

# Estimation of neutron star mass and radius from the high-frequency QPOs in GRB 200415A

Hajime SOTANI (RIKEN)

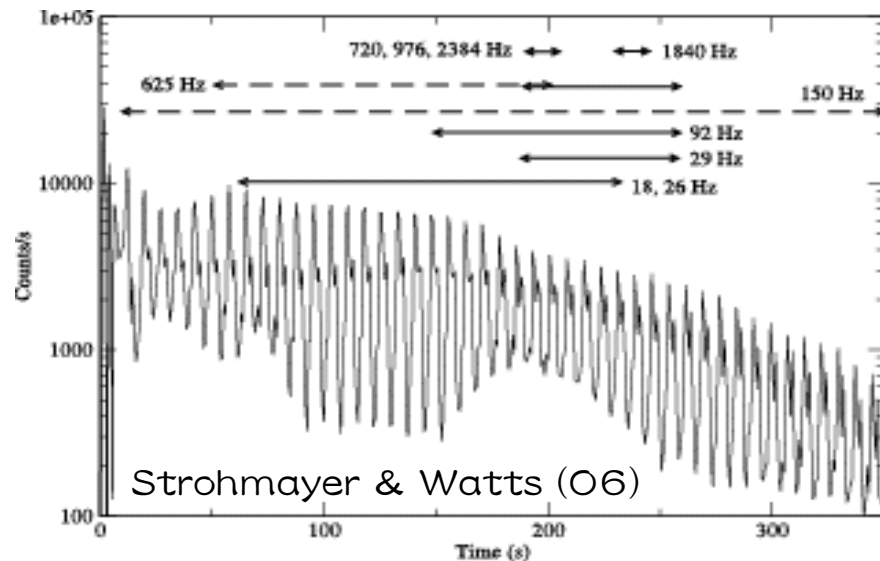
collaborate with

K. D. Kokkotas (Tuebingen), N. Stergioulas (Thessaloniki)

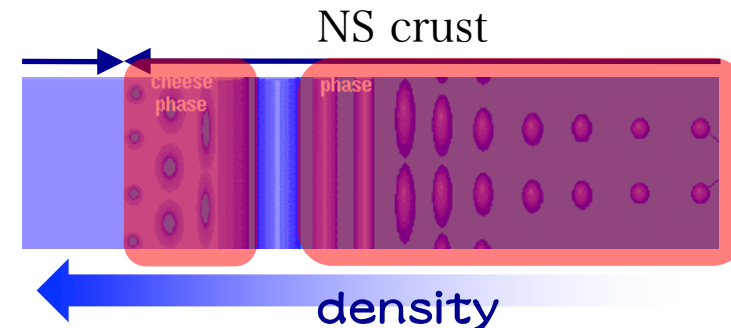
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# Magnetar QPOs & crust oscillations

- Quasi-periodic oscillations (QPOs) in afterglow of giant flares from soft-gamma repeaters (SGRs) (Barat+83, Israel+05, Strohmayer & Watts 05, Watts & Strohmayer 06)
  - SGR 0526-66 (5<sup>th</sup>/3/1979) : 43 Hz
  - SGR 1900+14 (27<sup>th</sup>/8/1998) : 28, 54, 84, 155 Hz
  - SGR 1806-20 (27<sup>th</sup>/12/2004) : 18, 26, 30, 92.5, 150, 626.5, 1837 Hz
    - additional QPO in SGR 1806-20 : 57 Hz (Huppenkothen+14)
    - additional QPOs : 51.4, 97.3, 157 Hz (Miller+18)



- Crustal torsional oscillation ?
- Magnetic oscillations ?

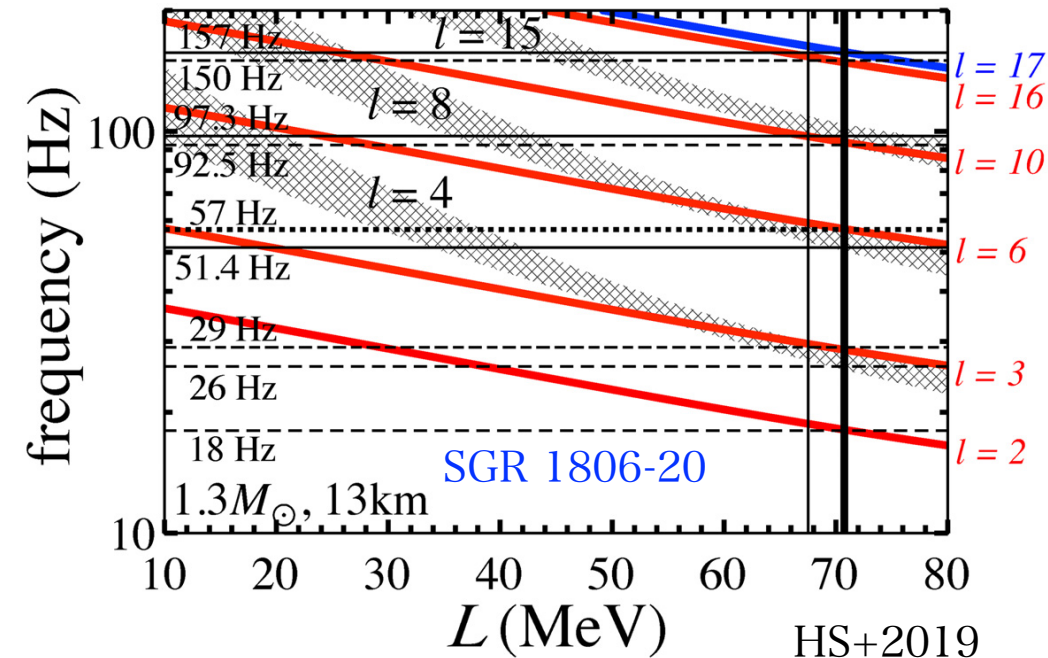
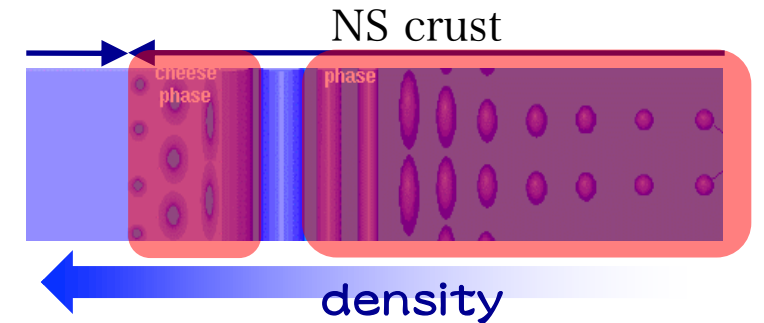


# Constraint on L from magnetar QPOs

- nuclear saturation parameters

$$w = w_0 + \frac{K_0}{18n_0^2} (n_b - n_0)^2 + \left[ S_0 + \frac{L}{3n_0} (n_b - n_0) \right] \alpha^2$$

- Constraint on  $K_0$ :  $K_0 = 240 \pm 20 \text{ MeV}$  (Shlomo+2006)
- Constraint on L
  - $L = 60 \pm 20 \text{ MeV}$ : fiducial value (Li+2019)
  - $L = 58 - 73 \text{ MeV}$ : constraint from QPOs (HS+2019)



# QPOs are newly found

## Article

### Very-high-frequency oscillations in the main peak of a magnetar giant flare

<https://doi.org/10.1038/s41586-021-04101-1>

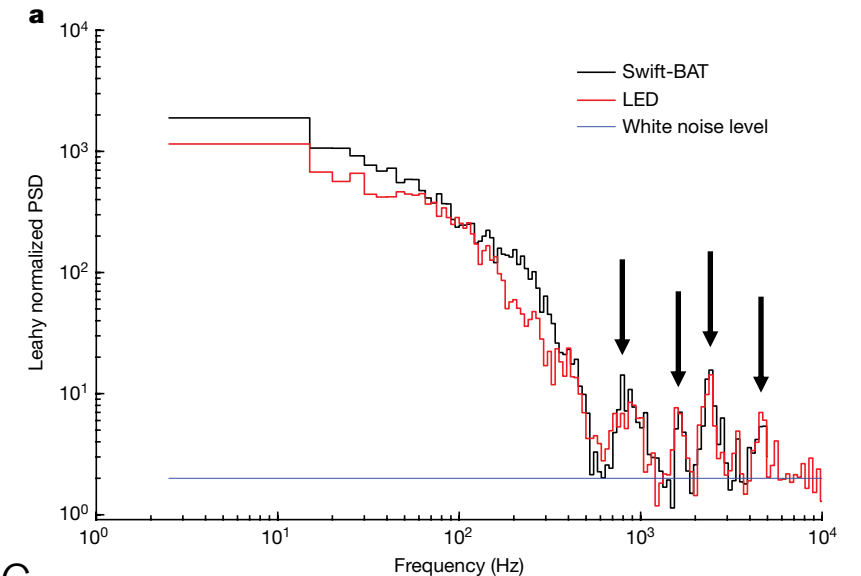
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A. J. Castro-Tirado<sup>1,2</sup>, N. Østgaard<sup>3</sup>, E. Göğüş<sup>4</sup>, C. Sánchez-Gil<sup>5</sup>, J. Pascual-Granado<sup>1</sup>, V. Reglero<sup>6,7</sup>, A. Mezentsev<sup>3</sup>, M. Gabler<sup>6</sup>, M. Marisaldi<sup>3,8</sup>, T. Neubert<sup>9</sup>, C. Budtz-Jørgensen<sup>9</sup>, A. Lindanger<sup>3</sup>, D. Sarría<sup>3</sup>, I. Kuvvetli<sup>9</sup>, P. Cerdá-Durán<sup>6</sup>, J. Navarro-González<sup>7</sup>, J. A. Font<sup>6,10</sup>, B.-B. Zhang<sup>11,12,13</sup>, N. Lund<sup>9</sup>, C. A. Oxborrow<sup>9</sup>, S. Brandt<sup>9</sup>, M. D. Caballero-García<sup>1</sup>, I. M. Carrasco-García<sup>14</sup>, A. Castellón<sup>2,15</sup>, M. A. Castro Tirado<sup>1,16</sup>, F. Christiansen<sup>9</sup>, C. J. Eyles<sup>7</sup>, E. Fernández-García<sup>1</sup>, G. Genov<sup>3</sup>, S. Guziy<sup>17,18</sup>, Y.-D. Hu<sup>1,19</sup>, A. Nicuesa Guelbenzu<sup>20</sup>, S. B. Pandey<sup>21</sup>, Z.-K. Peng<sup>11,12</sup>, C. Pérez del Pulgar<sup>2</sup>, A. J. Reina Terol<sup>2</sup>, E. Rodríguez<sup>1</sup>, R. Sánchez-Ramírez<sup>22</sup>, T. Sun<sup>1,23,24</sup>, K. Ullaland<sup>3</sup> & S. Yang<sup>3</sup>

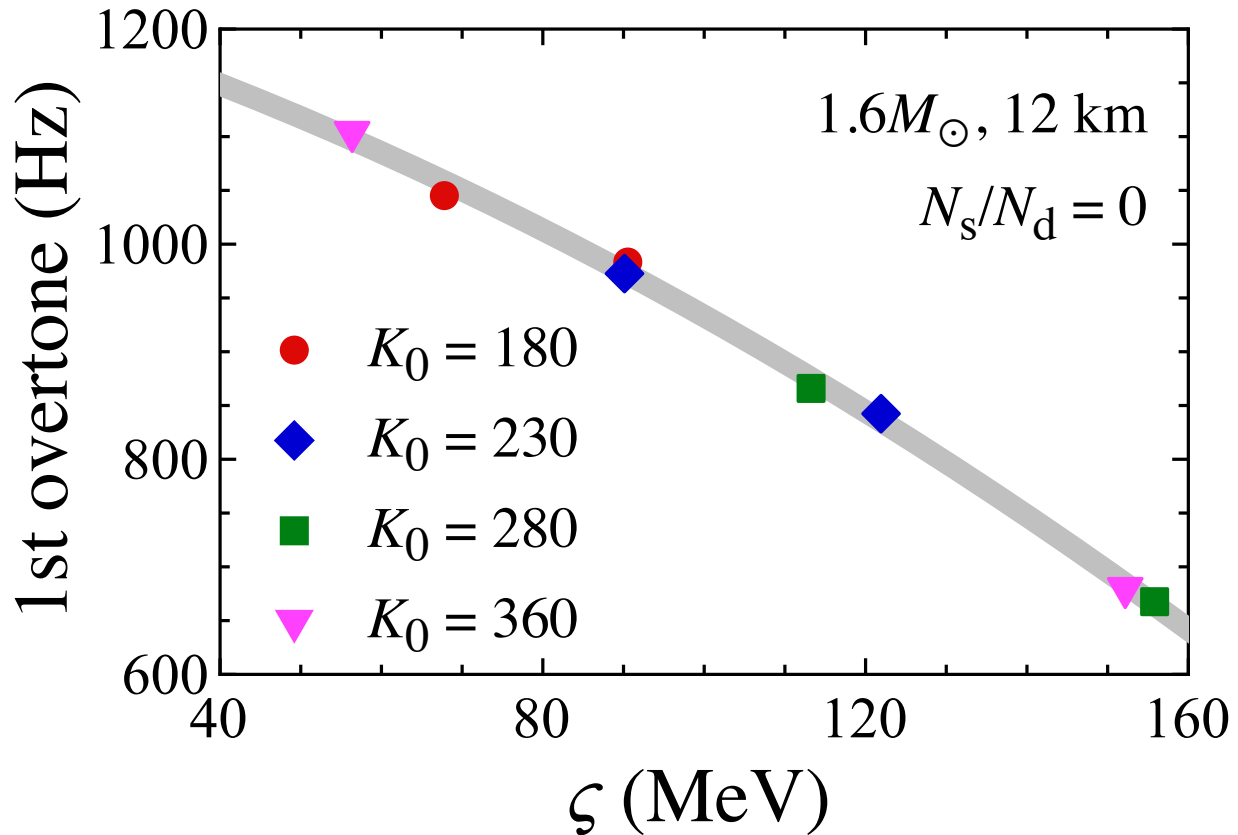


giant gamma-ray flare (GRB 200415A) in the direction of the NGC 253 galaxy, disappearing after 3.5 msec, on 15/4/2020.

Interval (Hz)	LED		HED	
	Peak Frequency (Hz)	Chance probability	Peak Frequency (Hz)	Chance probability
500 - 1100	835.9 <sup>-84.7</sup> <sub>+77.3</sub>	1.2 x 10 <sup>-4</sup>	-	-
1100 - 1700	1443.7 <sup>-68.7</sup> <sub>+74.8</sub> <sup>a</sup>	4.9 x 10 <sup>-2</sup>	1353.5 <sup>-230.7</sup> <sub>+217.7</sub>	1.2 x 10 <sup>-12</sup>
1800 - 2400	2131.7 <sup>-151.0</sup> <sub>+148.2</sub>	2.4 x 10 <sup>-9</sup>	2095.1 <sup>-277.5</sup> <sub>+180.8</sub>	5.0 x 10 <sup>-8</sup>
3900 - 4500	4249.7 <sup>-102.7</sup> <sub>+116.0</sub>	1.7 x 10 <sup>-4</sup>	4126.8 <sup>-71.1</sup> <sub>+73.0</sub>	1.1 x 10 <sup>-2</sup>

Observed frequencies are high  
 - polar type oscillations, such as f, p<sub>i</sub>-modes  
 - **overtones of torsional oscillations**

# 1<sup>st</sup> overtone



- two parameters in EOS, two in NS models
- overtones depend on  $K_0$  &  $L$ 
  - $f \sim v_s / \Delta R$  (Hansen & Cioffi 80)
  - $\Delta R$  depends on  $K_0$  &  $L$  (HS+17)
- as in Sotani+ 19, frequencies can be well characterized by

$$\varsigma = (K_0^4 L^5)^{1/9}$$

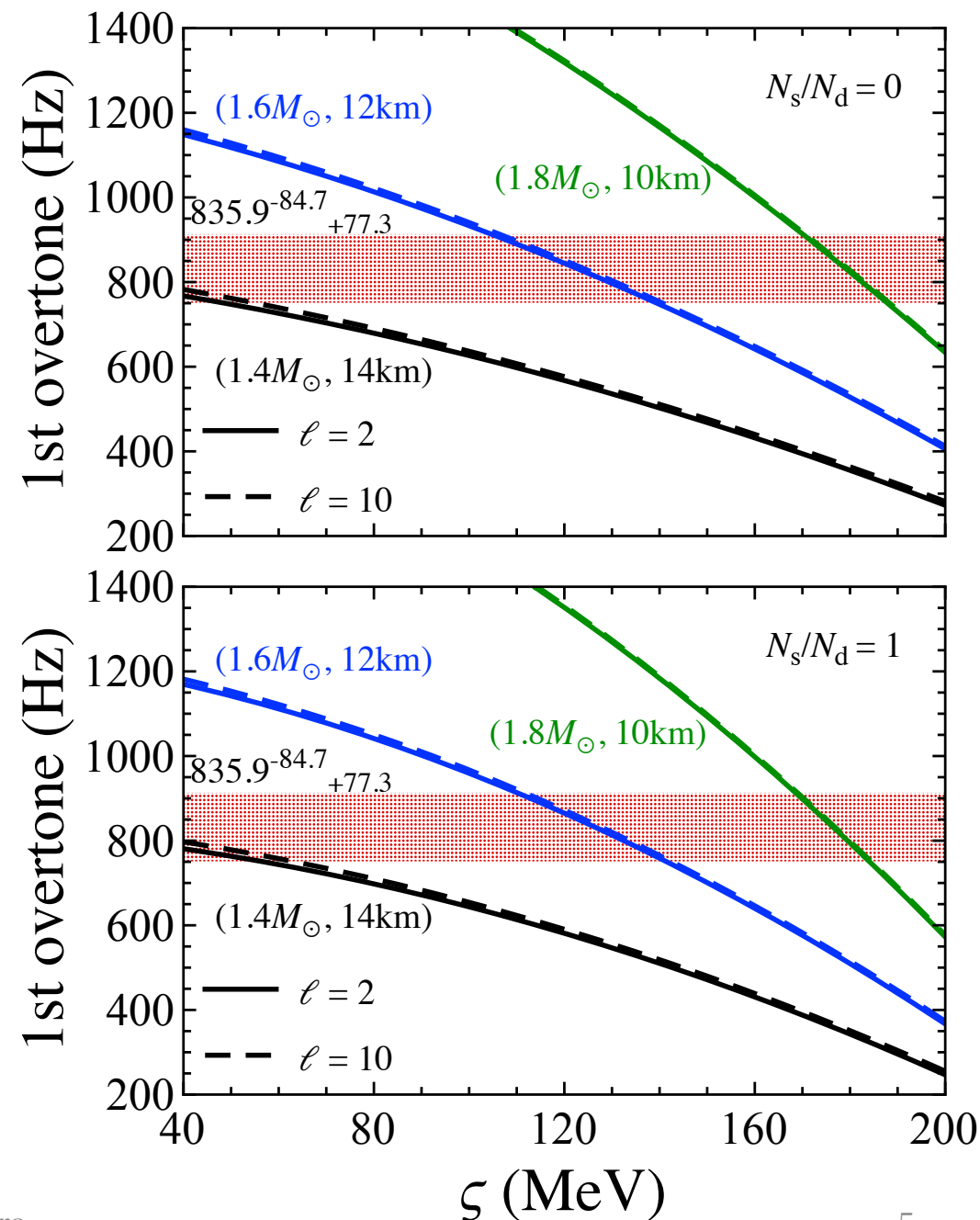
- In fact, fre. can be expressed as

$$\ell t_n = d_{\ell n}^{(0)} + d_{\ell n}^{(1)} \varsigma_{100} + d_{\ell n}^{(2)} \varsigma_{100}^2$$

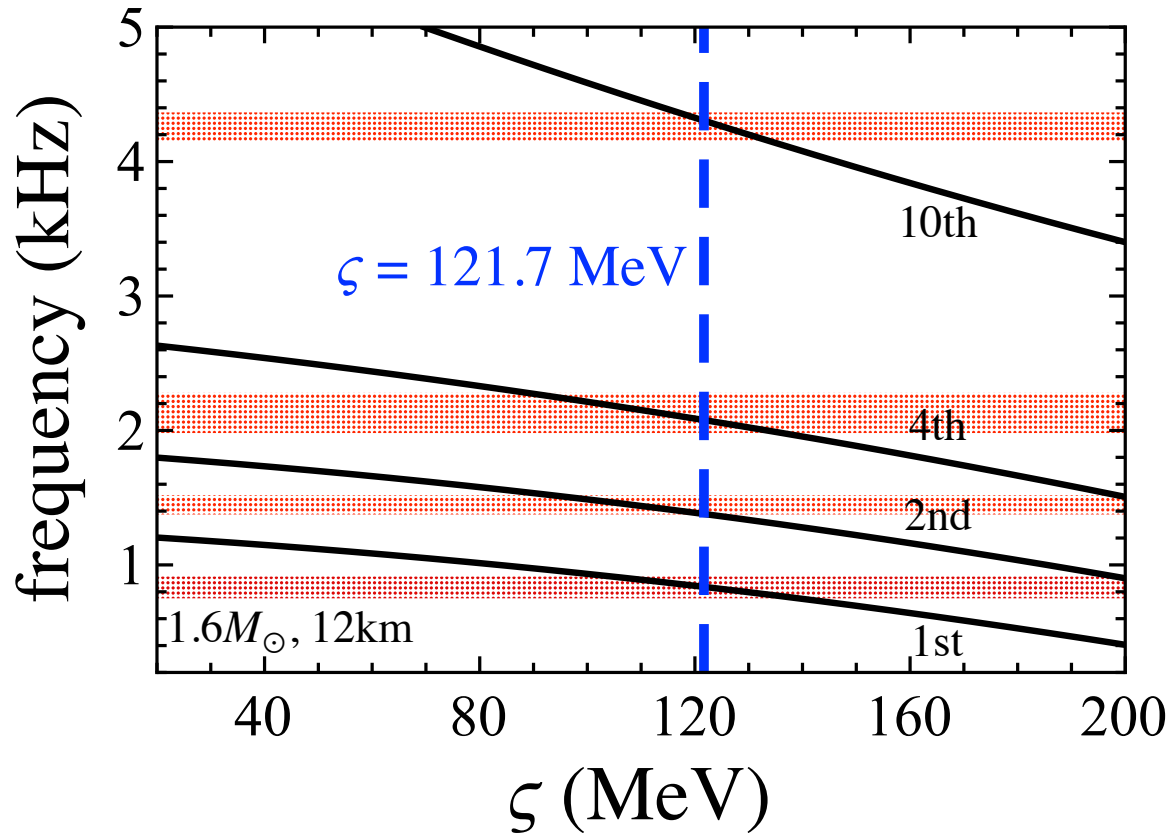
$$\varsigma_{100} \equiv \varsigma / (100 \text{ MeV})$$

# 1<sup>st</sup> overtone

- frequencies increases with M/R
  - $f \sim v_s / \Delta R$  (Hansen & Cioffi 80)
  - $\Delta R/R \sim R/M$  (HS+ 17)
- one can neglect the  $\ell$ -dep. &  $N_s/N_d$ -dep.
  - hereafter, we consider only the  $\ell = 2$  mode with  $N_s/N_d=0$
- to identify the 836 Hz QPO with the 1<sup>st</sup> overtone frequency, one must determine a specific value of  $\zeta$ , depending on (M,R)

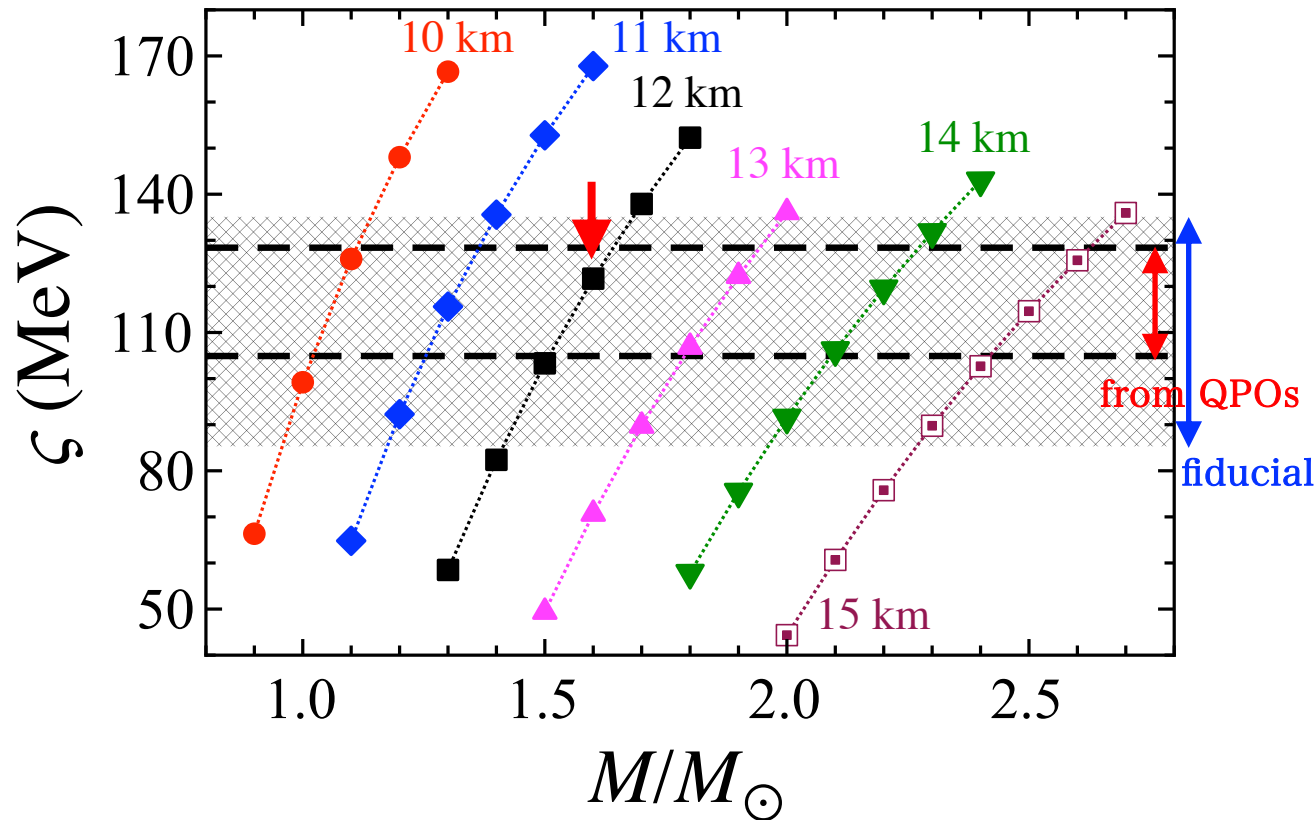


# identification of all QPOs



- the observed QPOs in GRB 200415A can be identified with the 1<sup>st</sup>, 2<sup>nd</sup>, 4<sup>th</sup>, and 10<sup>th</sup> overtones of crustal torsional oscillations
- for NS models with  $1.6M_{\odot}$  and 12km,  $\zeta$  should be 122 MeV for the identification.
- with different NS models, fre. shift up and down, which leads to  $\zeta$  for identification also shifts right and left.
  - frequencies increases with M/R

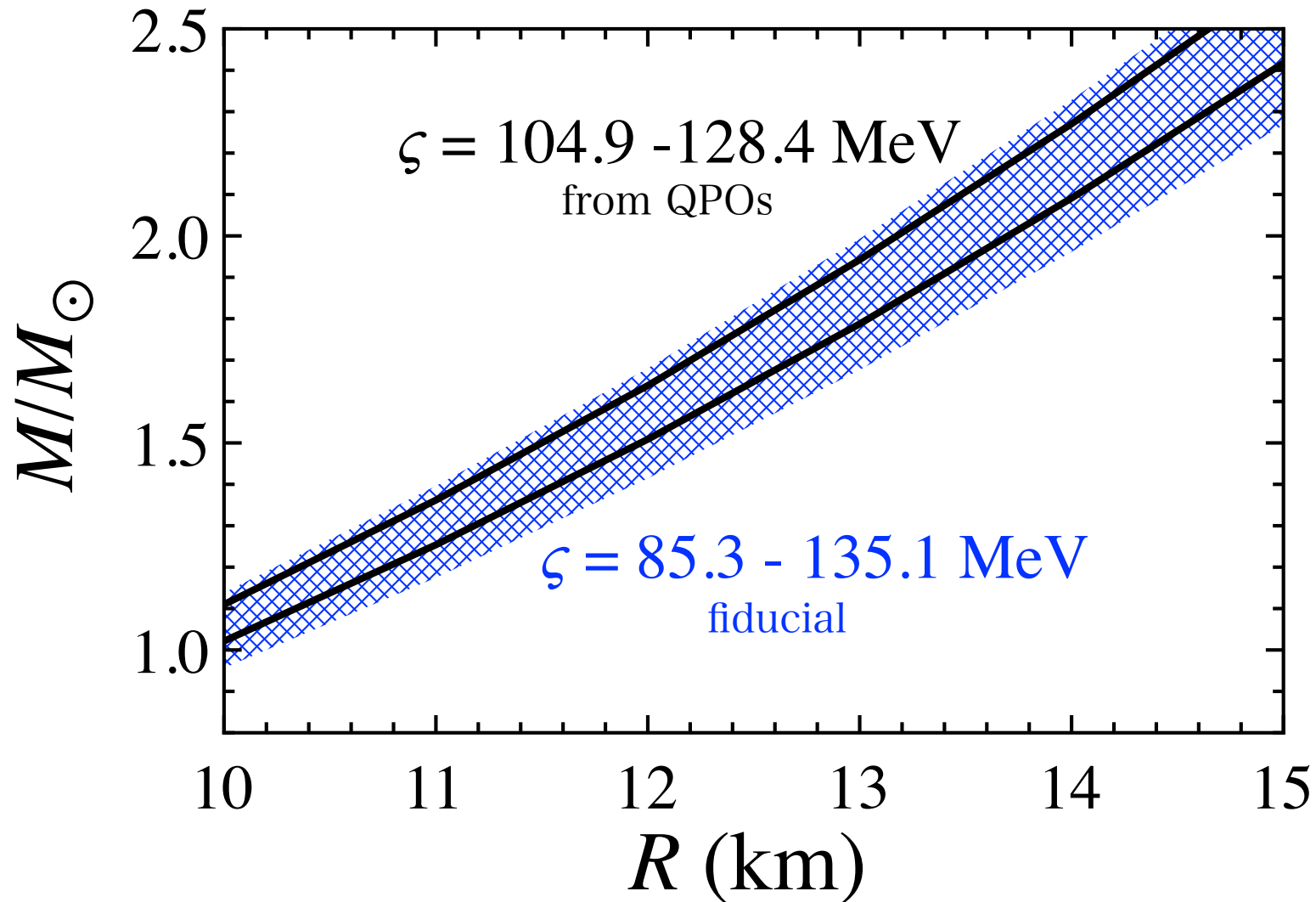
# NS models for identifying QPOs



- $\zeta$  for identifying the QPOs with various NS models
- fiducial value of  $\zeta = 85.3 - 135.1$  MeV
  - $L = 60 \pm 20$  MeV
  - $K_0 = 240 \pm 20$  MeV
- constrained from QPO obs.;  $\zeta = 104.9 - 128.4$  MeV
  - $L = 58 - 73$  MeV (HS+2018)
  - $K_0 = 240 \pm 20$  MeV
- compared to the fiducial value of  $\zeta$ , one can get the constraints on NS mass and radius



# NSs constrained from GRB 200415A



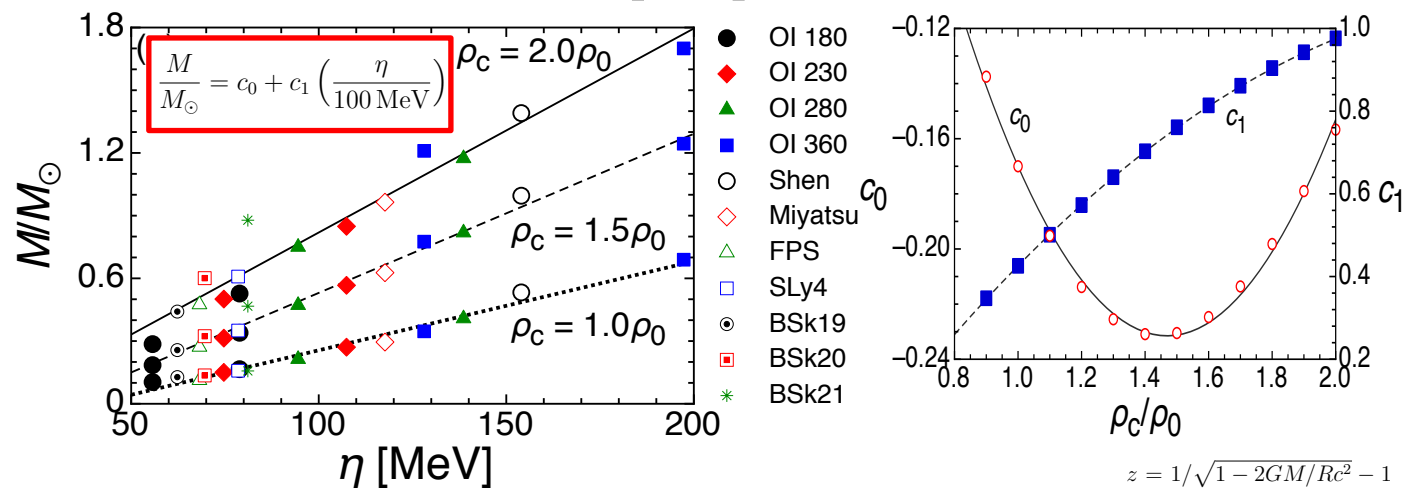
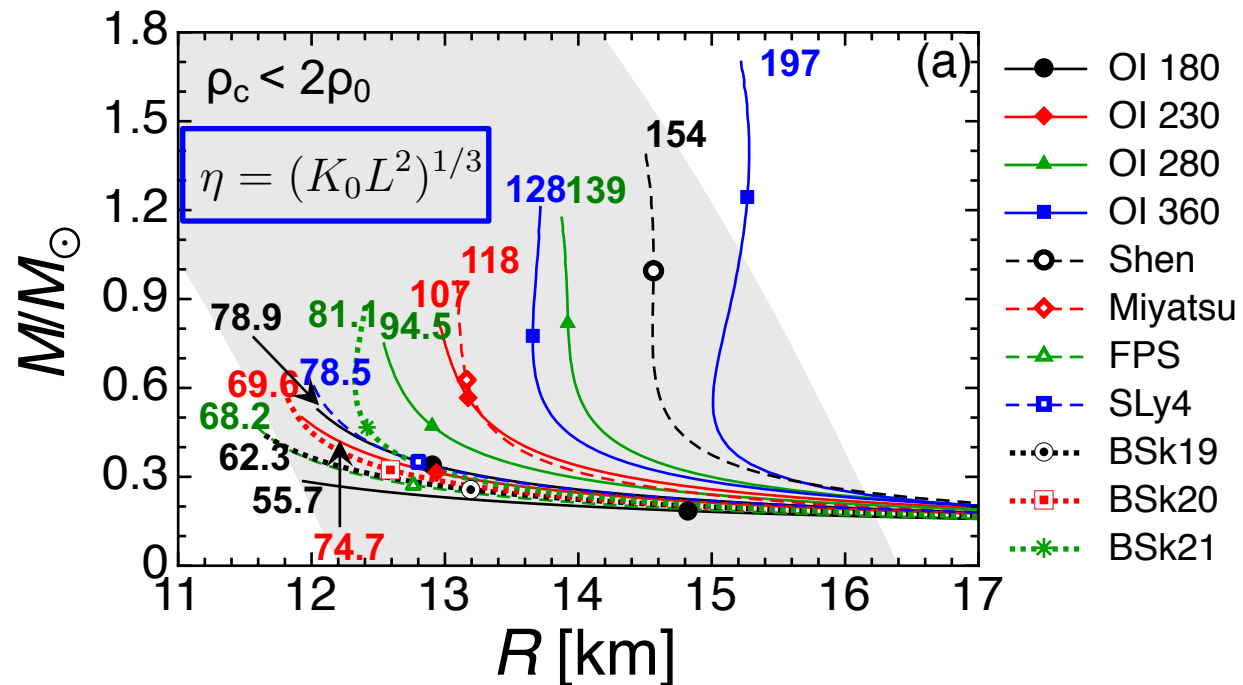
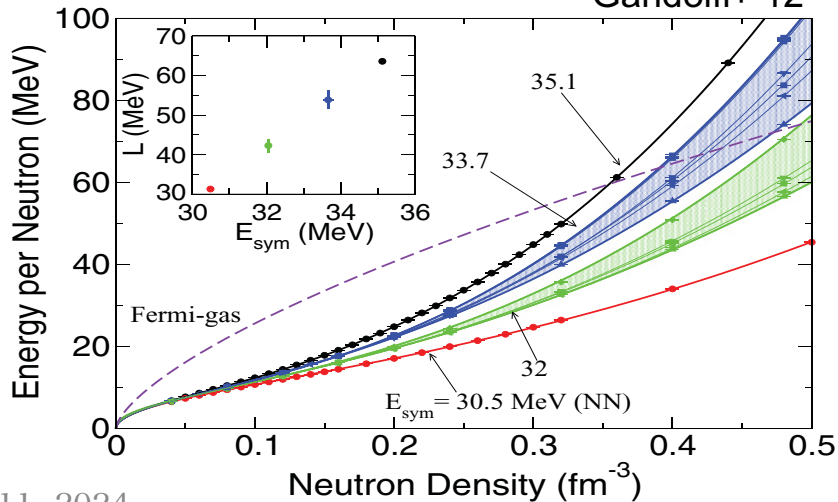
# Mass formula (HS+14)

- low-mass NSs
  - low-central density
  - EOS for a low-density region plays an important role
  - may be able to discuss the stellar models without the core EOS
  - $1.174M_{\odot}$  NS exists (Martinez+ 15)

- we focus on the NS models for  $\rho \lesssim 2\rho_0$

$$w = w_0 + \frac{K_0}{18n_0^2}(n - n_0)^2 + \left[ S_0 + \frac{L}{3n_0}(n - n_0) \right] \alpha^2$$

Gandolfi+ 12

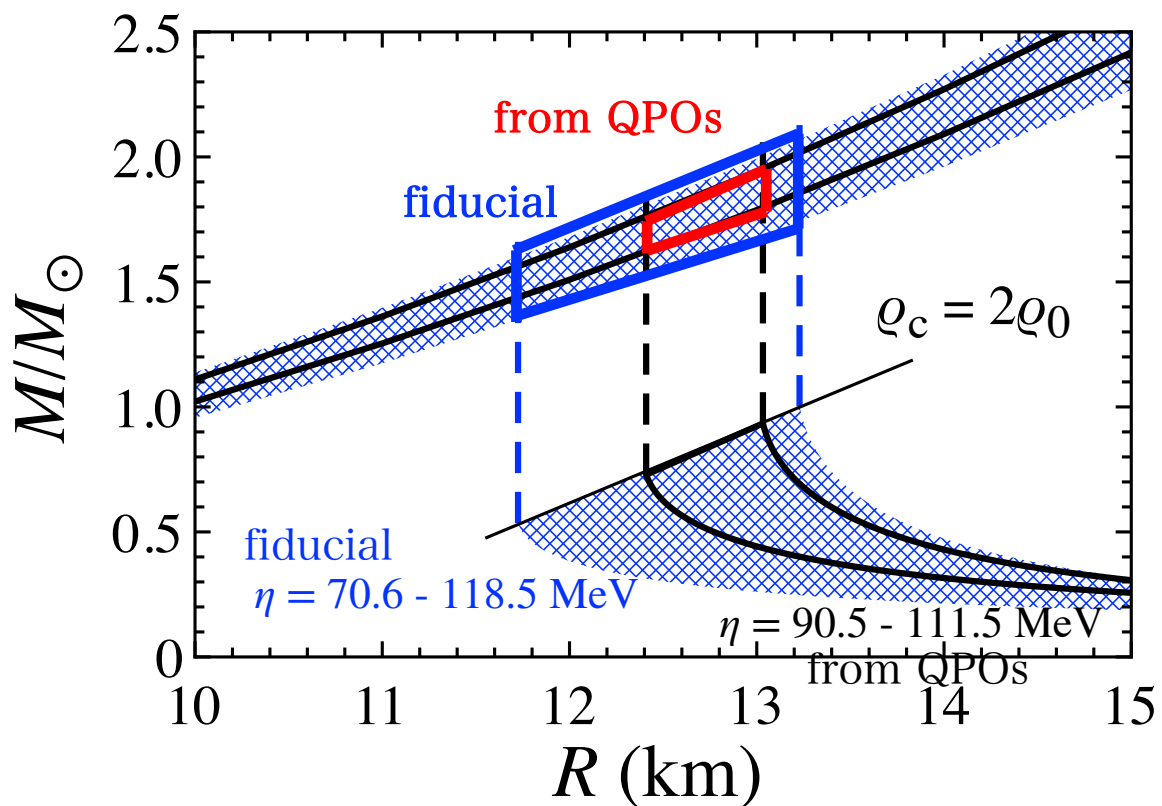


$$\frac{M}{M_{\odot}} = 0.371 - 0.820u_c + 0.279u_c^2 - (0.593 - 1.254u_c + 0.235u_c^2) \left( \frac{\eta}{100 \text{ MeV}} \right)$$

$$z = 0.00859 - 0.0619u_c + 0.0255u_c^2 - (0.0429 - 0.108u_c + 0.0120u_c^2) \left( \frac{\eta}{100 \text{ MeV}} \right)$$

$z = 1/\sqrt{1 - 2GM/Rc^2} - 1$

# make constraint more severe

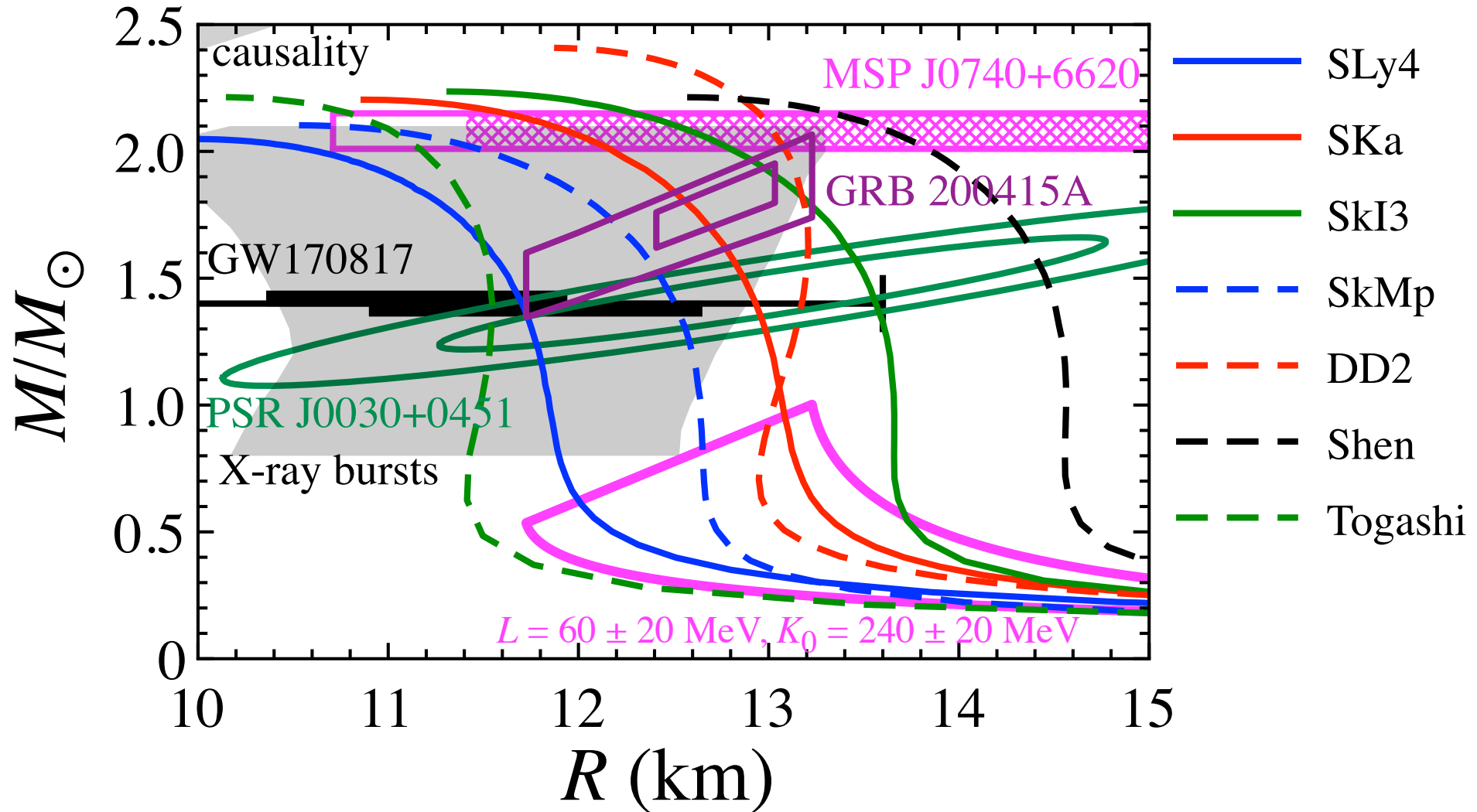


- low-mass NS can be expressed with  $\eta$  and  $\rho_c$  up to  $\rho_c = 2\rho_0$  (HS+ 14);  $\eta = (K_0 L^2)^{1/3}$  &  $u_c \equiv \rho_c/\rho_0$ 

$$\frac{M}{M_{\odot}} = 0.371 - 0.820u_c + 0.279u_c^2 - (0.593 - 1.254u_c + 0.235u_c^2) \left(\frac{\eta}{100 \text{ MeV}}\right)$$

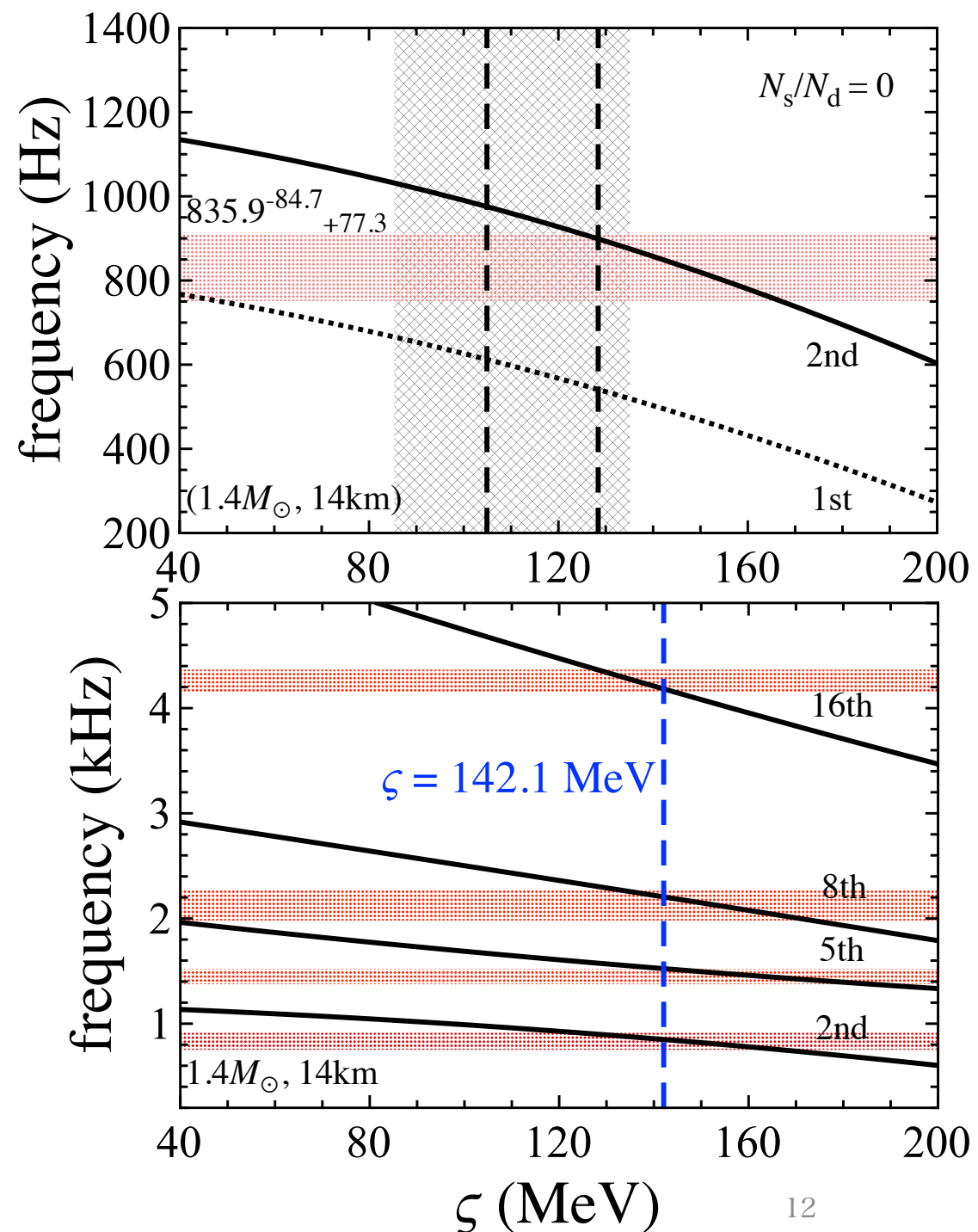
$$z = 0.00859 - 0.0619u_c + 0.0255u_c^2 - (0.0429 - 0.108u_c + 0.0120u_c^2) \left(\frac{\eta}{100 \text{ MeV}}\right)$$
- we focus on  $z = 1/\sqrt{1 - 2GM/Rc^2} - 1$ 
  - $\eta = 70.6 - 118.5$  MeV ( $\zeta = 85.3 - 135.1$  MeV)
  - $\eta = 85.3 - 135.1$  MeV ( $\zeta = 104.9 - 128.4$  MeV)
- suppose that the radius of NS with  $\rho_c \geq 2\rho_0$  is constant
- then, we can get the NS mass and radius constraint as an intersection

# Comparison with other constraints



# Another possibility

- up to now, we identify the lowest QPO in GRB 200415A with the 1<sup>st</sup> overtone
- the identification with the 2<sup>nd</sup> overtone is also possible
  - $\zeta$  for this identification for NS models with  $1.4M_{\odot}$  and 14 km is relatively large
  - frequency increases with M/R
  - to identify with this correspondence, standard NS models must give us out of the fiducial value of  $\zeta$



# Magnetic effects

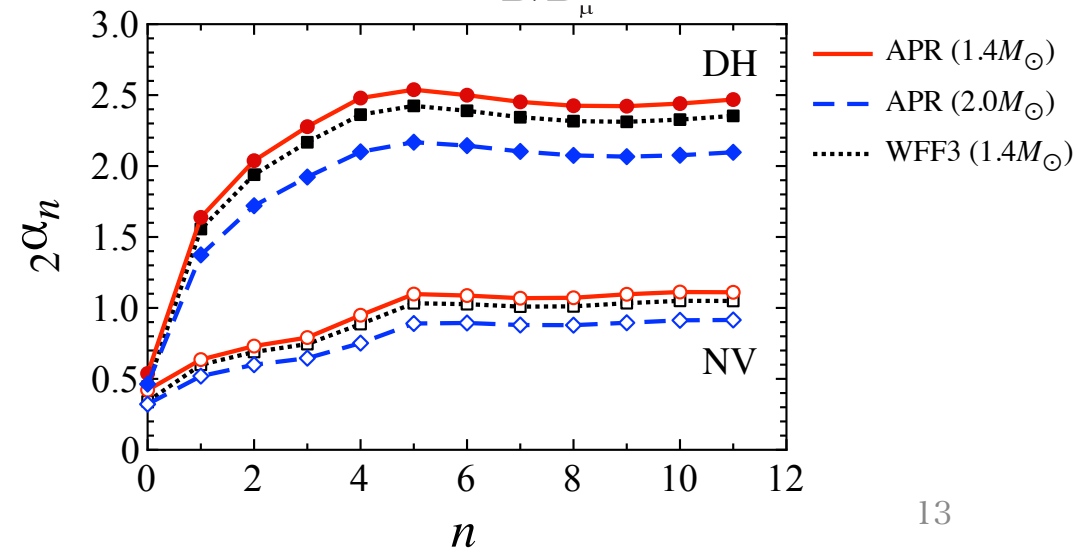
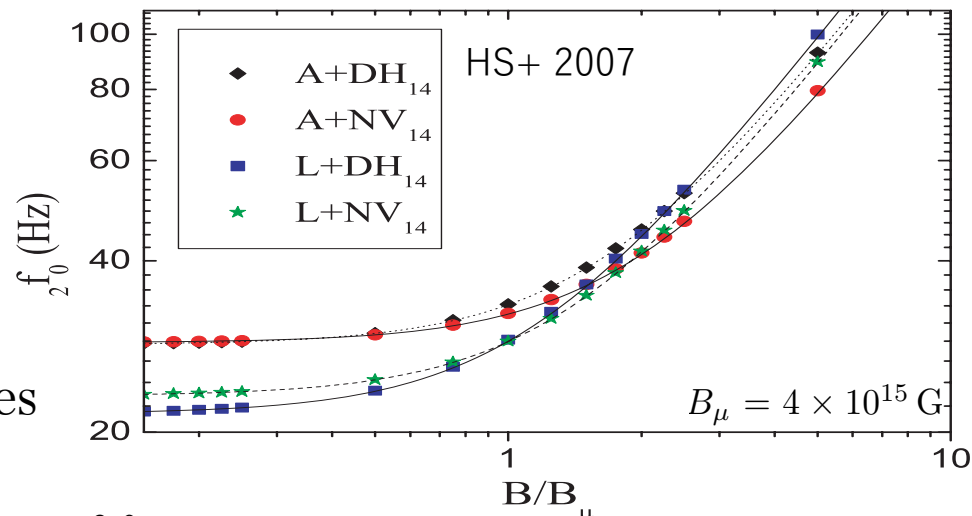
- the shift in the torsional oscillations frequencies obeys the following formula (HS+2007; Gabler+2018)

$$\frac{\ell f_n}{\ell f_n^{(0)}} \approx \left[ 1 + \ell \alpha_n \left( \frac{B}{B_\mu} \right)^2 \right]^{1/2} \quad B_\mu = 4 \times 10^{15} \text{ G}$$

- for the overtones,
  - for EOS NV  $2\alpha_n \approx 0.8 - 1.1$
  - for EOS DH  $2\alpha_n \approx 2 - 2.5$
- the deviation of the magnetized neutron star frequencies from those of the non-magnetized ones are
  - $\lesssim 3.4\%$  for the EOS NV
  - $\lesssim 7.5\%$  for the EOS DH,

if we assume  $B \approx 10^{15} \text{ G}$

- These values are still within the limits of uncertainty ( $\sim 10\%$ ) estimated in Castro-Tirado+ (2021)
- So, simply we neglect the magnetic effects here.



# Conclusion

- magnetar QPOs are newly found in a giant gamma-ray flare (GRB 200415A)
- they can be identified with the overtones of the crustal torsional oscillations
- we get the constraint on NS mass and radius

