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## General formulae for the periapsis shift of a quasi-circular orbit in static spherically symmetric spacetimes and the strong energy condition

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We study the periapsis shift of a quasi-circular orbit in general static spherically symmetric spacetimes. We derive two formulae in full order with respect to the gravitational field, one in terms of the gravitational mass  $m$  and the Einstein tensor and the other in terms of the orbital angular velocity and the Einstein tensor. These formulae reproduce the well-known ones for the forward shift in the Schwarzschild spacetime. In a general case, the shift deviates from that in the vacuum spacetime due to a particular combination of the components of the Einstein tensor at the radius  $r$  of the orbit. The formulae give a backward shift due to the extended-mass effect in Newtonian gravity. In general relativity, in the weak-field and diffuse regime, the active gravitational mass density,  $\rho_A = (\epsilon + p_r + 2p_t)/c^2$ , plays an important role, where  $\epsilon$ ,  $p_r$  and  $p_t$  are the energy density, the radial stress and the tangential stress of the matter field, respectively. We show that the shift is backward if  $\rho_A$  is beyond a critical value  $\rho_{c2} \approx 2.8 \times 10^{-15} \text{g/cm}^3 (m/M_\odot)^2 (r/\text{a.u.})^{-4}$ , while a forward shift greater than that in the vacuum spacetime instead implies  $\rho_A < 0$ , i.e. the violation of the strong energy condition, and thereby provides evidence for dark energy. We obtain new observational constraints on  $\rho_A$  in the Solar System and the Galactic Centre.

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