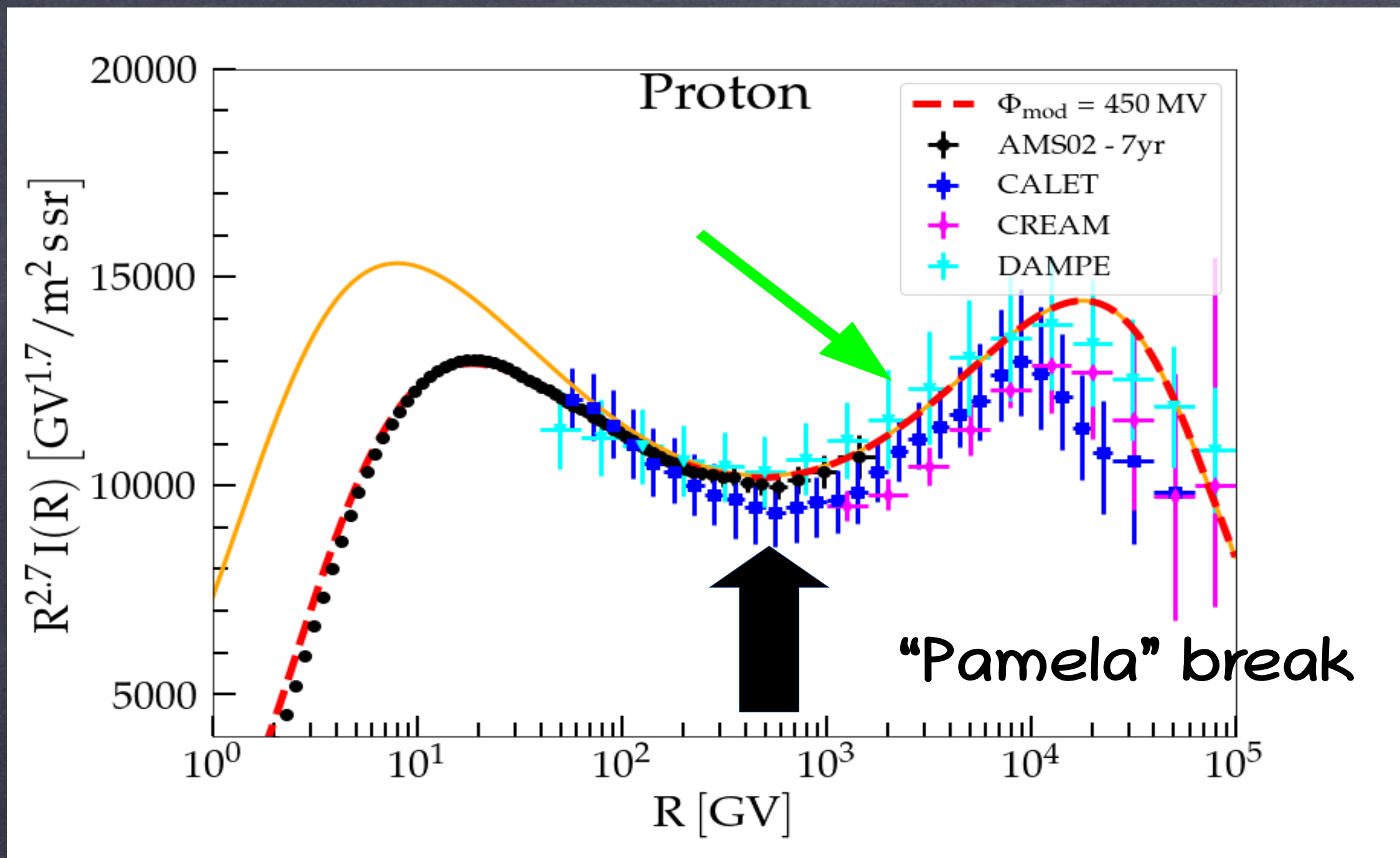
repeated crossings of disk induced by diffusion in halo decreases with E due to $D_H \sim E^{0.7}$

diffusion in disk constant in E

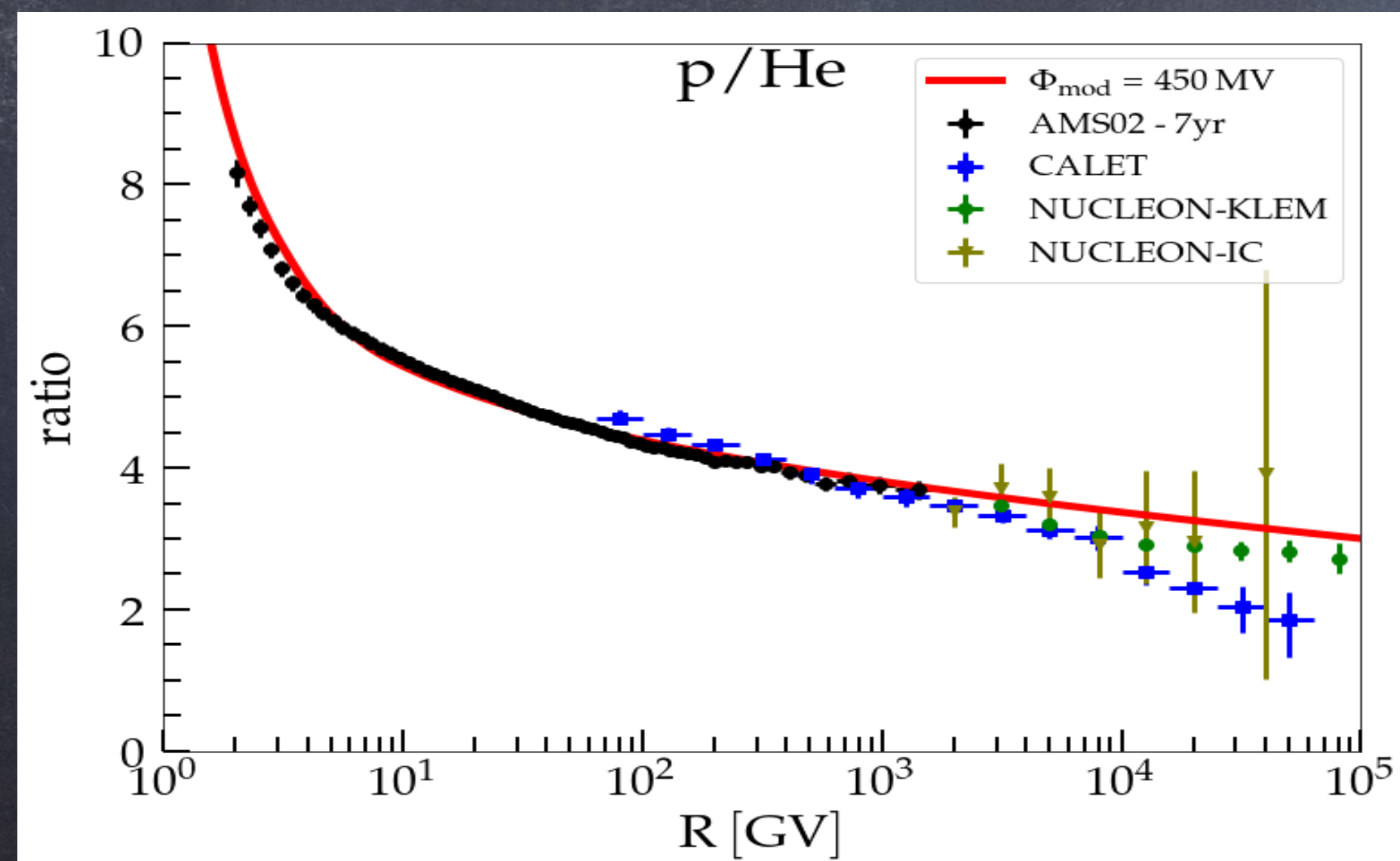
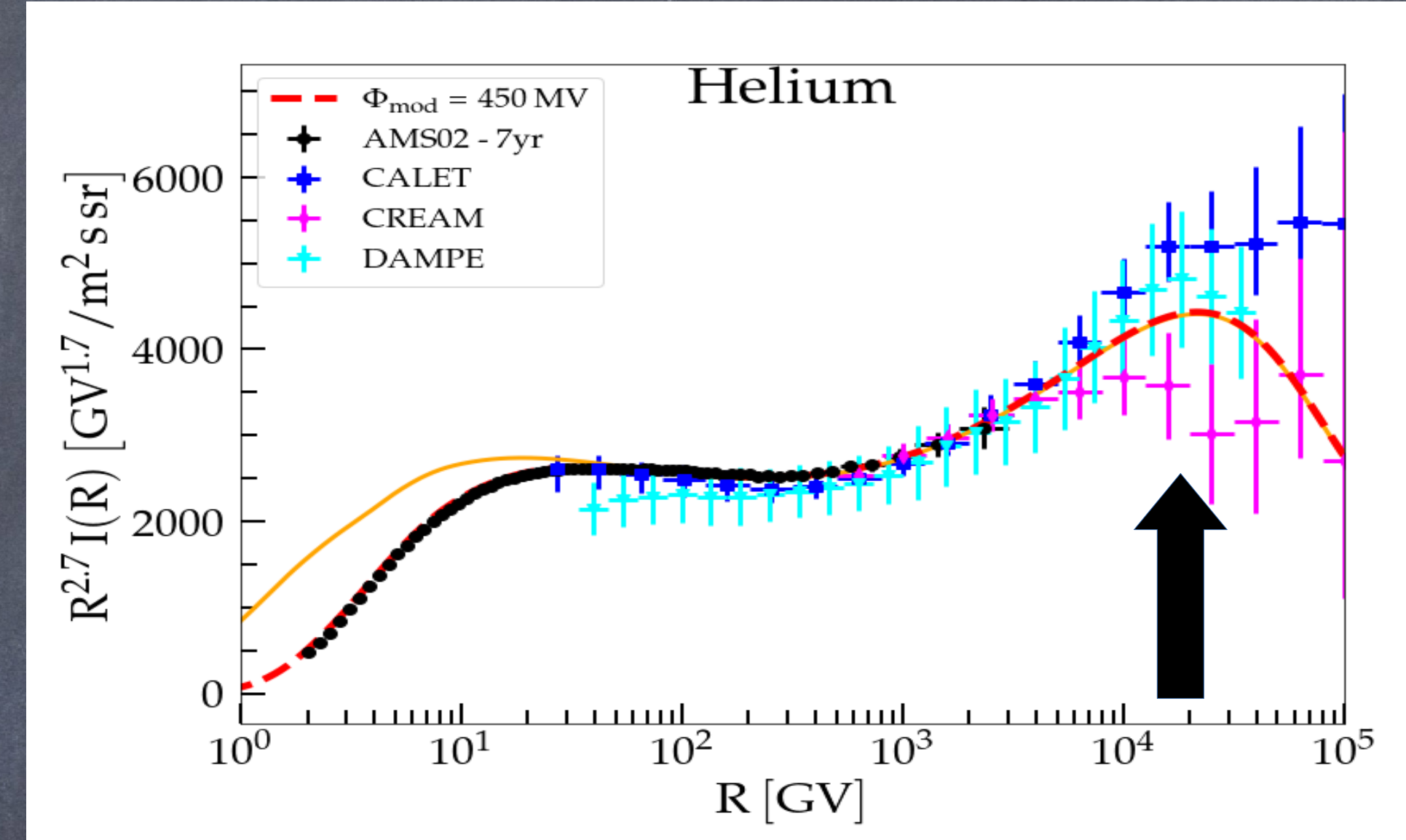
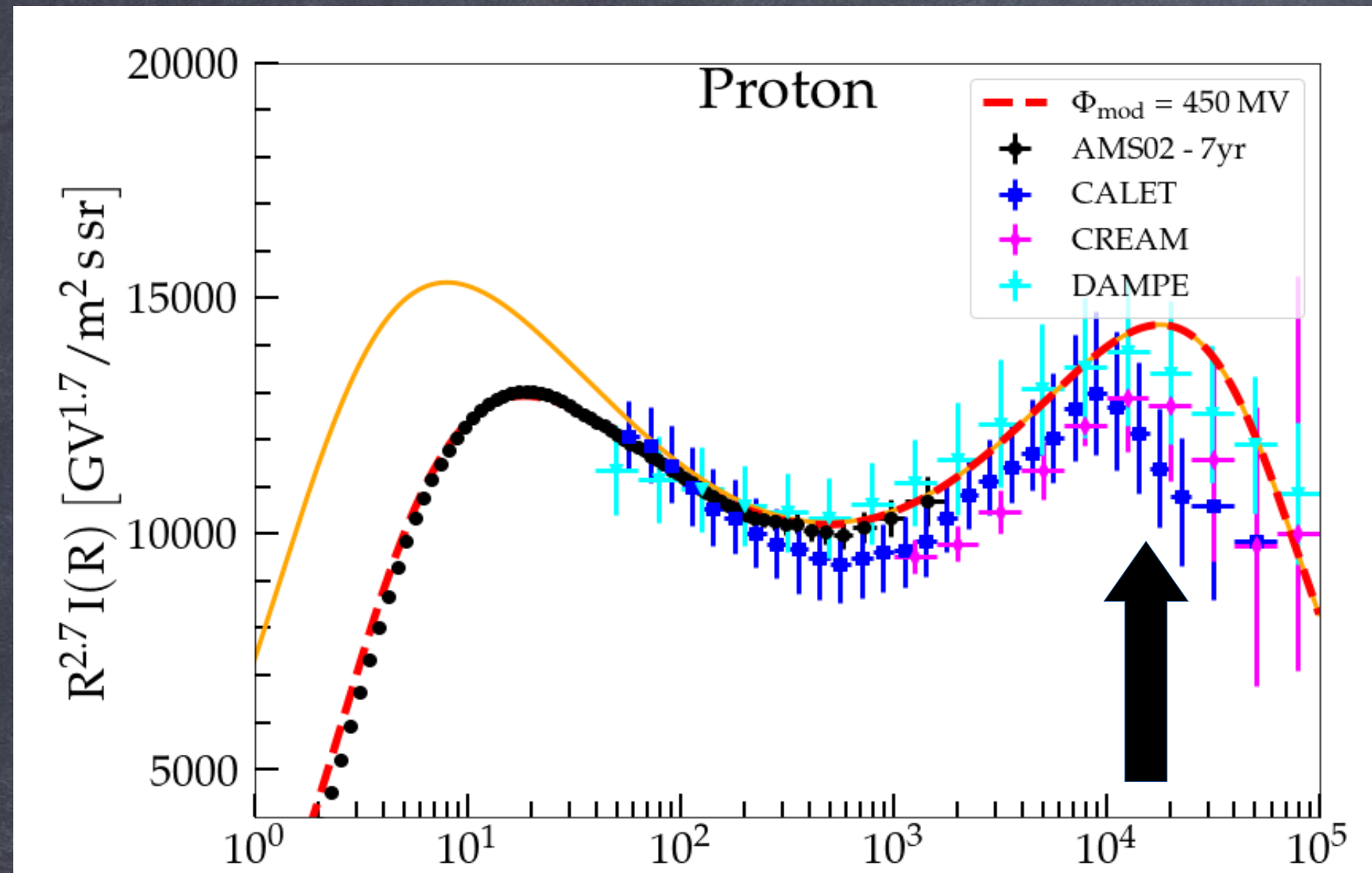
$$\tau_d^{\min} \sim \frac{h^2}{D_{\text{eff},\perp}} \approx 2 \times 10^5 \left(\frac{h}{150 \text{ pc}} \right)^2 \left(\frac{\text{pc}}{D_m} \right) \text{ yr},$$

$$X_{\min} \approx 0.4 n_d \left(\frac{h}{150 \text{ pc}} \right)^2 \left(\frac{\text{pc}}{D_m} \right) \text{ g/cm}^2.$$



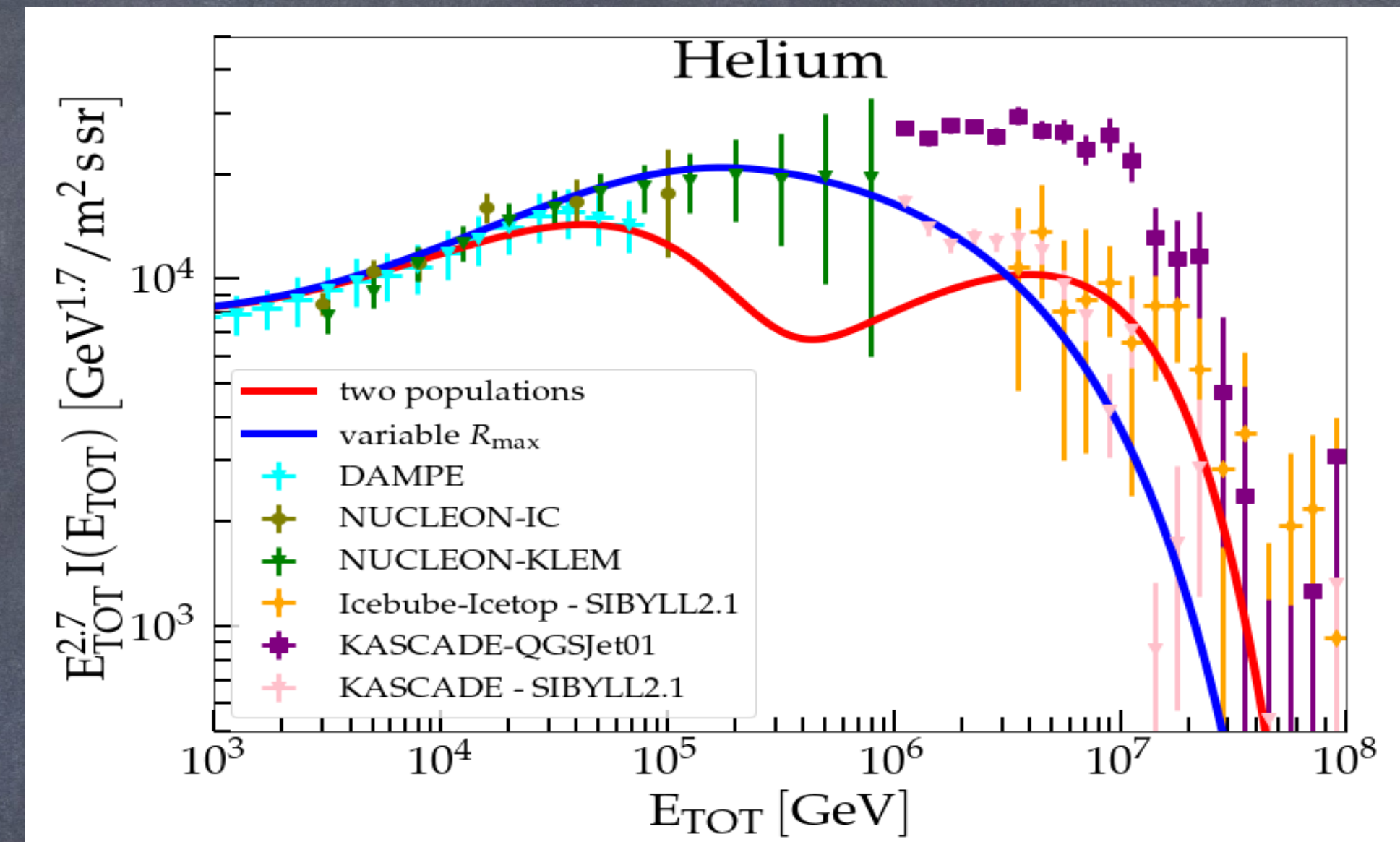
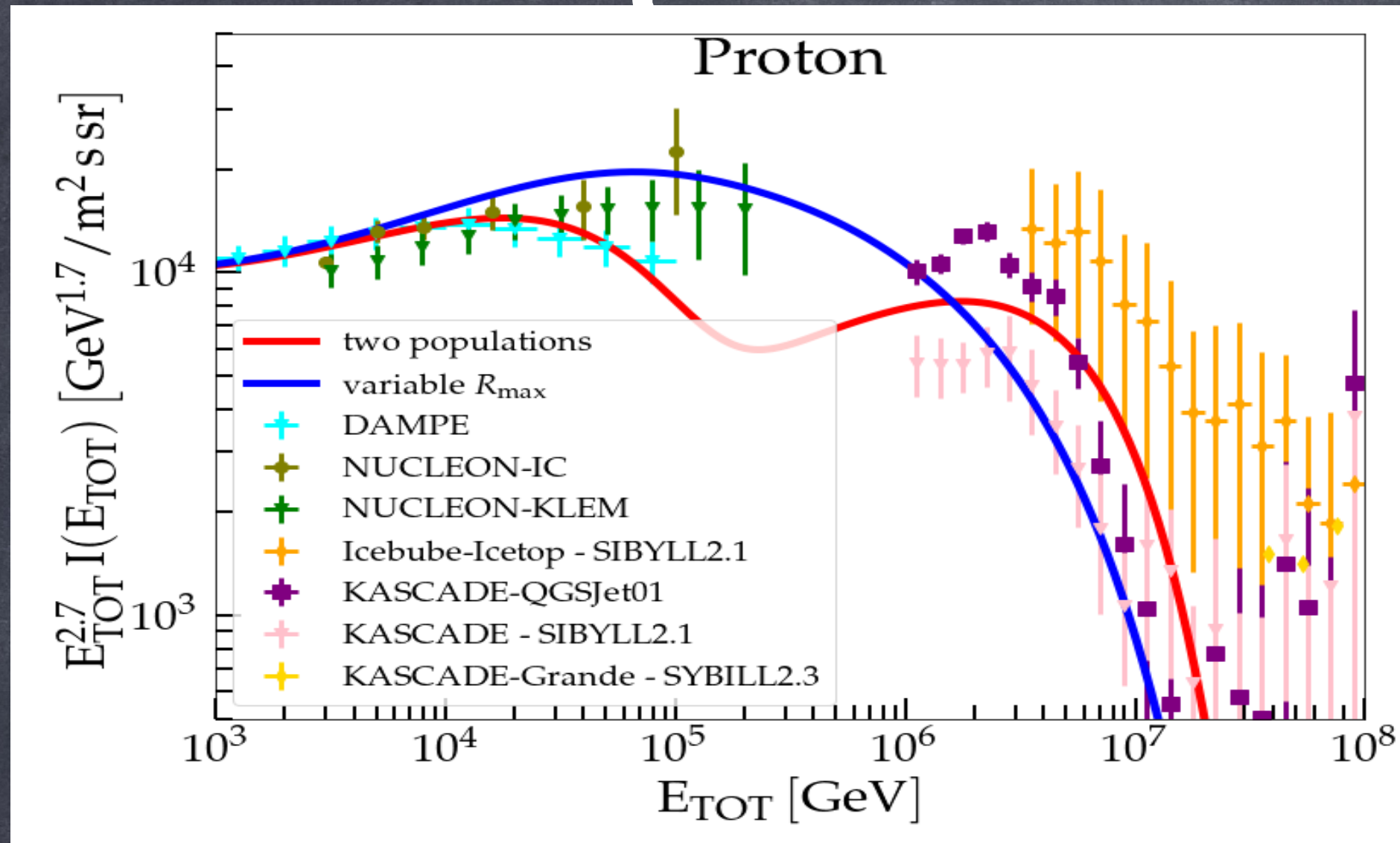


"Dampe" break and the "knee"



gaseous disk				
n_d	f_{He}	h_d	R_d	
1 cm^{-3}	0.1	150 pc	15 kpc	
Galactic disk (GD)				
h	L_c	b^2	D_m	L_{RR}
150 pc	10 pc	0.4	1 pc	50 – 100 pc
Galactic halo (GH)				
H	D_0	δ	u	
4 kpc	$10^{28} \text{ cm}^2/\text{s}$	0.7	40 km/s	
bulk of SNRs				
γ_p	γ_{He}	γ_n	$R_{\text{max}}^{\text{bulk}}$	
4.35	4.30	4.33	50 TV	
PeV sources				
γ_p	γ_{He}	γ_n	$R_{\text{max}}^{\text{PeV}}$	$\epsilon_{\text{bulk}}^{\text{PeV}}$
4.35	4.30	4.33	5 PV	0.15

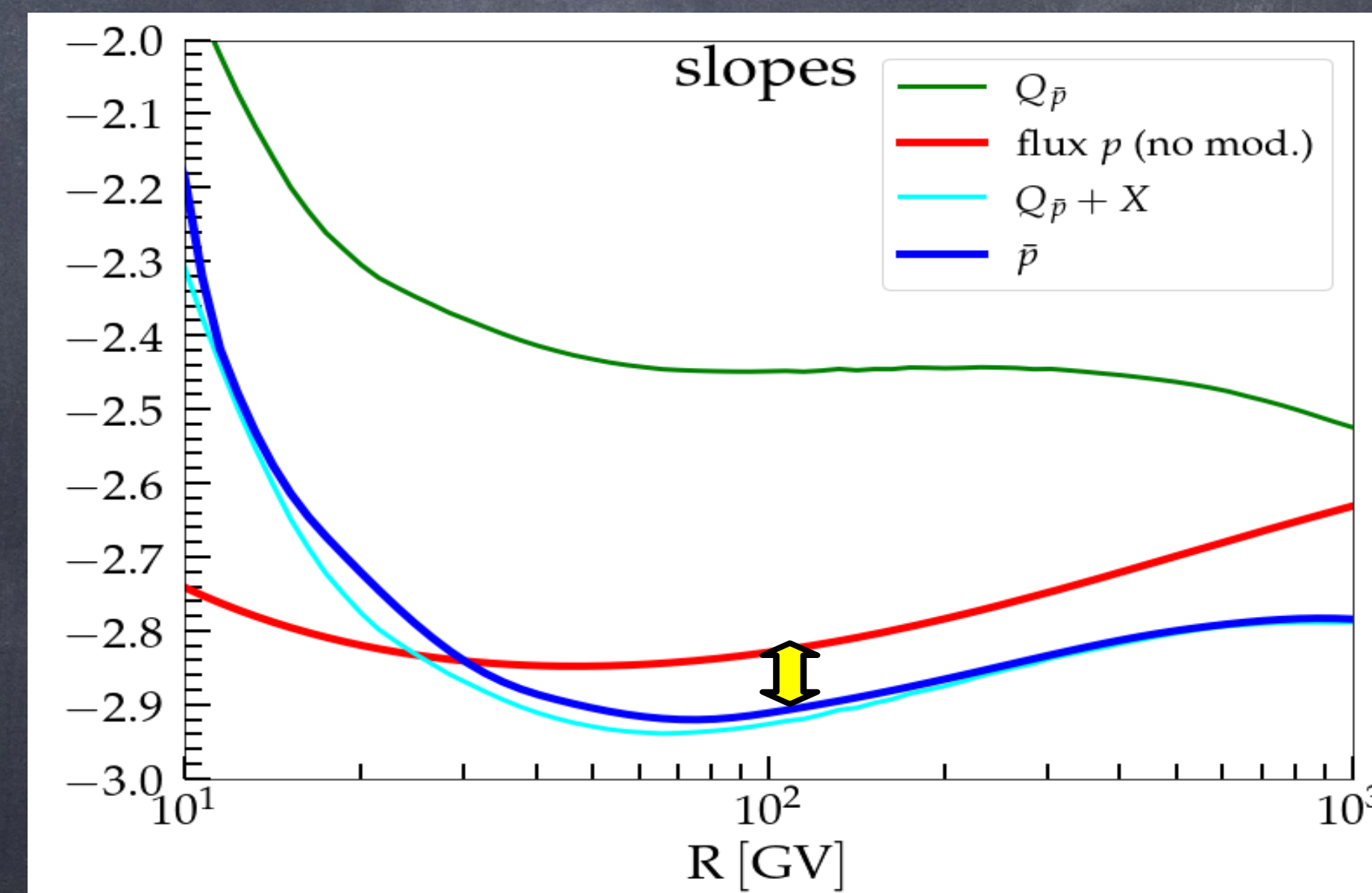
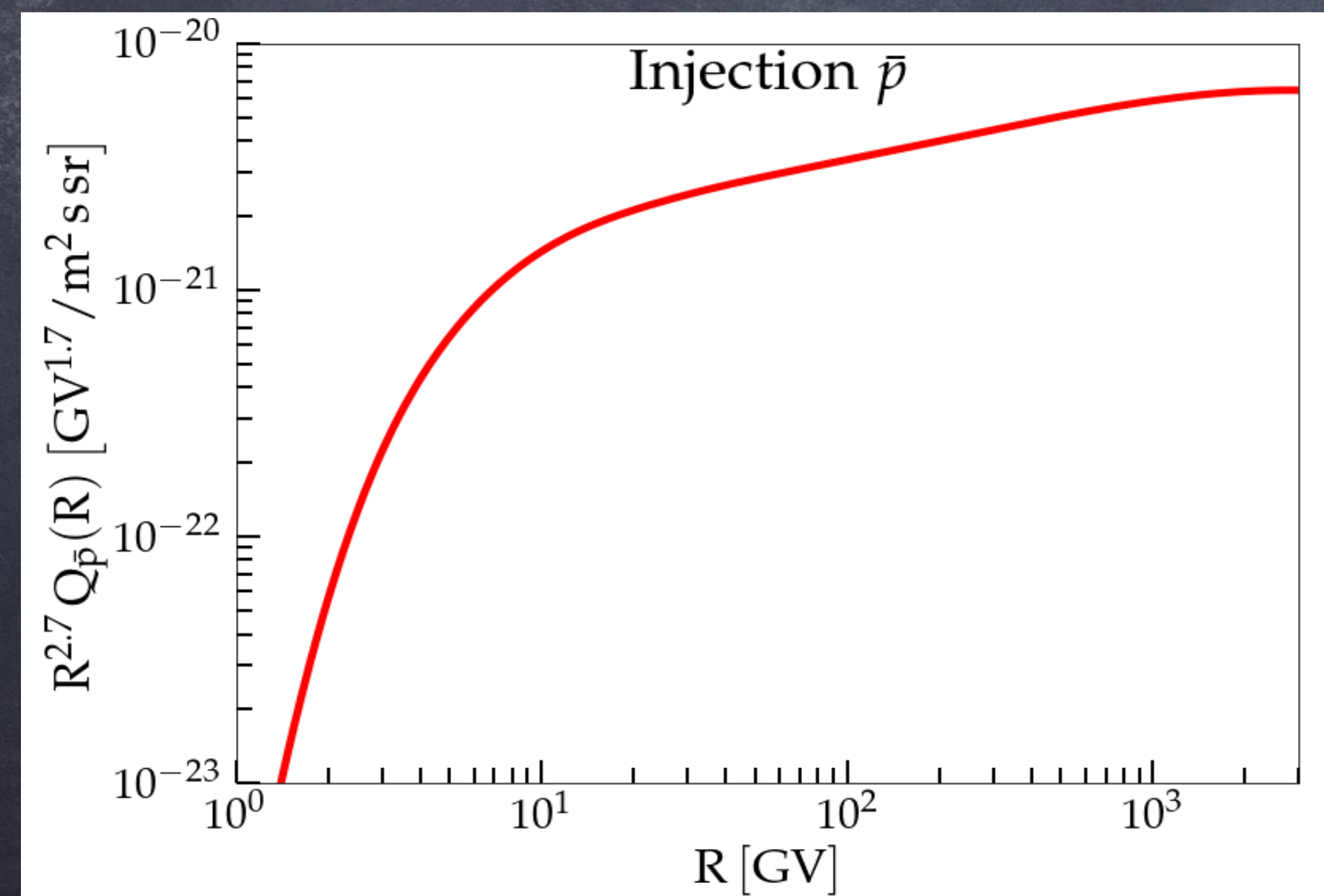
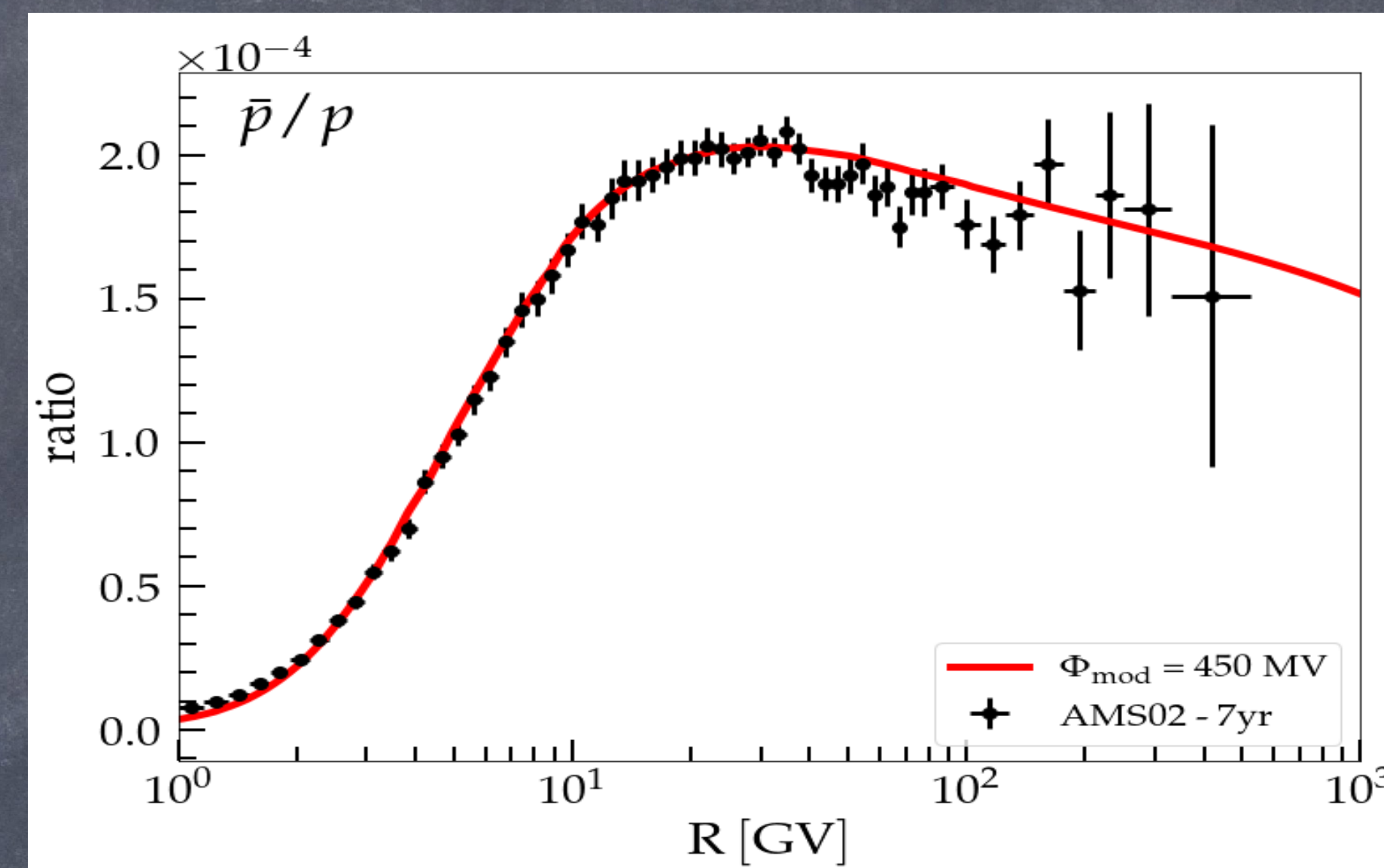
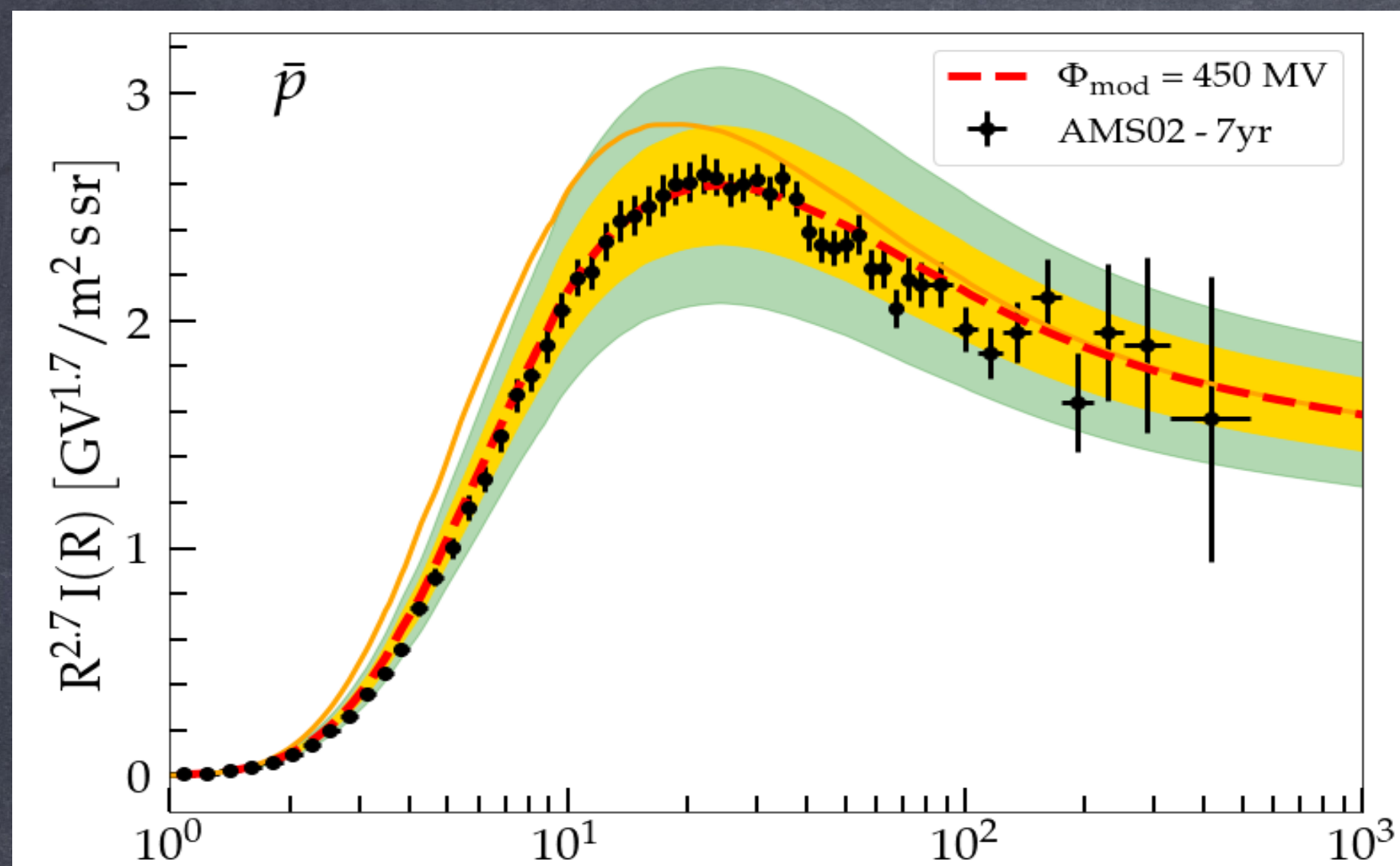
"DAMPE" break and the "knee"



- special SNRs, star clusters
- ...
- ~ 10-20% of typical CR source luminosity
- more in agreement with theory

gaseous disk				
n_d	f_{He}	h_d	R_d	
1 cm^{-3}	0.1	150 pc	15 kpc	
Galactic disk (GD)				
h	L_c	b^2	D_m	L_{RR}
150 pc	10 pc	0.4	1 pc	50 – 100 pc
Galactic halo (GH)				
H	D_0	δ	u	
4 kpc	$10^{28} \text{ cm}^2/\text{s}$	0.7	40 km/s	
bulk of SNRs				
γ_p	γ_{He}	γ_n	$R_{\text{max}}^{\text{bulk}}$	
4.35	4.30	4.33	50 TV	
PeV sources				
γ_p	γ_{He}	γ_n	$R_{\text{max}}^{\text{PeV}}$	$\epsilon_{\text{bulk}}^{\text{PeV}}$
4.35	4.30	4.33	5 PV	0.15

Antiprotons



summary & caveats/perspectives

- in Galactic disk weak scattering + field lines along GP
 - ▶ can lead to energy-independent diffusion perp. to GP
 - ▶ effect appears at $R \gtrsim TV$
- E_{\max} of bulk SNRs \sim to $50 TV$ only a fraction of sources reach
- possible to explain features in CR spectra in GV-PV range
 - ▶ without breaks in injection or propagation
 - ▶ physically motivated scenario
(but need cross-check with dedicated theory/simulations)

summary & caveats/perspectives

Caveats...

- ▶ nuclei data at multi-TV have large uncertainties
- ▶ uncertainties in spallation cross-section and chains
- ▶ need for better understanding of turbulence/propagation
- ▶ acceleration and PeVatrons?
- ▶ include source grammage? Check leptons...

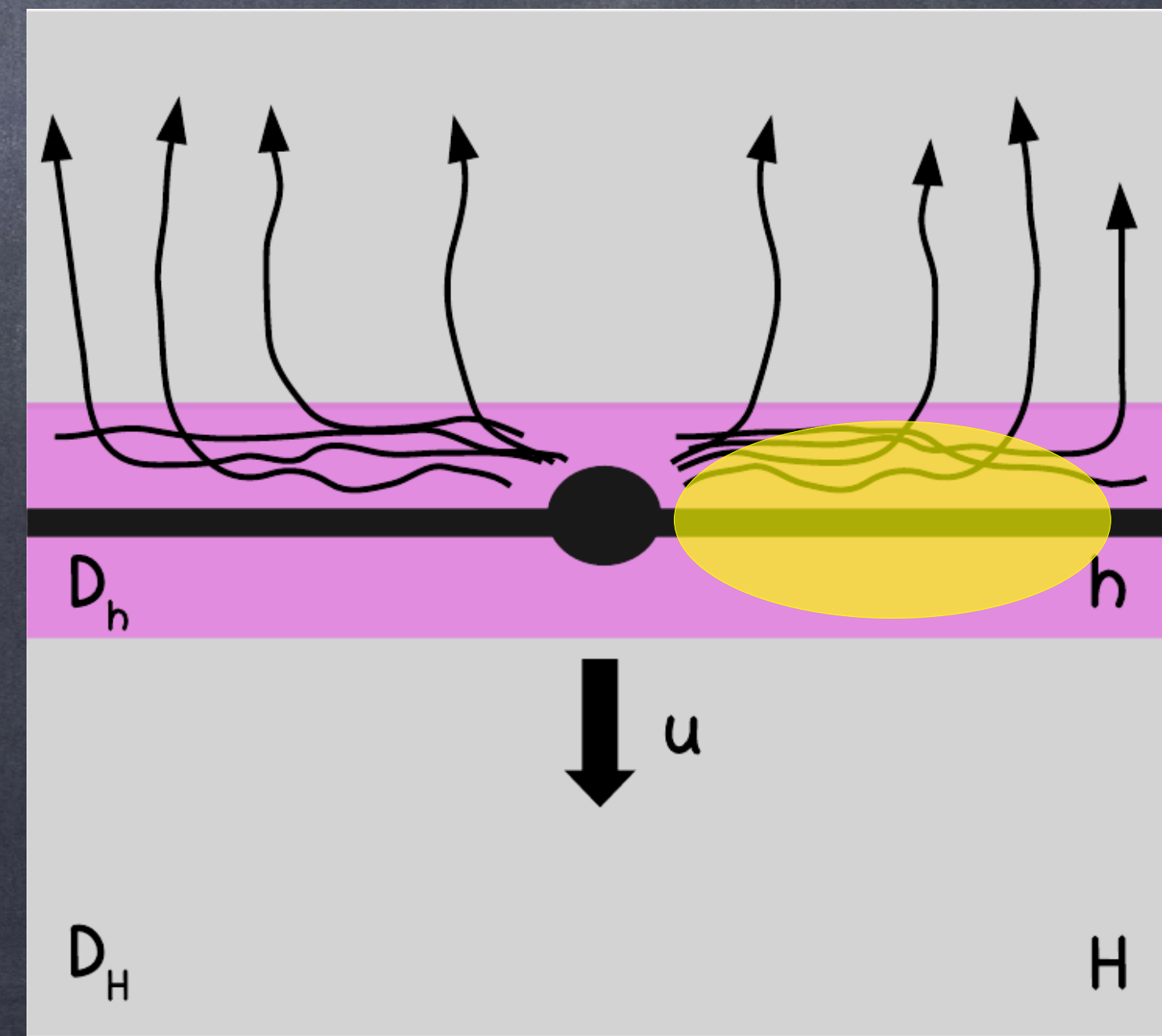
Anisotropy...

$$d_{\parallel} \sim D_{\parallel}/D_{\perp} h \approx 1 - 2 \text{ kpc}$$

average number of contributing sources at VHE

$$\langle N_{\text{PV}} \rangle \approx 10 \left(\frac{\xi_{\text{PV}}}{0.15} \right) \left(\frac{v_{\text{SNe}}}{1/30 \text{ yr}} \right) \left(\frac{h}{150 \text{ pc}} \right)^2 \left(\frac{\text{pc}}{D_m} \right) \left(\frac{d}{\text{kpc}} \right)^2,$$

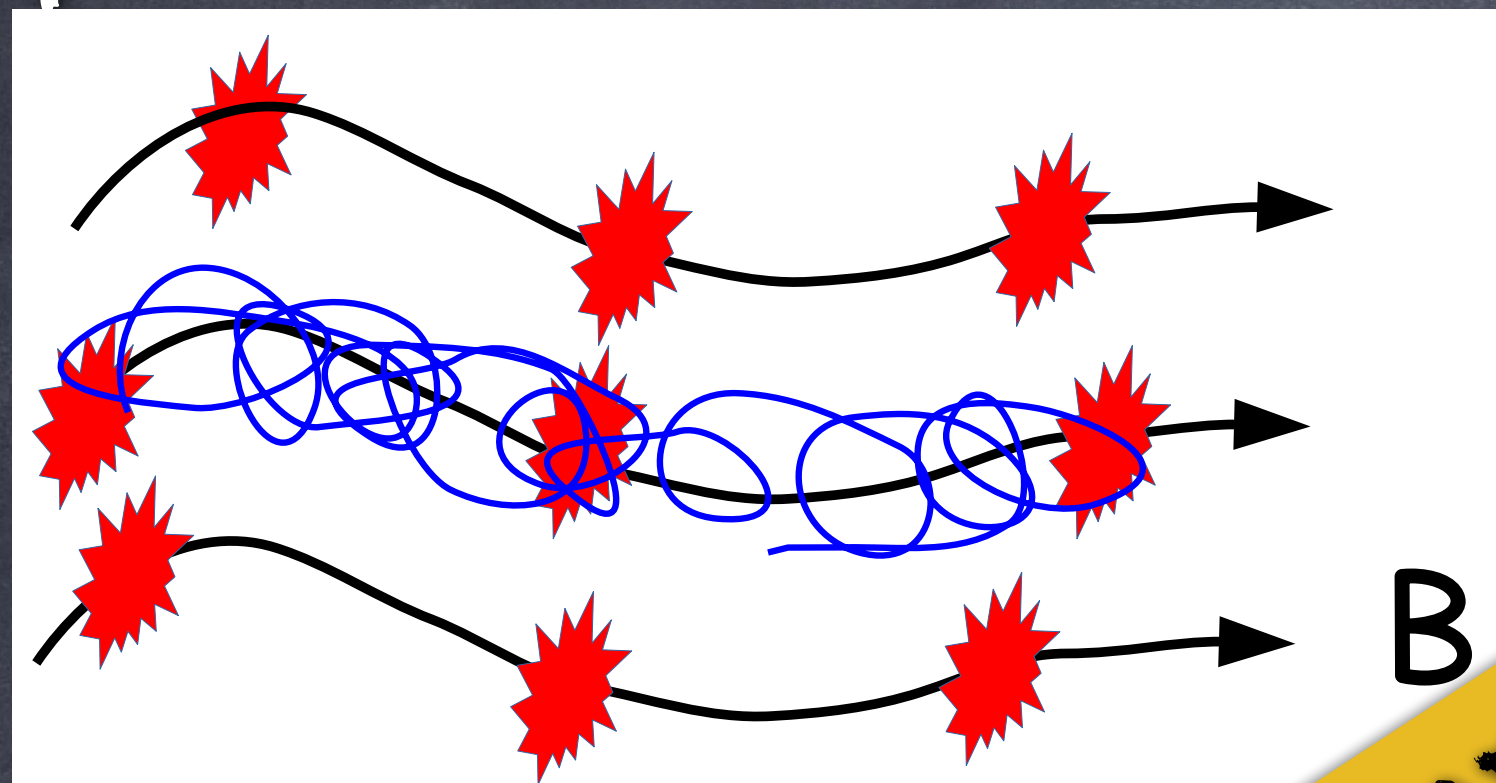
crucial test



Thank You

Parallel CR transport

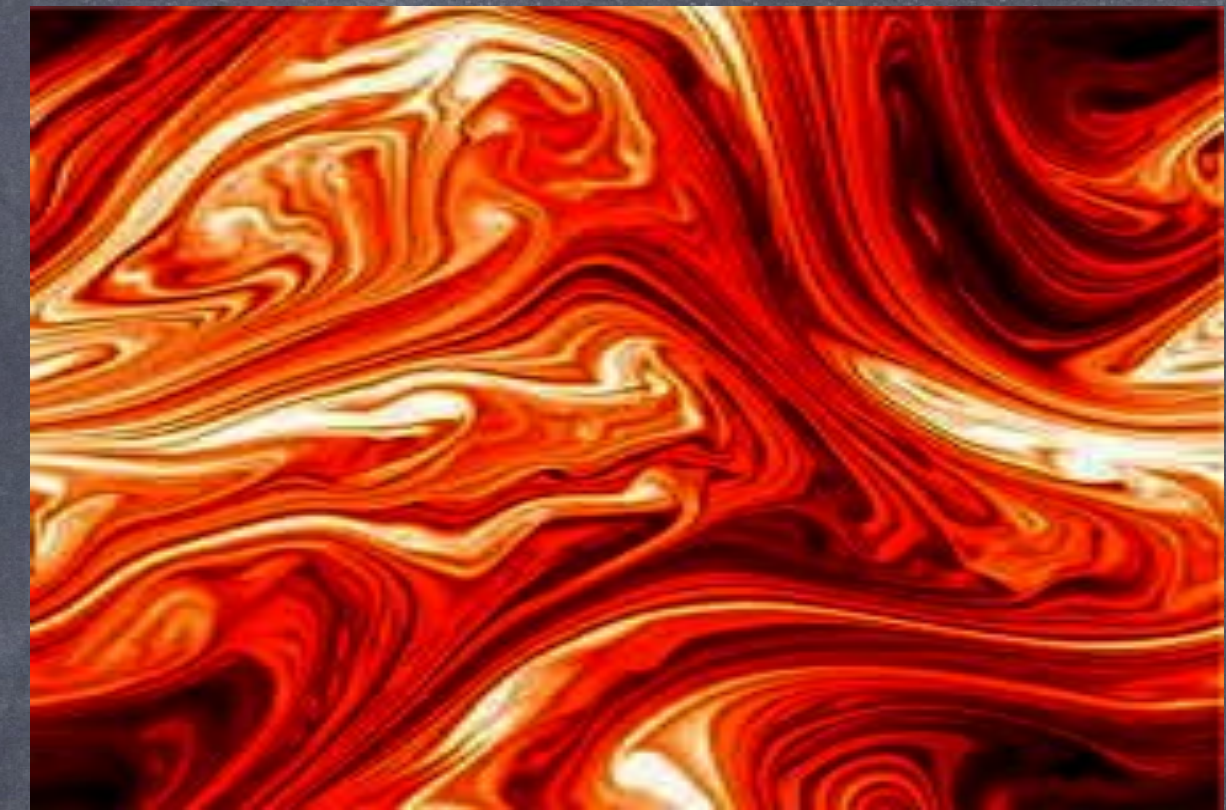
parallel diffusion



(parallel) diffusion coefficient

$$D_{\parallel}(E) \propto \lambda_{\text{mfp}} \propto E^{\delta}$$

MHD turbulence



- CR gyromotion
- scattering off waves
- mean-free path λ_{mfp}
- $k \sim 1/r_L$ (resonance)

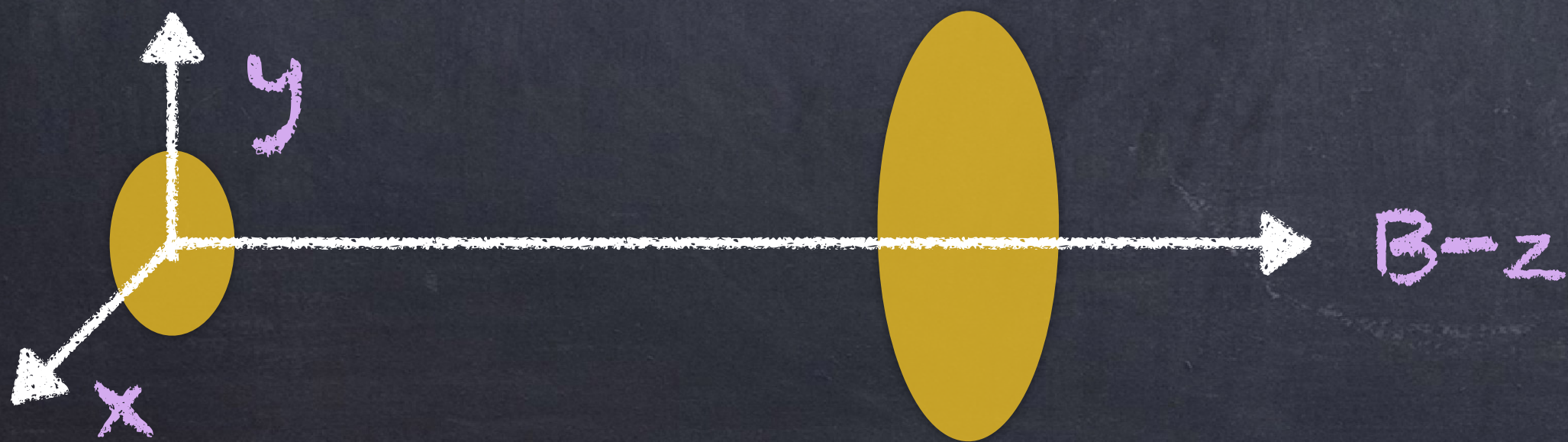
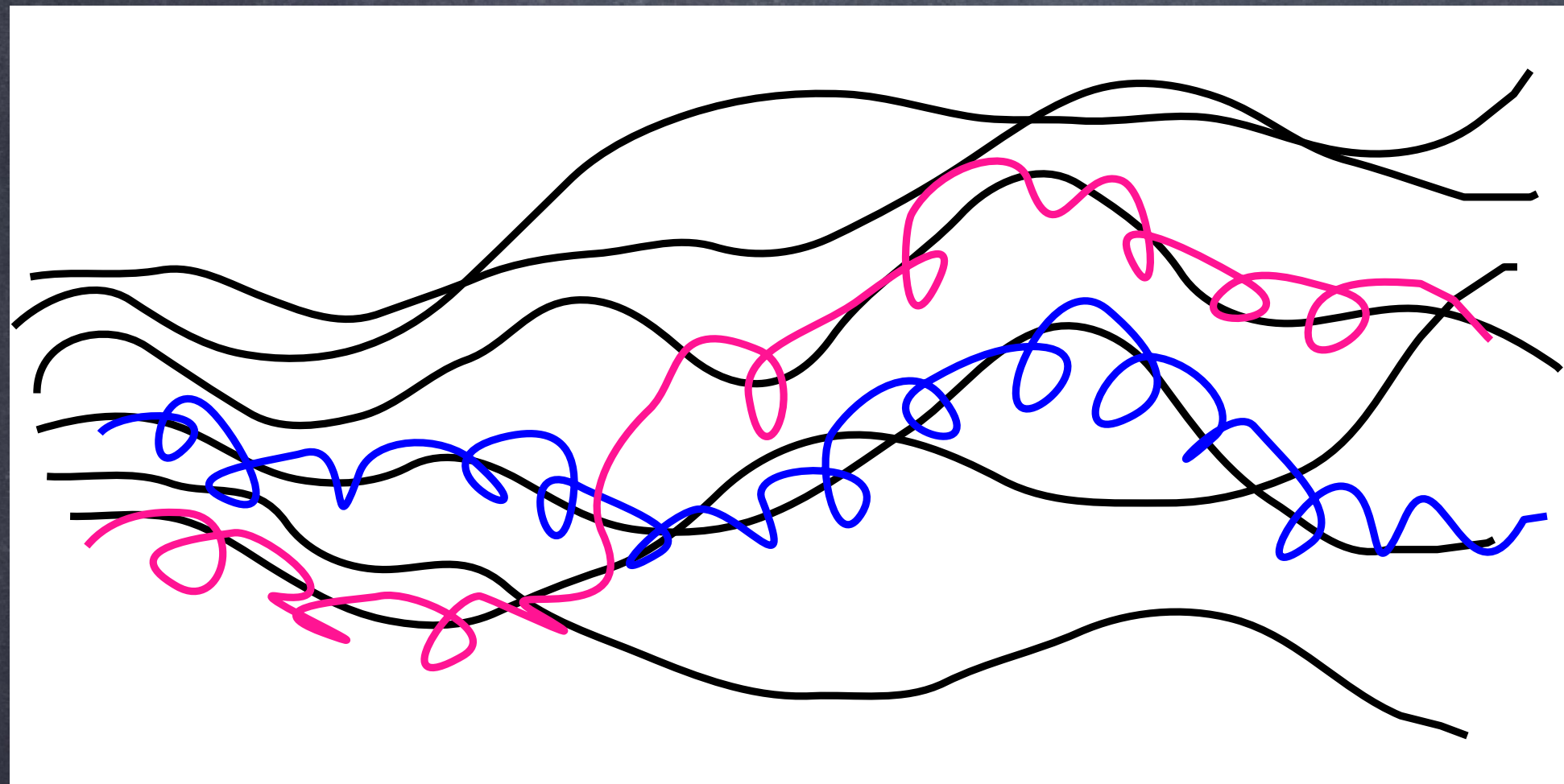
- source injection (10s pc)
- cascade to $k \sim 1/r_L$?
- damping?

Mertsch (2020) - review turbulence & transport

Perpendicular CR transport

Shalchi (2020) - review perp. Transport

perpendicular diffusion



- field line random walk (FLRW)
 - ▶ turbulent motion of field lines
 - ▶ large-scale ($\gg r_L$) turbulence

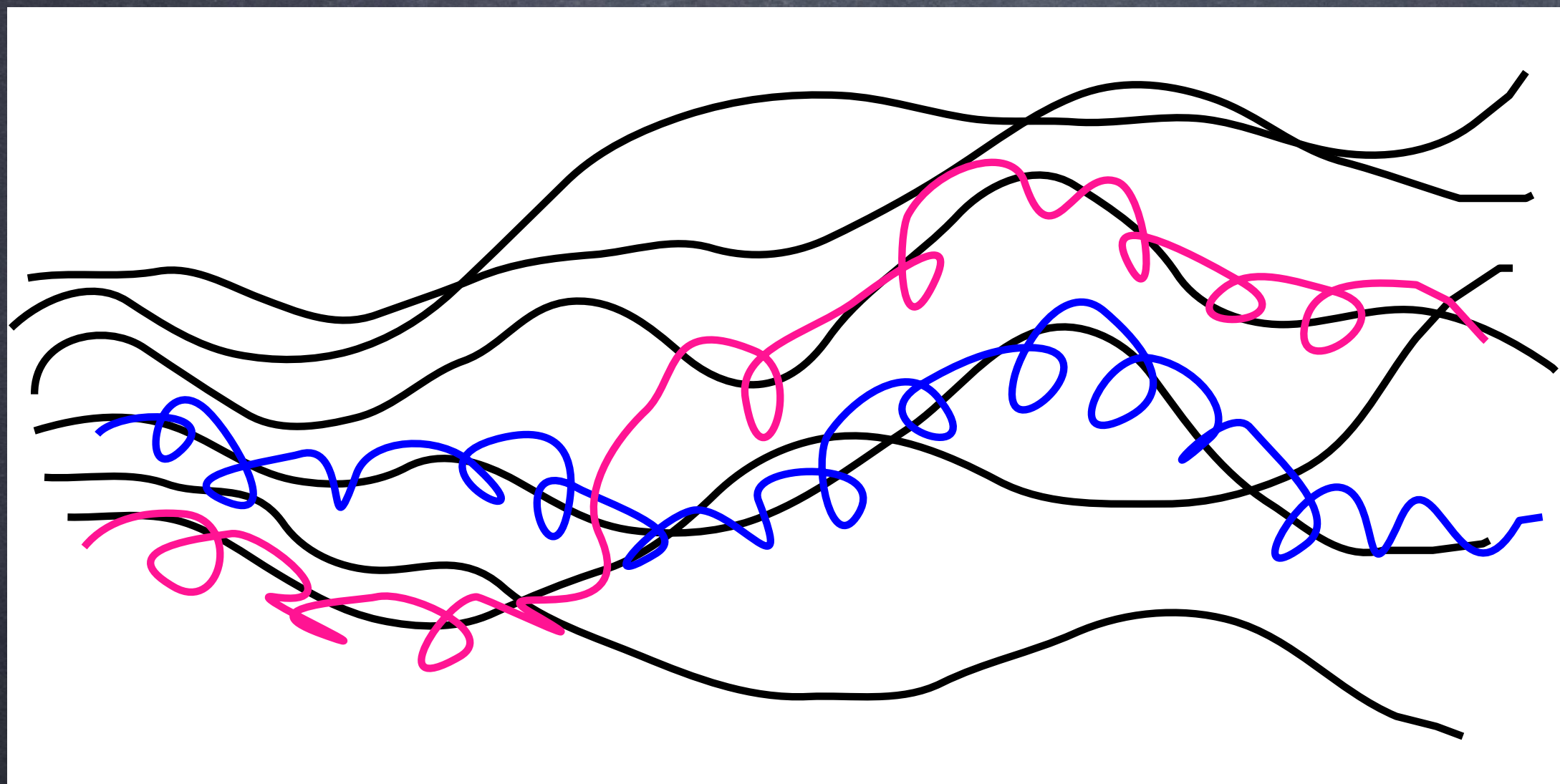
$$\langle (x - x_0)^2 \rangle = \langle (y - y_0)^2 \rangle = 2D_m z.$$

$$D_m = \left(\frac{\delta B}{B_0} \right)^2 \frac{L_c}{4} = 0.25 \left(\frac{b^2}{0.1} \right) \left(\frac{L_c}{10 \text{ pc}} \right) \text{ pc},$$

Perpendicular CR transport

Shalchi (2020) - review perp. Transport

perpendicular diffusion



- field line walk (FLRW)
 - ▶ turbulent motion of field lines
 - ▶ large-scale ($\gg r_L$) turbulence
- Small-scale perp. diffusion
 - ▶ CRs jump between field lines
 - ▶ scattering, drifts...

→ LARGE-SCALE PERPENDICULAR DIFFUSION

$$D_{\perp}(E) \lesssim D_{\parallel}(E)$$

Perp. diffusion: weak scattering limit

Rechester & Rosenbluth 1978

Chandran 2000

Snodin et al. (2022)

Pezzi & Blasi (2024)

weak scattering ALONG field lines + FLRW

▶ $\lambda_{\text{mfp}} \gtrsim L_{\text{RR}}$

$$\langle (x - x_0)^2 \rangle = \langle (y - y_0)^2 \rangle = 2D_m z.$$

▶ $L_{\text{RR}} \gtrsim L_{\text{coh}} \rightarrow$ trajectory decorrelates from initial field line


▶ L_{RR} statistically independent random step

▶ within L_{coh} , $z(t) \sim vt$

$$\begin{cases} (\Delta R)^2 = 2D_m L_{\text{RR}} \\ \Delta t = \frac{L_{\text{RR}}}{v} \end{cases}$$

perpendicular diffusion becomes energy-independent

▶ $D_{\perp} = \frac{1}{2} \frac{(\Delta R)^2}{\Delta t}$


$$D_m v \approx 3 \times 10^{28} \left(\frac{D_m}{\text{pc}} \right) \text{cm}^2/\text{s},$$

▶ (ΔR) rms perp. displacement during each random step L_{RR}

