A Cosmic Microwave Background (CMB) fluctuation map showing temperature variations across the sky. The map is a Mollweide projection, appearing as a curved, dome-like surface. The color scale ranges from dark blue (cooler) to red (warmer), with yellow and orange indicating intermediate temperatures. The fluctuations are most prominent in the lower right quadrant, showing a large-scale structure. The overall pattern is a complex, noisy texture of small-scale variations.

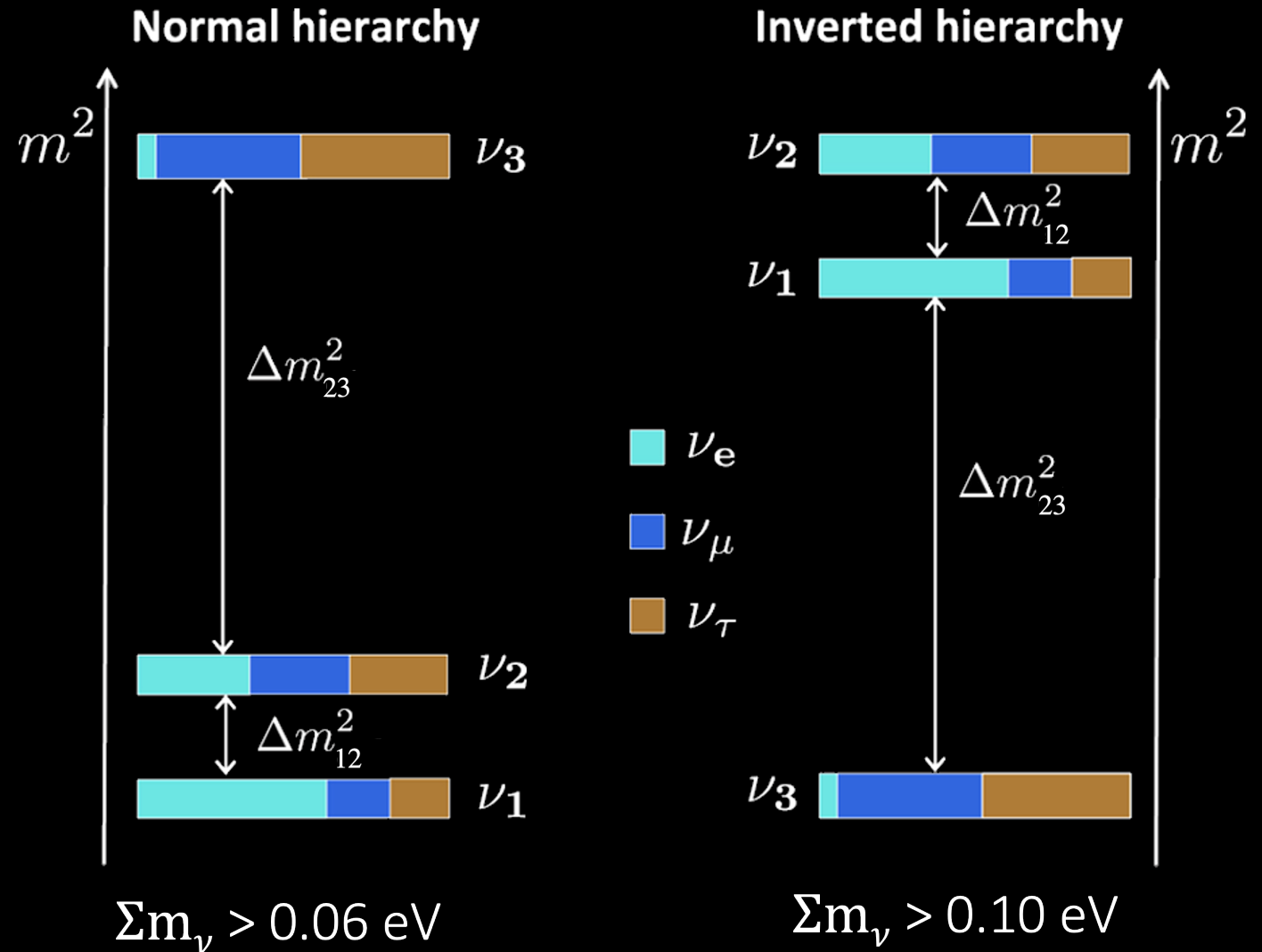
# Cosmological limits on neutrino mass sum for beyond- $\Lambda$ CDM models

---

Helen Shao, Jo Dunkley, Jahmour Givans,  
Mathew Madhavacheril, Frank Qu, Blake  
Sherwin, Gerrit Farren, et al.

# Neutrino Mass

- Neutrinos oscillate between masses

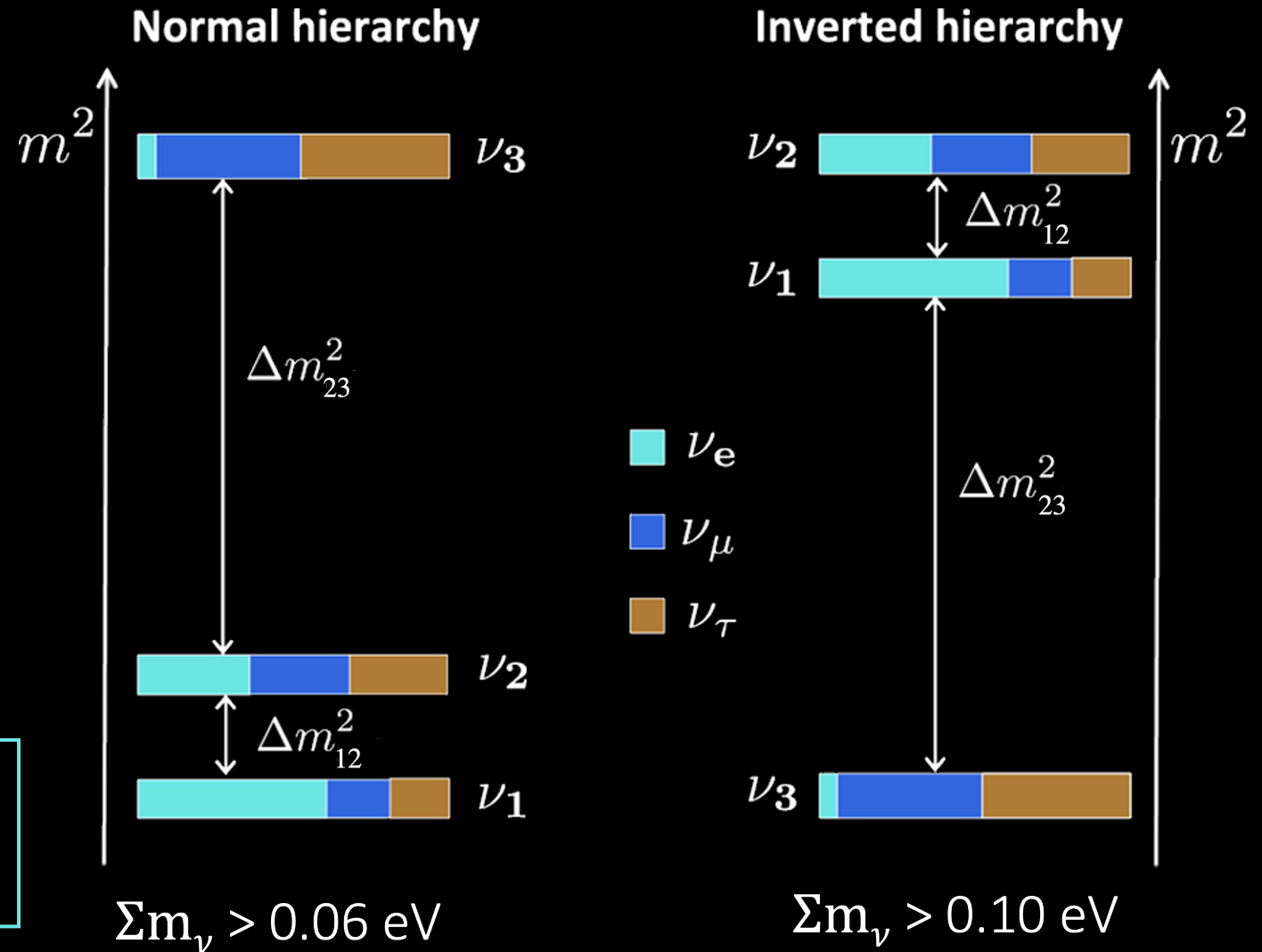


# Neutrino Mass

- Neutrinos oscillate between masses
- Direct detection experiments (KATRIN):  
 $m_\beta < 0.8 \text{ eV}$  (Acker 2021, 90%)

$$\Delta m_{12}^2$$

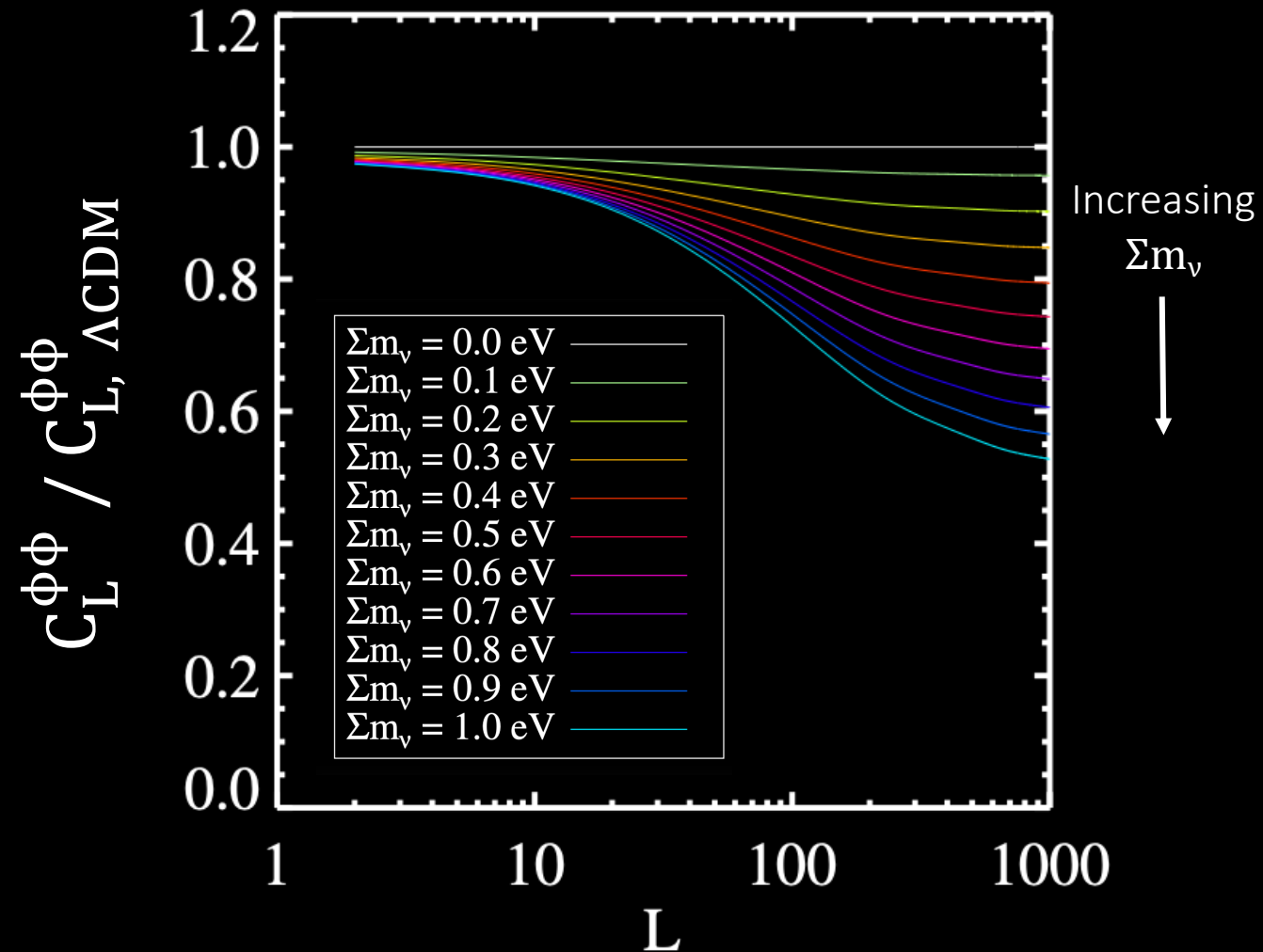
$$\Delta m_{23}^2 \text{ or } \Delta m_{13}^2$$



# $\Sigma m_\nu$ from cosmology

- Neutrino free-streaming  
→ suppression of structure growth on small-scales

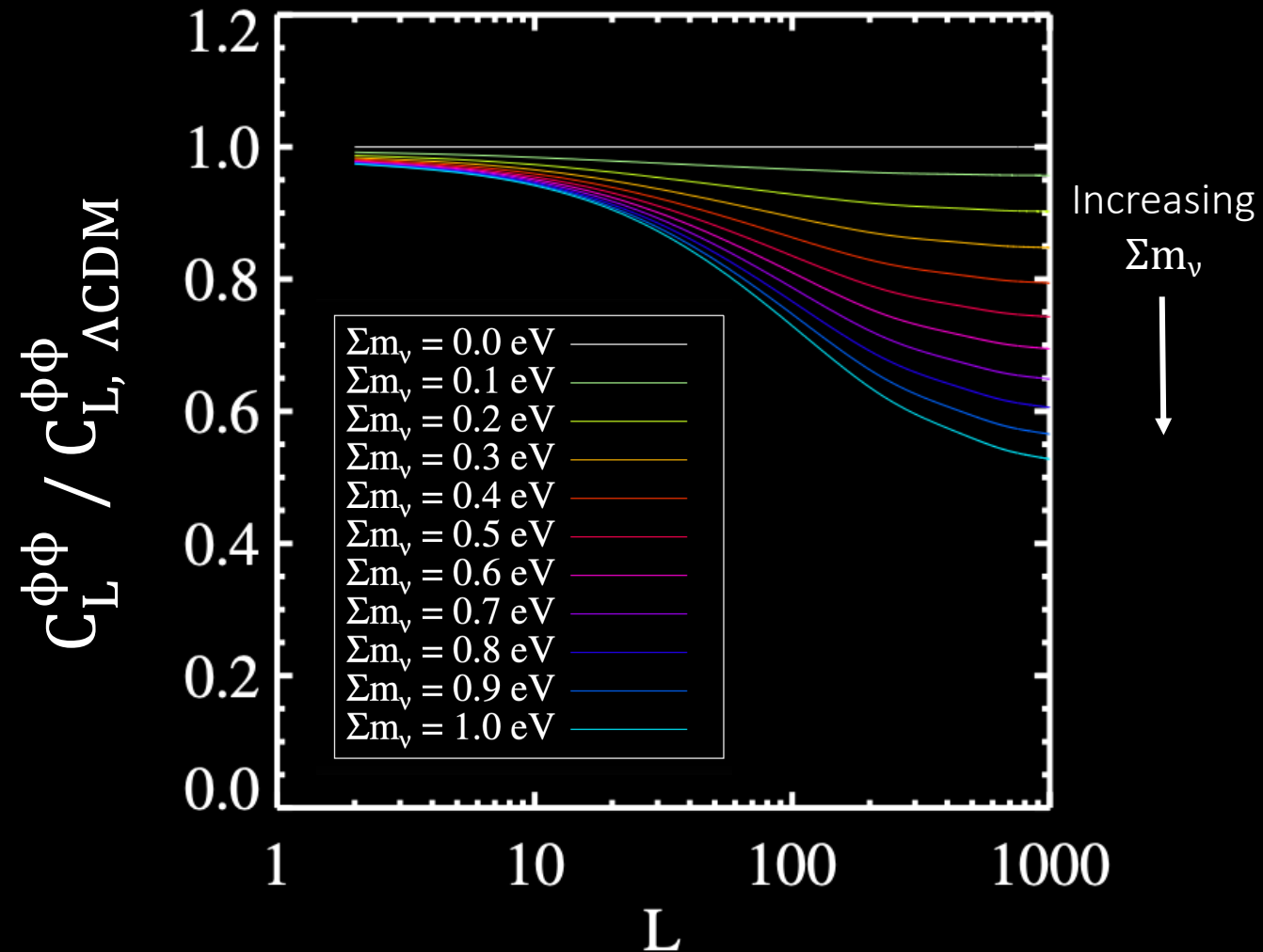
CMB Lensing Potential Power (2D)  
relative



# $\Sigma m_\nu$ from cosmology

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- $\Sigma m_\nu < 0.12$  eV (Planck18, 95%),  
< 0.072 eV (DESI, 95%)

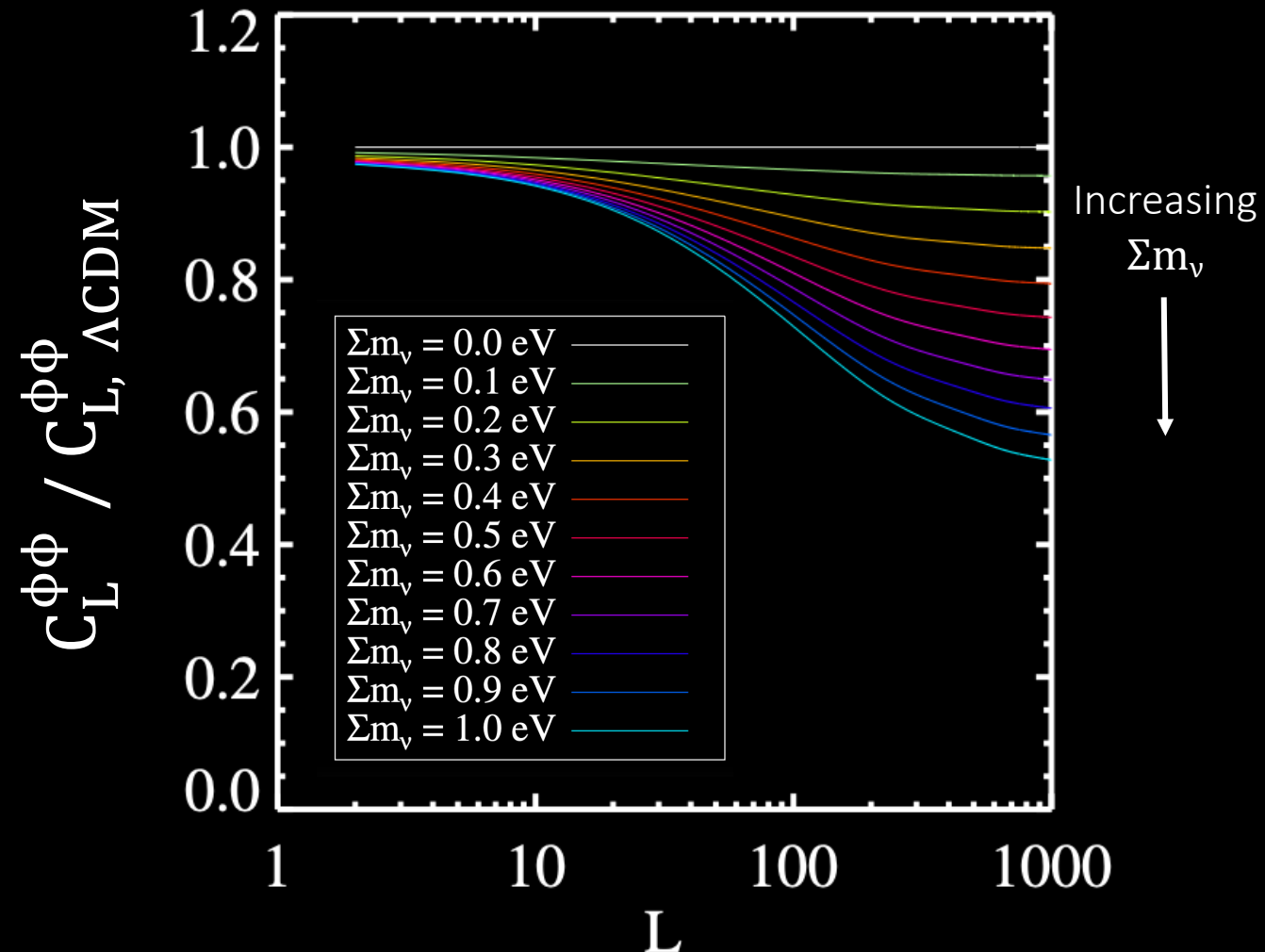
CMB Lensing Potential Power (2D)  
relative

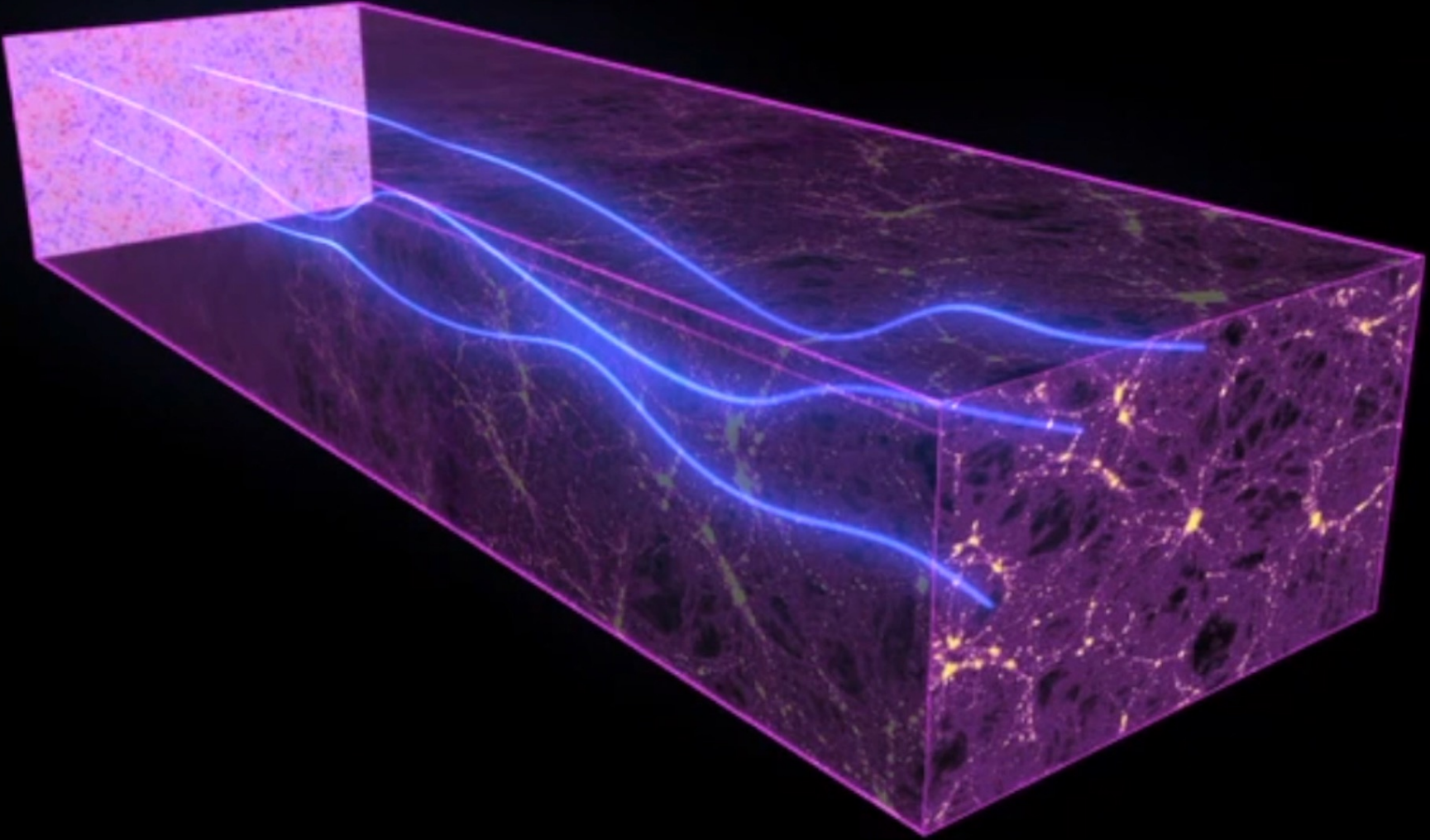


# $\Sigma m_\nu$ from cosmology

- Neutrino free-streaming  
→ suppression of structure growth on small-scales
- $\Sigma m_\nu < 0.12$  eV (Planck18, 95%),  
< 0.072 eV (DESI, 95%)
- Question: are  $\Sigma m_\nu$  bounds robust to cosmologies beyond LCDM?

CMB Lensing Potential Power (2D)  
relative





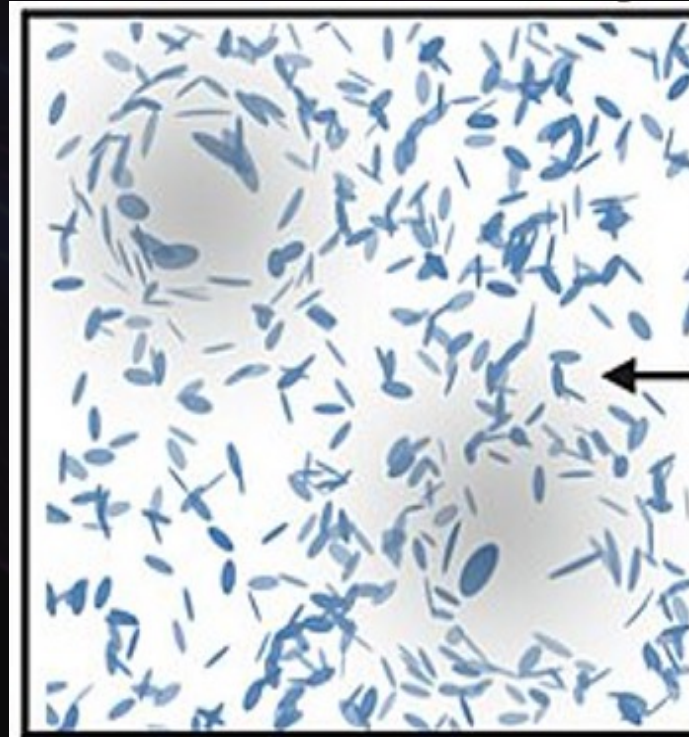




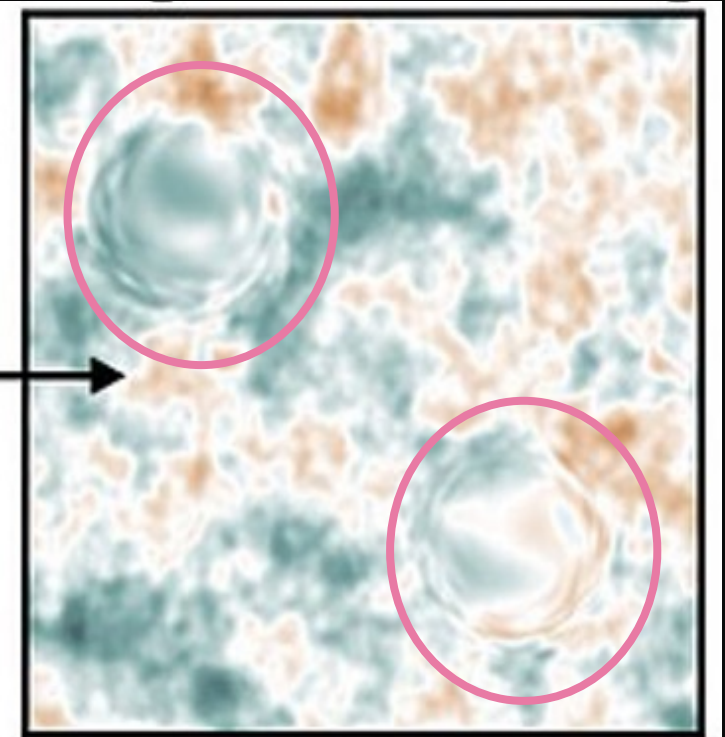
CMB lensing: late universe

Primary CMB: early universe

Galaxies



CMB Lensing



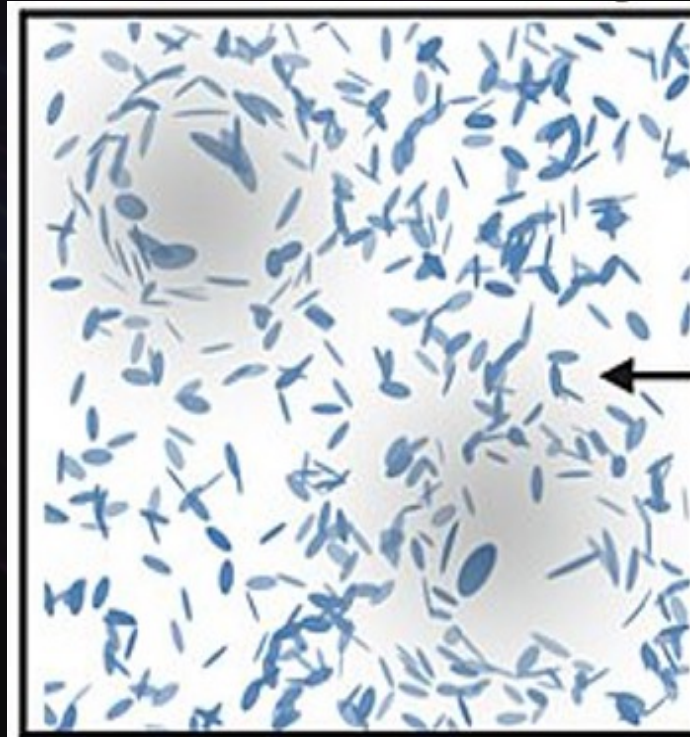
CMB lensing: late universe

Primary CMB: early universe

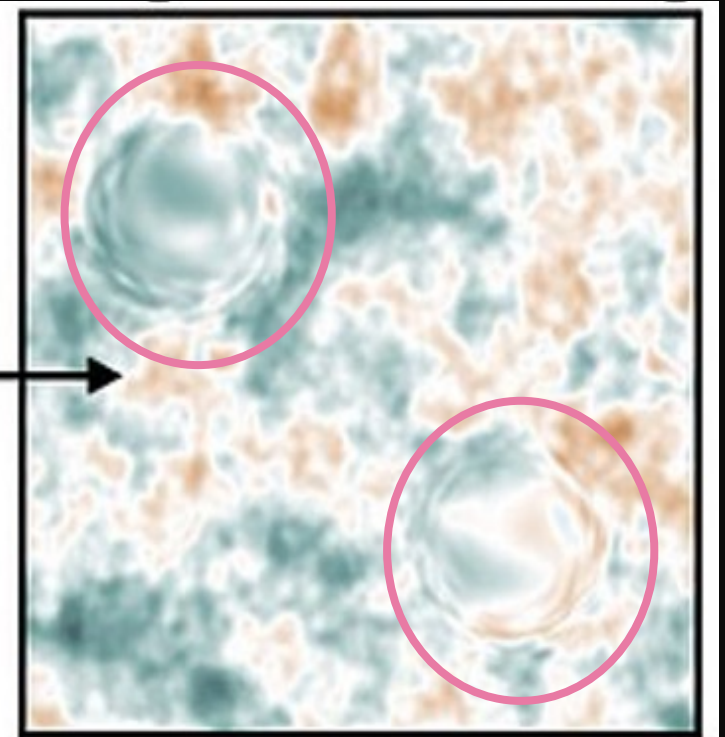
$C_\ell^{\Phi\Phi}$  = lensing power

- Matter clustering
- $\Sigma m_\nu$  suppresses clustering

Galaxies

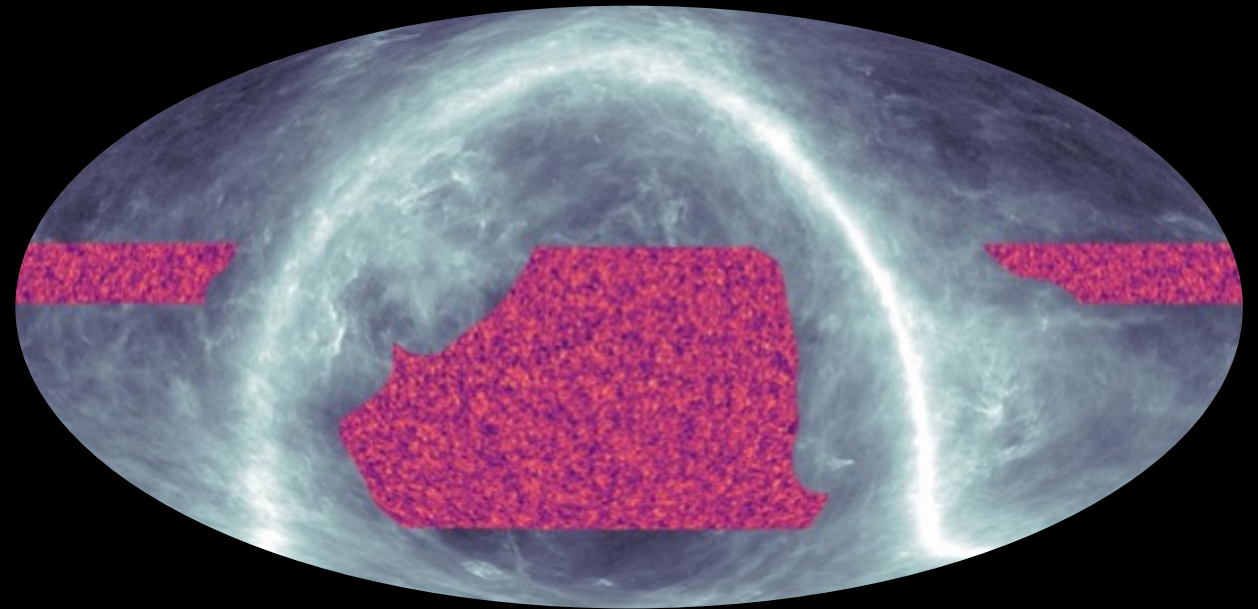


CMB Lensing



# Atacama Cosmology Telescope (ACT)

- 5x Planck resolution
- 2007-2022: 46% of sky
- DR6 lensing: No  $A_{\text{Len}}$  (Planck) anomaly



# Data & Likelihoods

## CMB anisotropies

High- $\ell$ : CamSpec  
TT, TE, EE  
(Rosenberg et al.  
2022)

low- $\ell$ : TT (Planck  
2018), EE sroll2  
(Pagano et al.  
2020)

## Planck Lensing

Planck PR4  
NPIPE (Carron et  
al. 2022)  
 $100 \leq L \leq 2048$

## ACT Lensing

ACT DR6  
(Madhavacheril  
et al. 2023)  
(ACT + Planck  
Lensing)  
 $40 \leq L \leq 763$

## BAO

6dF (Beutler et  
al. 2016)

SDSS  
• DR7 (Percival et  
al. 2010)  
• BOSS DR12  
(Dawson et al.  
2013)  
• DR16 (Alam et  
al 2016)

## Supernovae

Pantheon+  
(Scolnic et al.  
2022)

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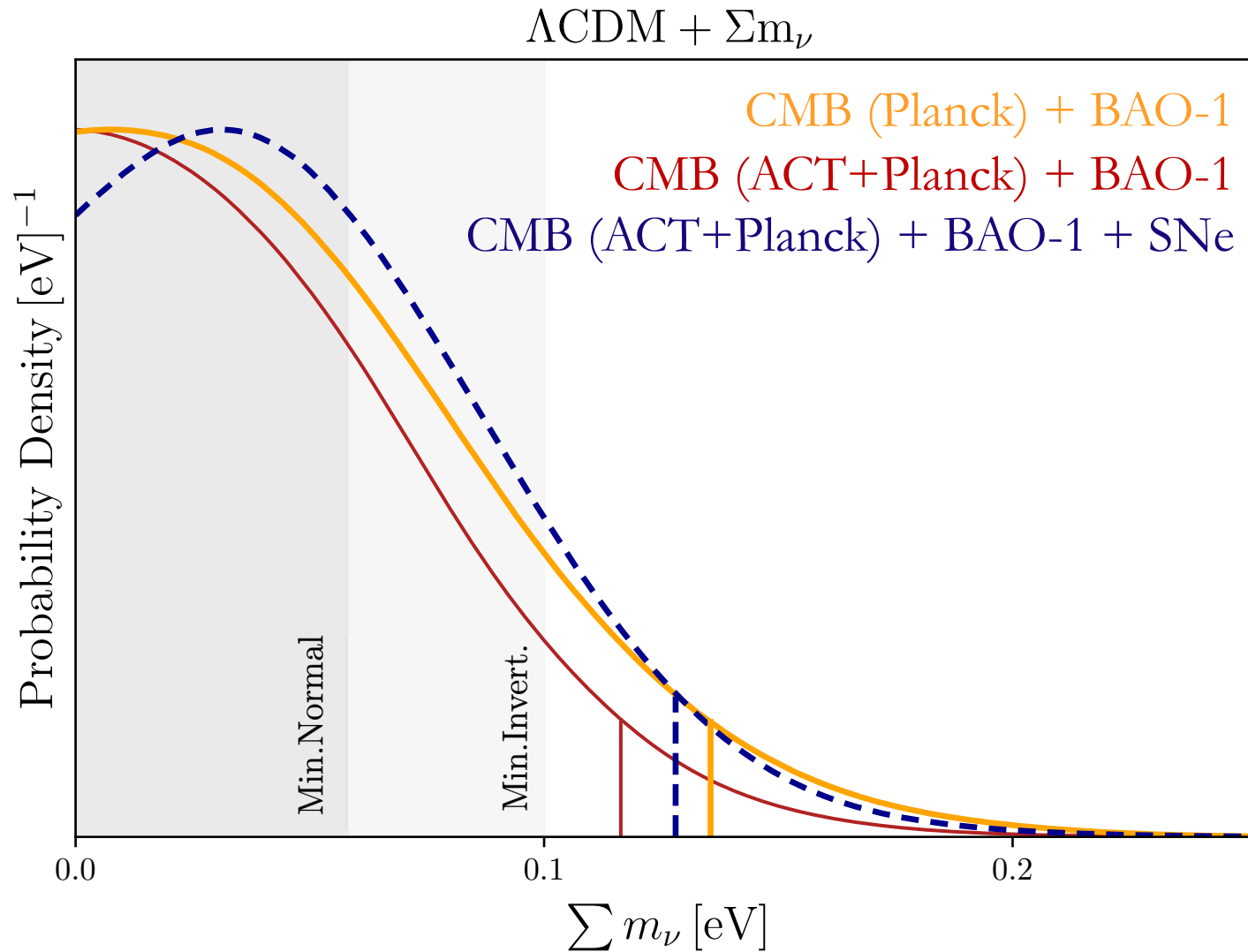
SDSS  
• DR7 (Percival et  
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(Dawson et al.  
2013)  
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al 2016)

DESI 2024

## Supernovae

Pantheon+  
(Scolnic et al.  
2022)

# $\Lambda$ CDM + $\Sigma m_\nu$



Vertical lines indicate  
 $2\sigma$  bounds  
Consistent with  
(Madhavacheril et al., 2023)

$$\Sigma m_\nu < 0.135 \text{ eV}$$

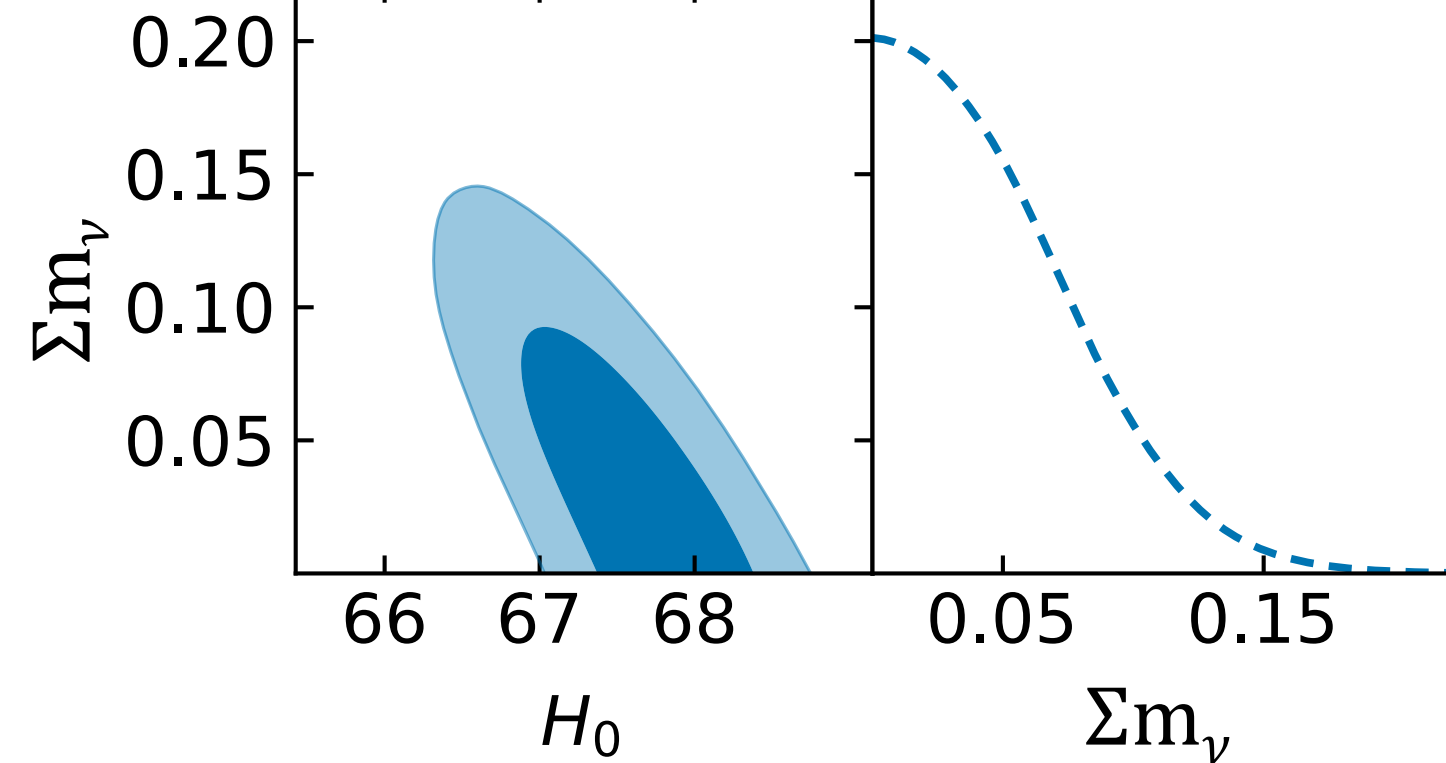
$$\Sigma m_\nu < 0.121 \text{ eV}$$

$$\Sigma m_\nu < 0.129 \text{ eV}$$

■ CMB (ACT + PLANCK) + BAO-1

$$\chi(z_{dec}) = \int_0^{z_{dec}} dz / H(z)$$

$$H(z) = H_0 \sqrt{\Omega_\gamma (1+z)^4 + (\Omega_m)(1+z)^3 + \Omega_{DE}(z) + \rho_\nu(z) / \rho_{cr,0}}$$



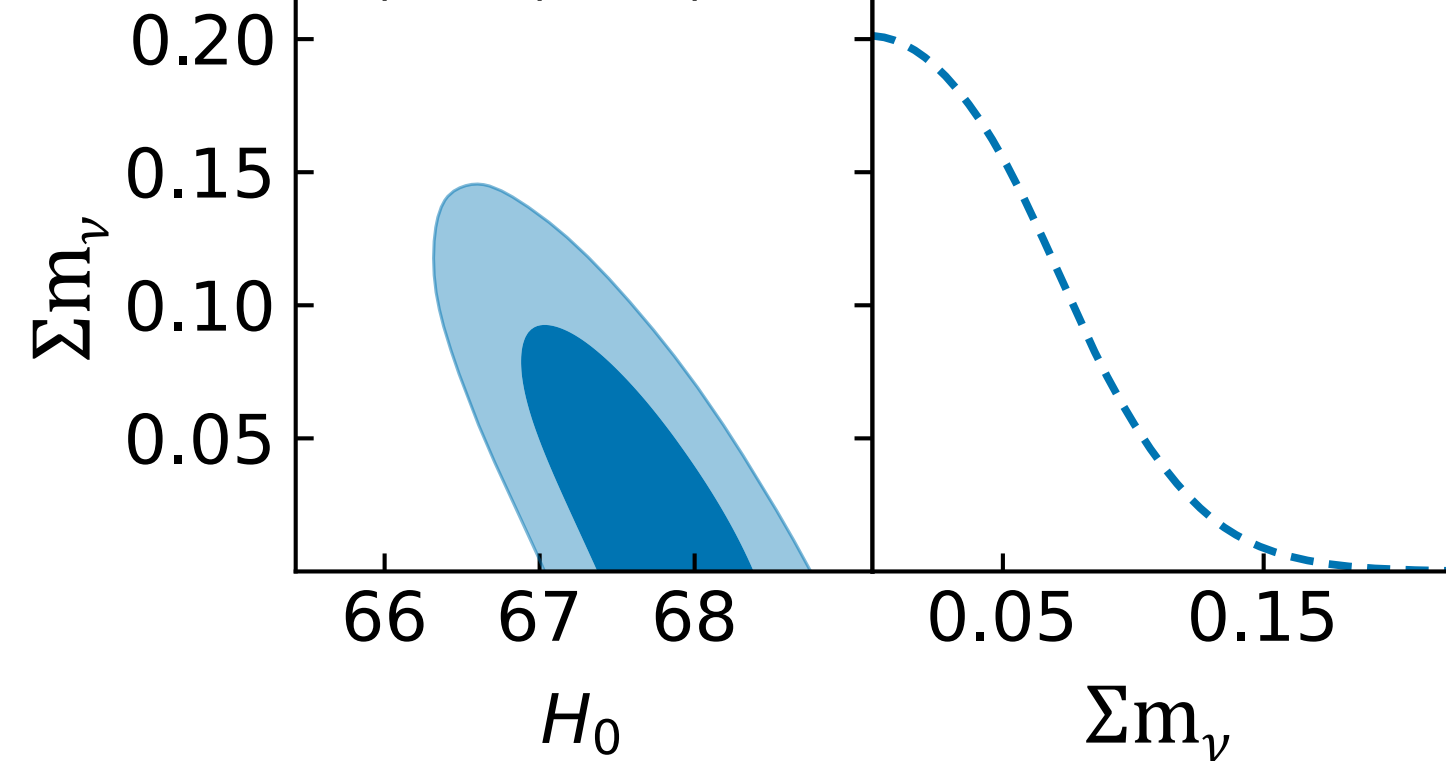
$$\Sigma m_\nu < 0.121 \text{ eV}$$
$$H_0 = 67.45 \pm 0.48$$



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$\Sigma m_\nu$

0.20  
0.15  
0.10  
0.05

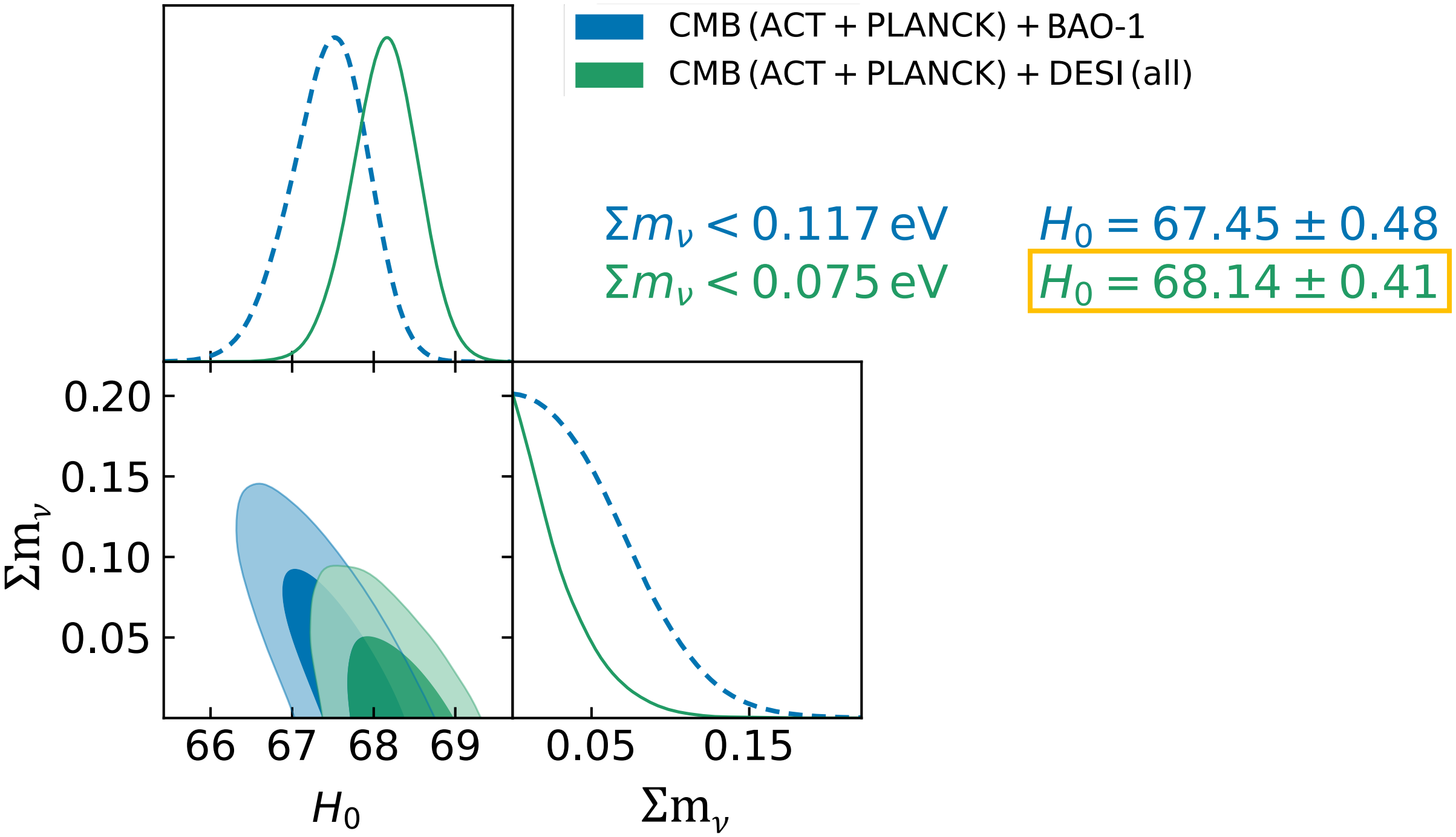
66 67 68

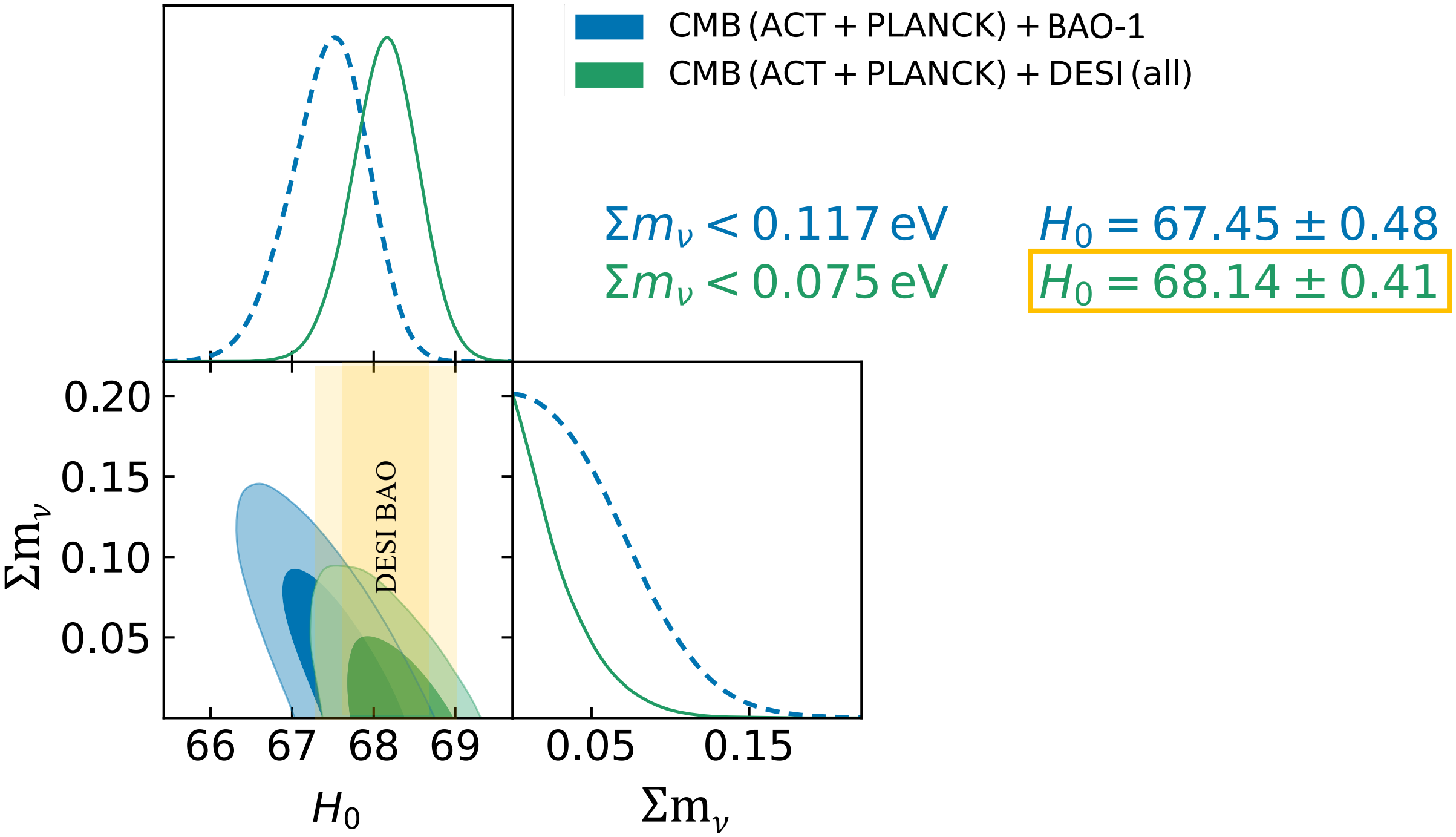
$H_0$

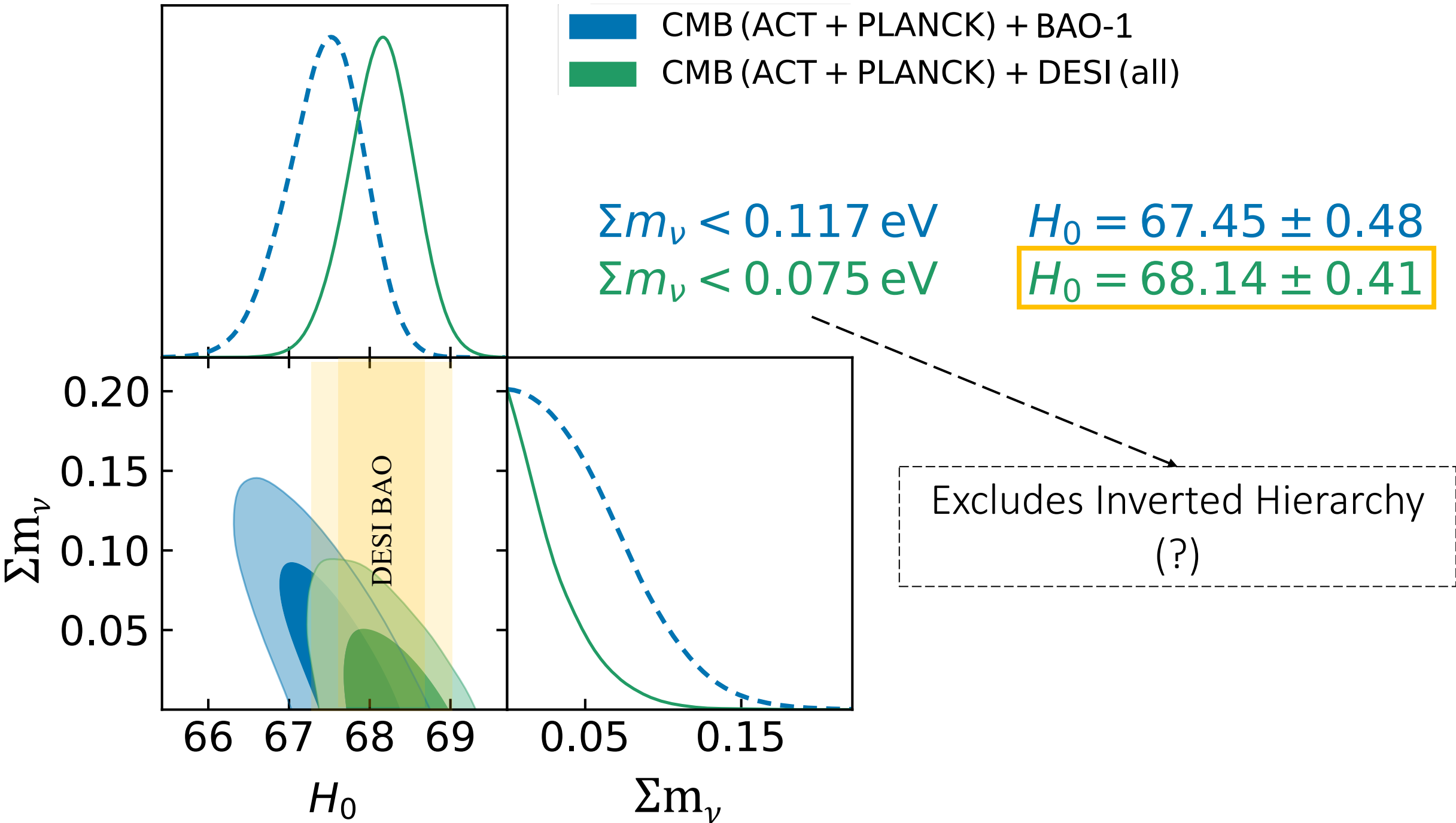
0.05 0.15

$\Sigma m_\nu$

$\Sigma m_\nu < 0.121 \text{ eV}$   
 $H_0 = 67.45 \pm 0.48$

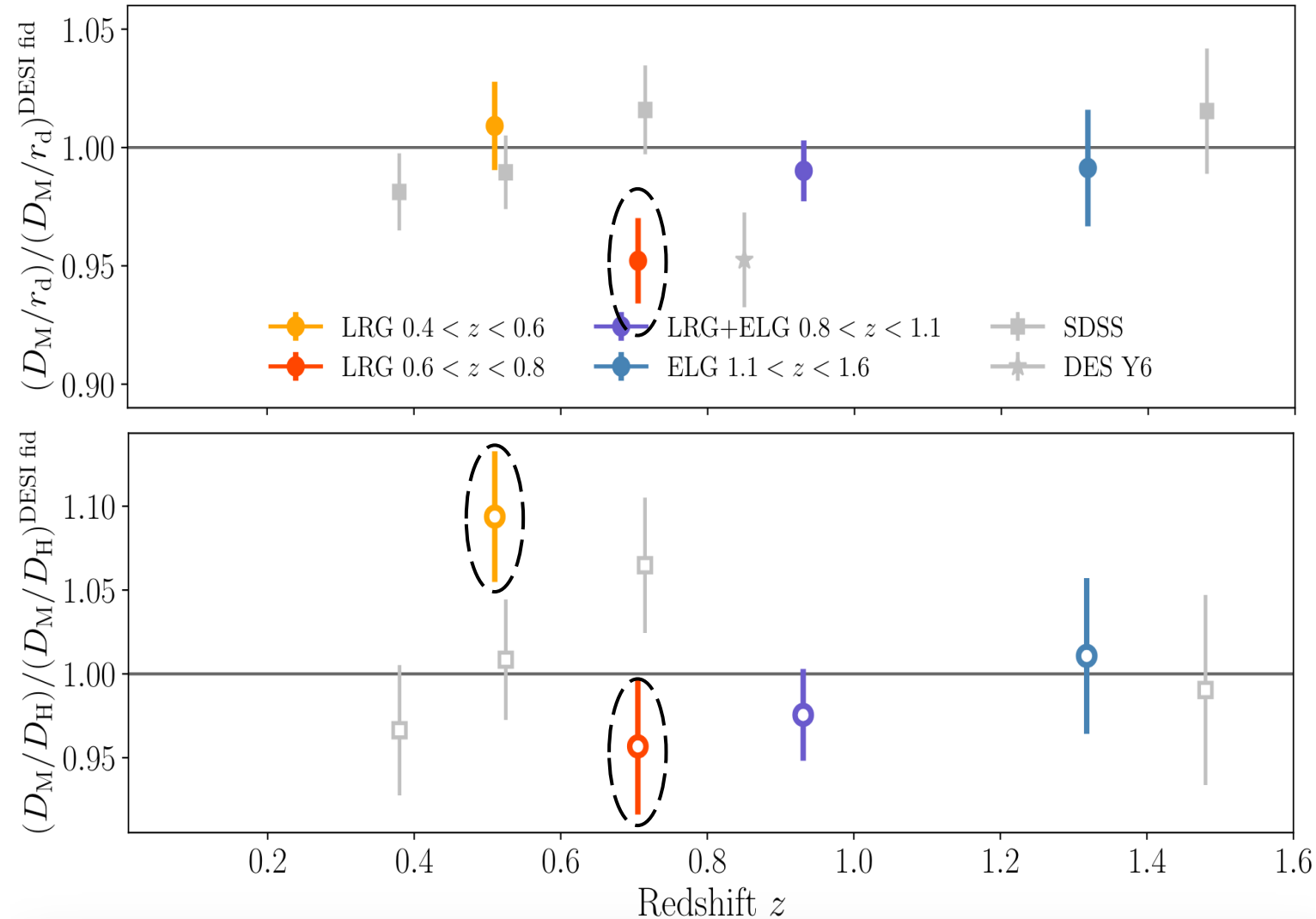






# DESI 2024

**$0.6 < z < 0.8$  LRG**  
 $\sim 3\sigma$  discrepancy  
between DESI and  
SDSS results

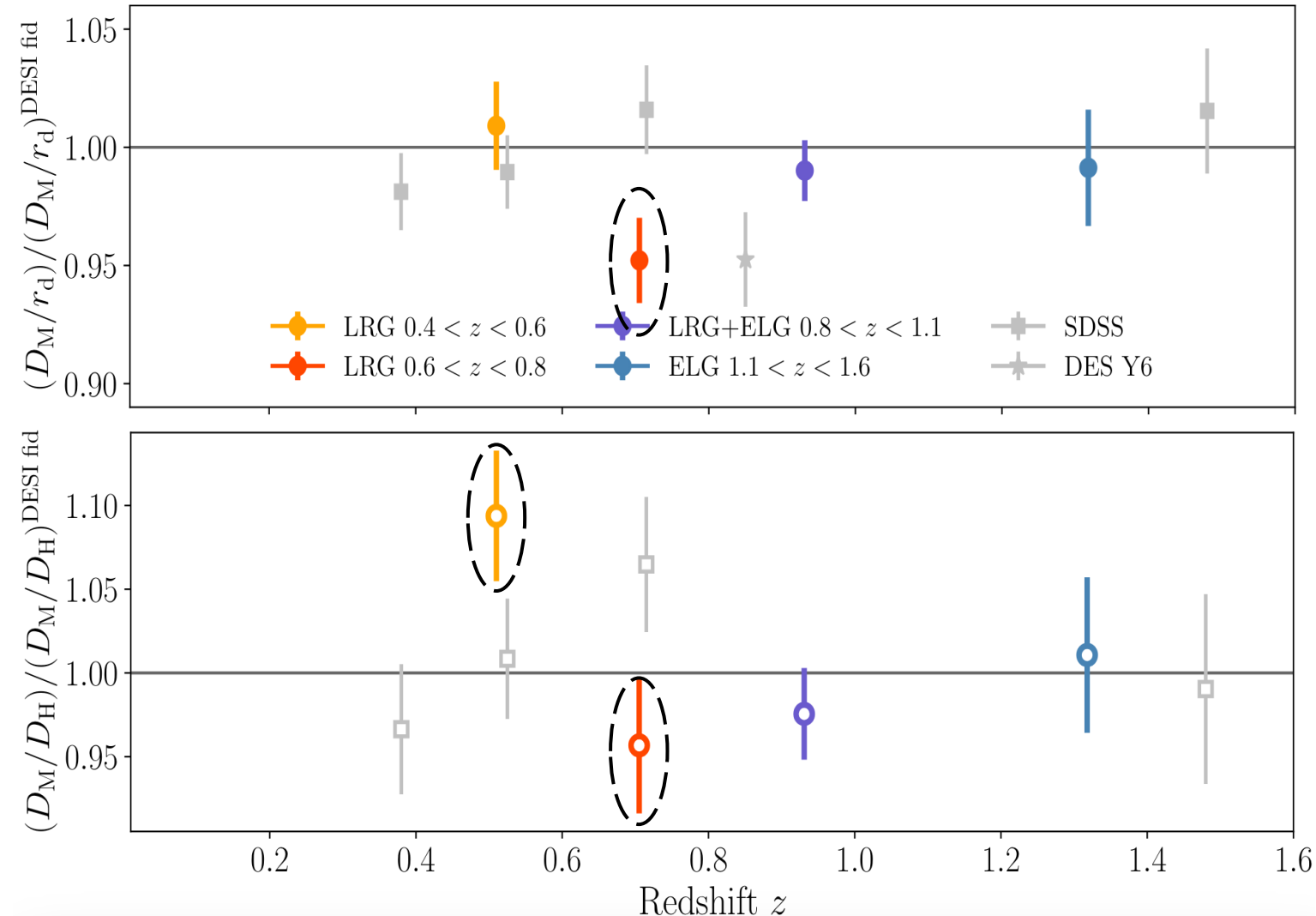


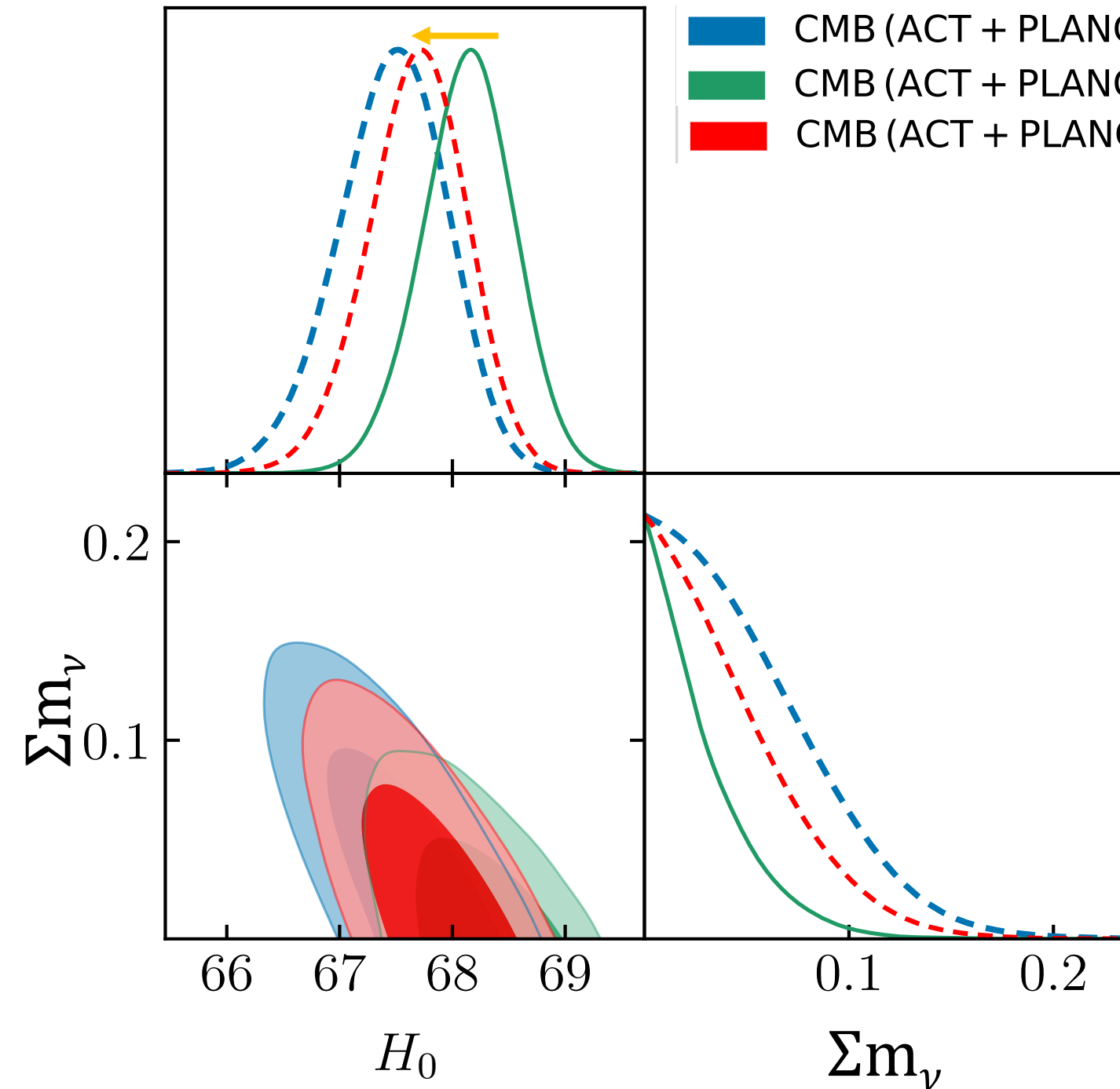
# BAO-2 Dataset

(1) SDSS:  $z=0.15, 0.38, 0.51$  (larger effective volume),  $0.6 < z < 0.8$  ( $3\sigma$  deviation)

(2) DESI: LRGs & ELGs in  $0.8 < z < 1.1$ , ELGs and QSOs at higher  $z$

(3) Combined DESI+SDSS for Ly $\alpha$  BAO





$$\Sigma m_\nu < 0.121 \text{ eV}$$

$$\Sigma m_\nu < 0.075 \text{ eV}$$

$$\Sigma m_\nu < 0.104 \text{ eV}$$

$$H_0 = 67.45 \pm 0.48$$

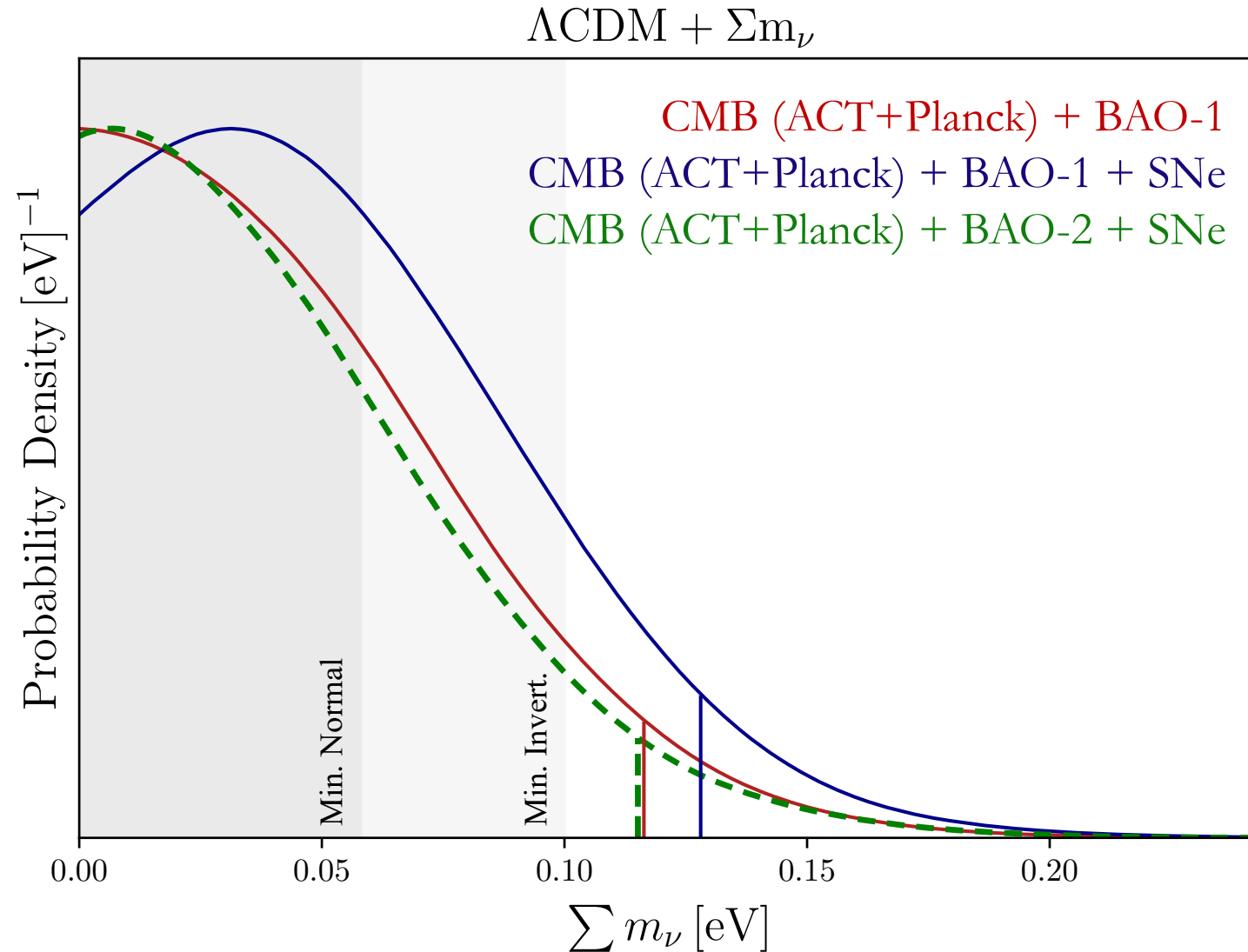
$$H_0 = 68.14 \pm 0.41$$

$$H_0 = 67.77 \pm 0.44$$



# $\Lambda$ CDM + $\Sigma m_\nu$

See also: Allali & Notari, 2024  
arXiv: 2406.14554



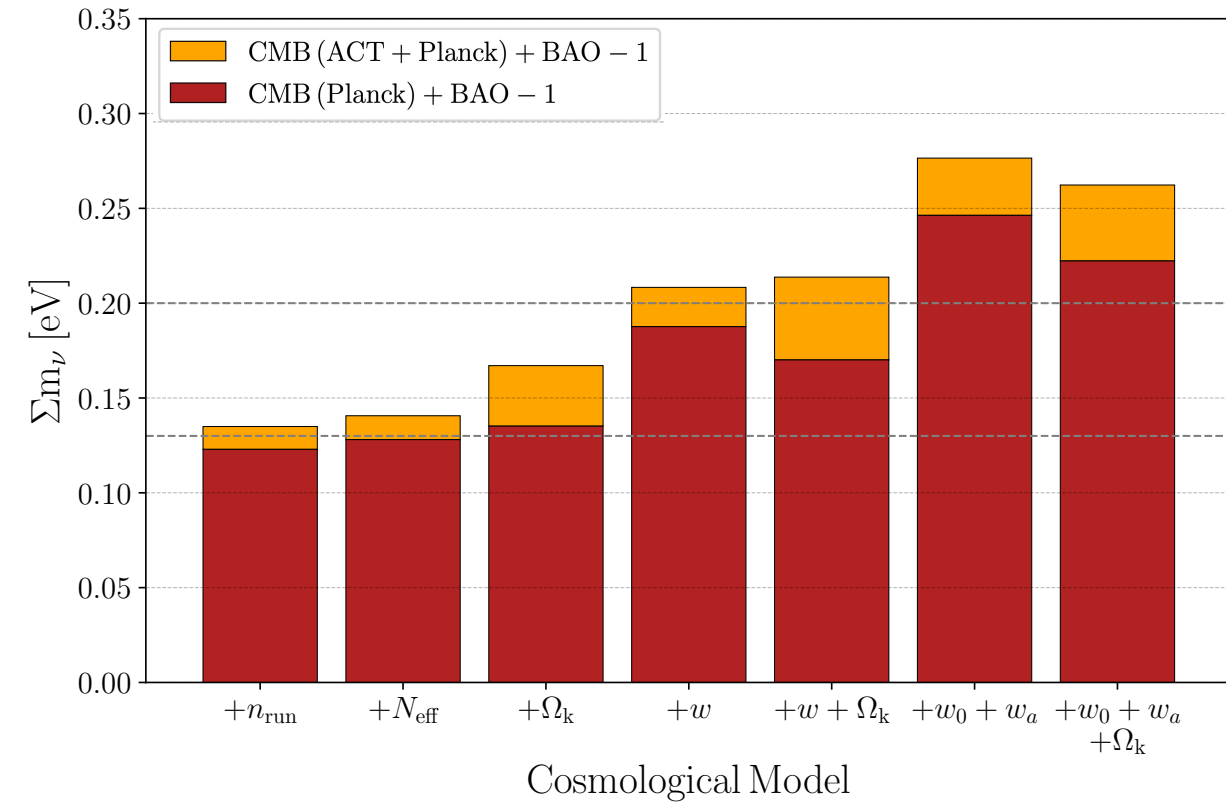
Vertical lines indicate  
 $2\sigma$  bounds

$$\Sigma m_\nu < 0.121 \text{ eV}$$

$$\Sigma m_\nu < 0.129 \text{ eV}$$

$$\Sigma m_\nu < 0.116 \text{ eV}$$

# $\Sigma m_\nu$ Bounds in Extended Cosmologies

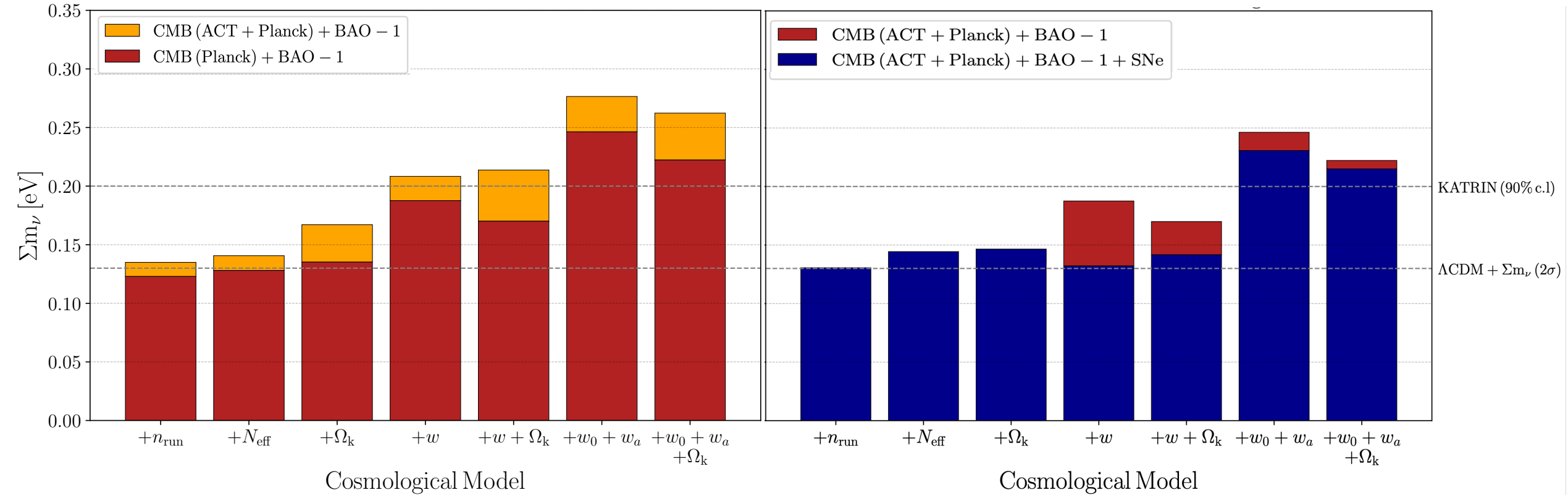


“CMB” – CMB temperature and polarization anisotropies

“Planck” – Planck PR4 lensing

“ACT + Planck” – Planck PR4 + ACT DR6 lensing

# $\Sigma m_\nu$ Bounds in Extended Cosmologies

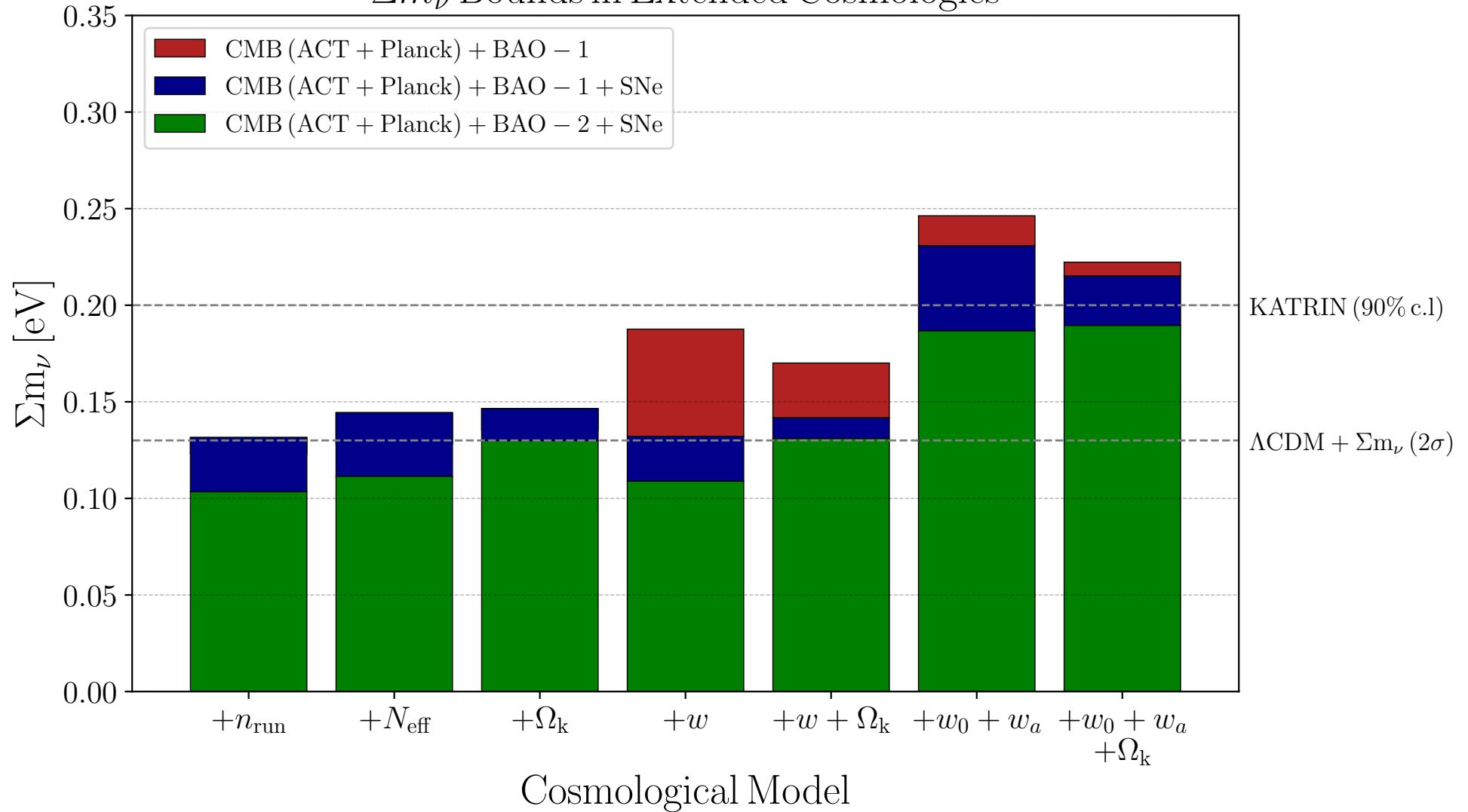


“CMB” – CMB temperature and polarization anisotropies

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# $\Sigma m_\nu$ Bounds in Extended Cosmologies

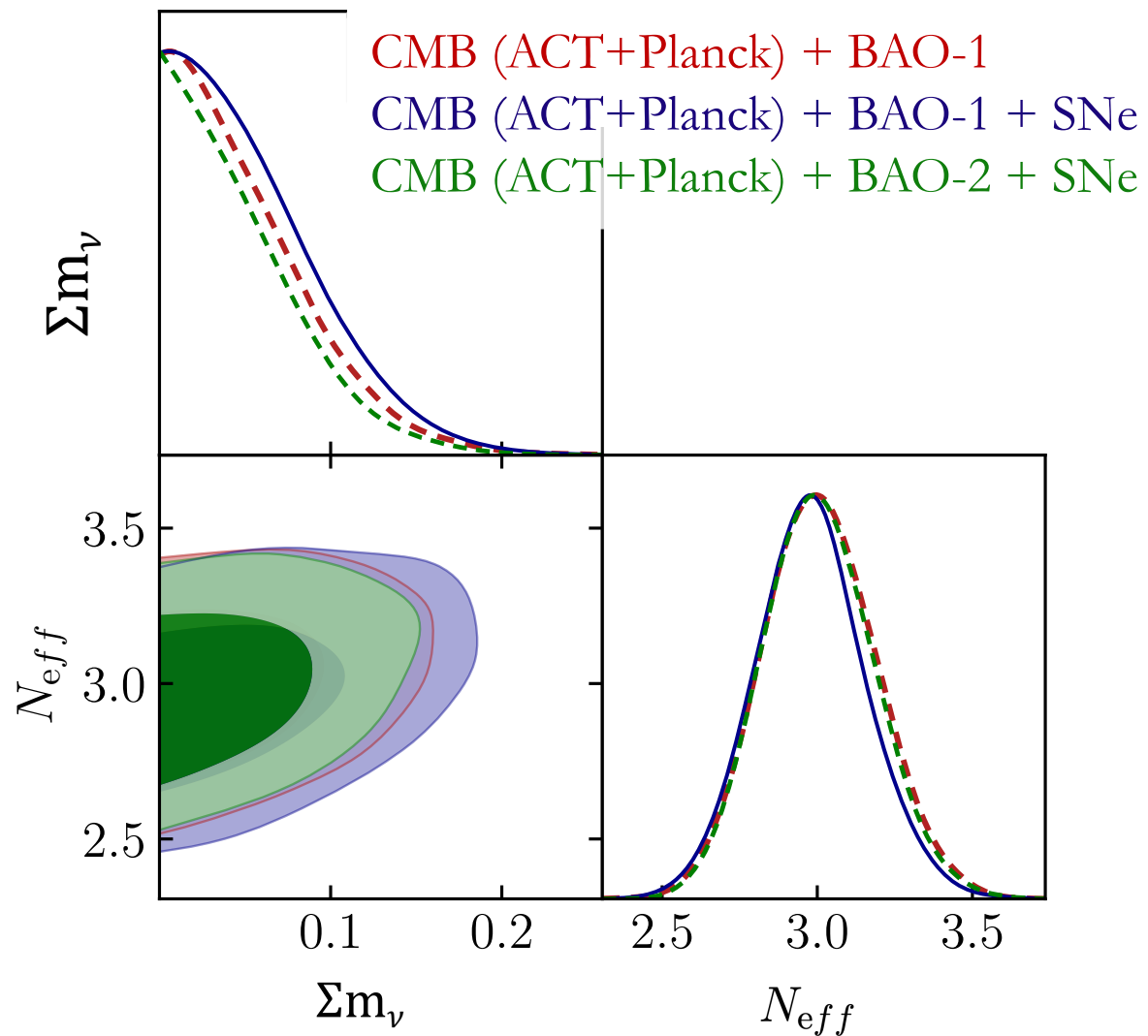


“CMB” – CMB temperature and polarization anisotropies

“BAO-1” – SDSS only

“BAO-2” – SDSS + DESI

# $\Lambda$ CDM + $N_{\text{eff}}$ + $\Sigma m_\nu$



Radiation energy density

Number of effective relativistic species

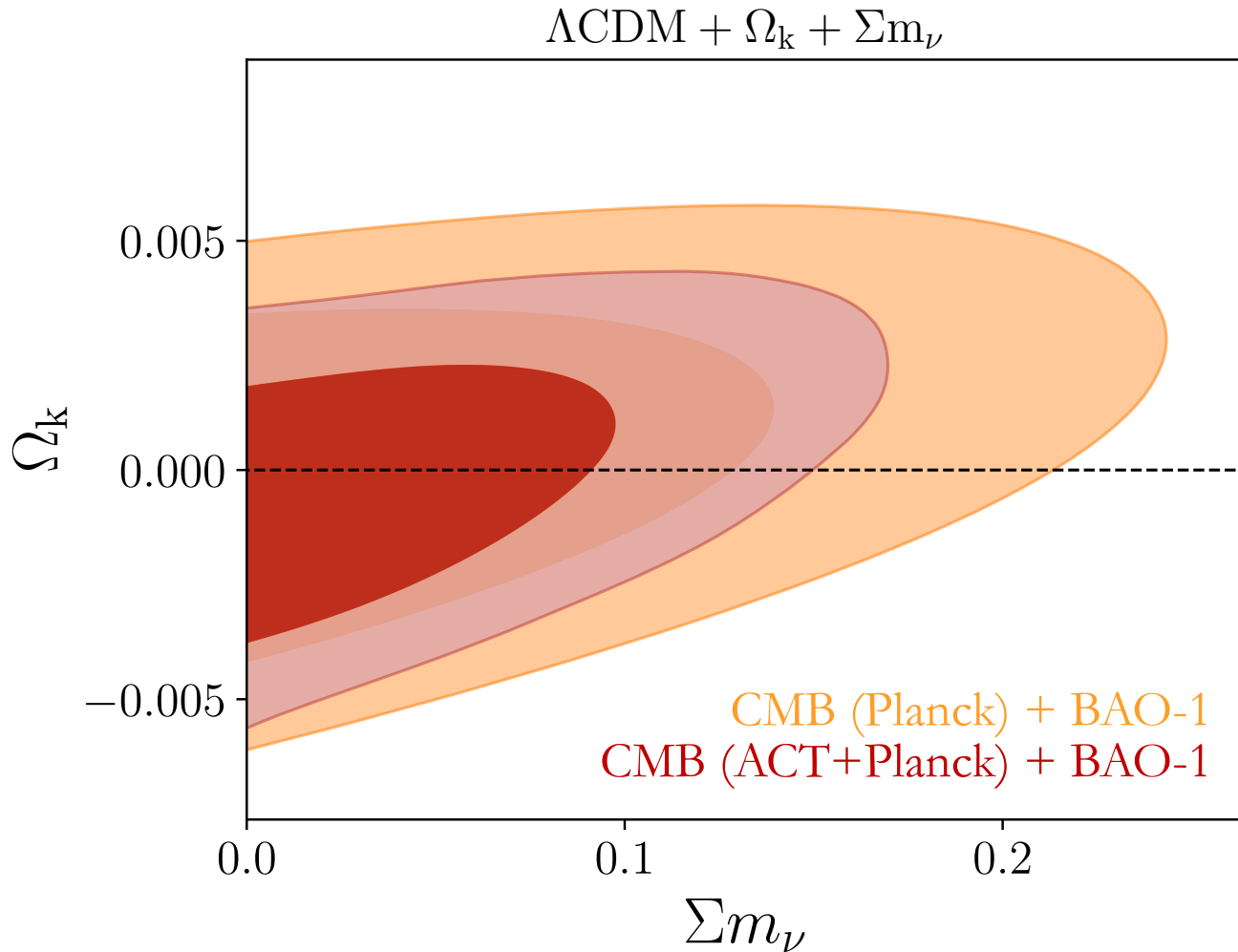
$$\rho_{\gamma+\nu} = \rho_\gamma \left[ 1 + \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} N_{\text{eff}} \right]$$

$$\Sigma m_\nu < 0.14 \text{ eV}$$

$$\Sigma m_\nu < 0.13 \text{ eV}$$

$$\Sigma m_\nu < 0.12 \text{ eV}$$

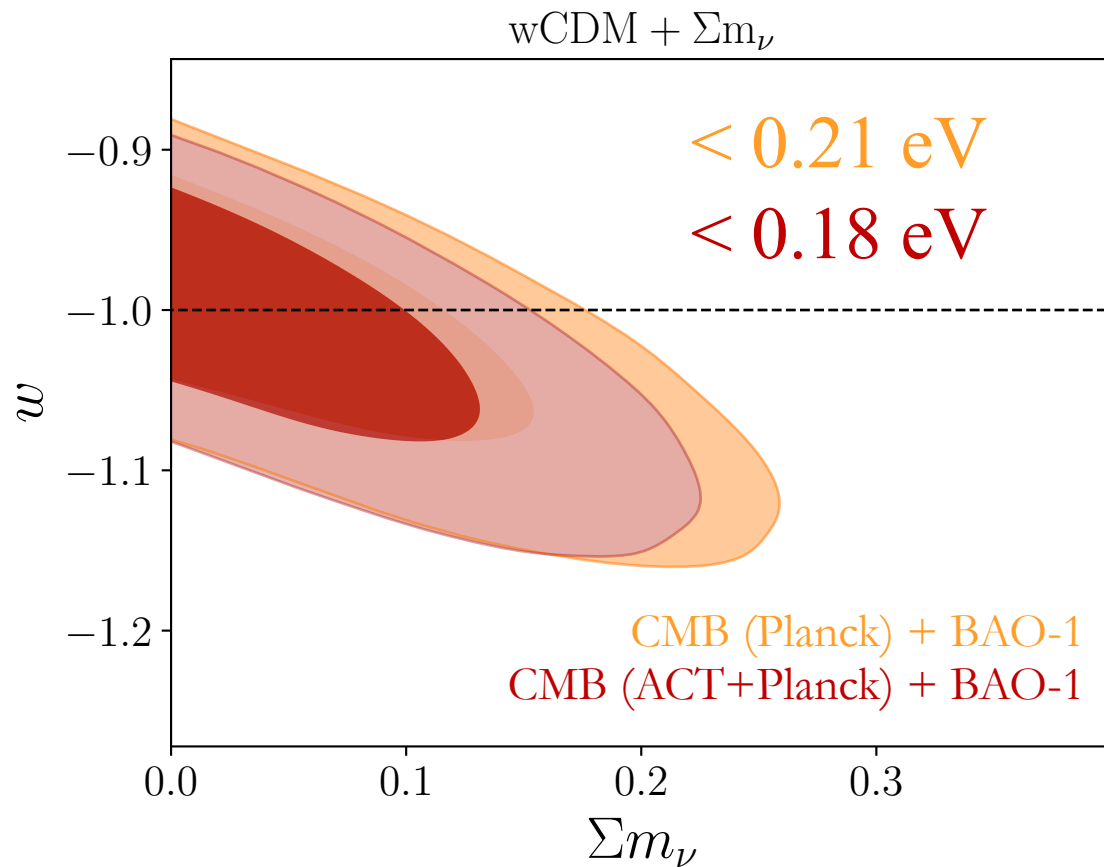
# $\Lambda$ CDM + $\Omega_k$ + $\Sigma m_\nu$



Dataset	$\Sigma m_\nu$ (95% c.l.)
CMB (Planck) + BAO-1	< 0.17 eV
CMB (Planck) + BAO-1 + SNe	< 0.13 eV
CMB (ACT+Planck) + BAO-1	< 0.13 eV
CMB (ACT+Planck) + BAO-1 + SNe	< 0.14 eV
CMB (ACT+Planck) + BAO-2 + SNe	< 0.13 eV

# wCDM + $\Sigma m_\nu$

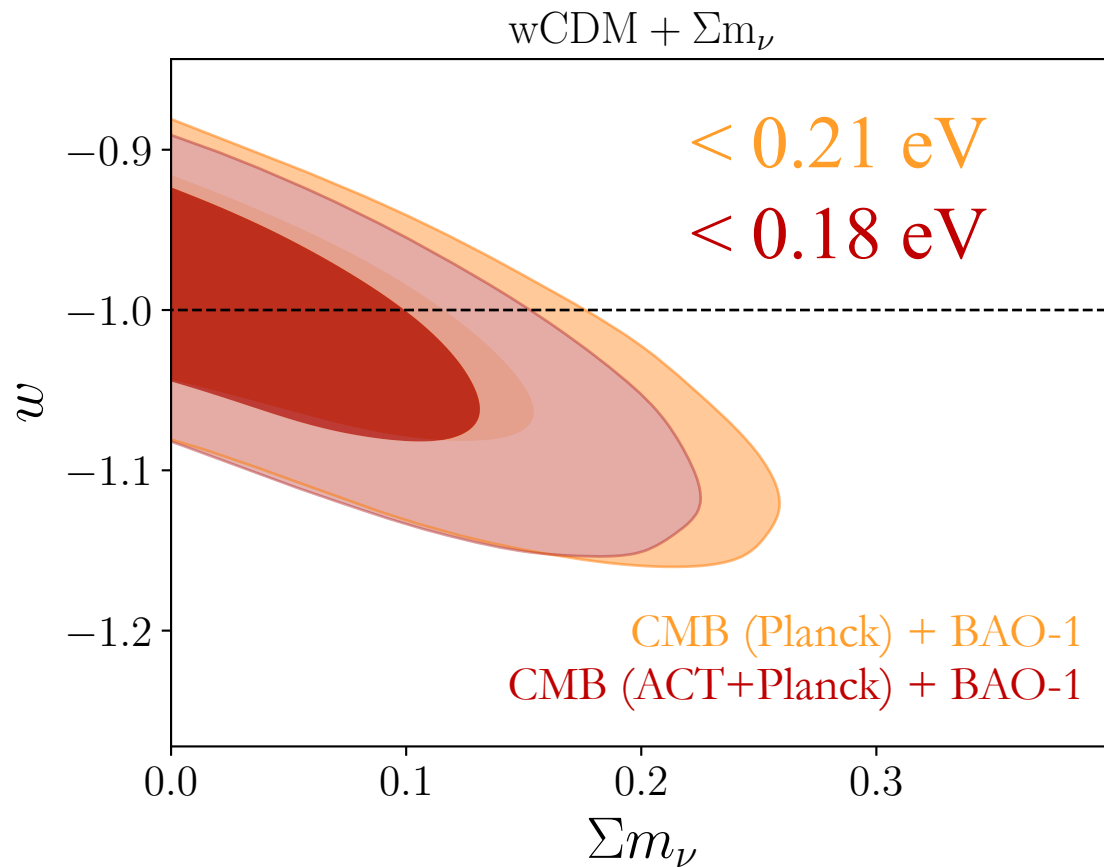
$$\rho_{\text{DE}}(z) = w * p(z)$$



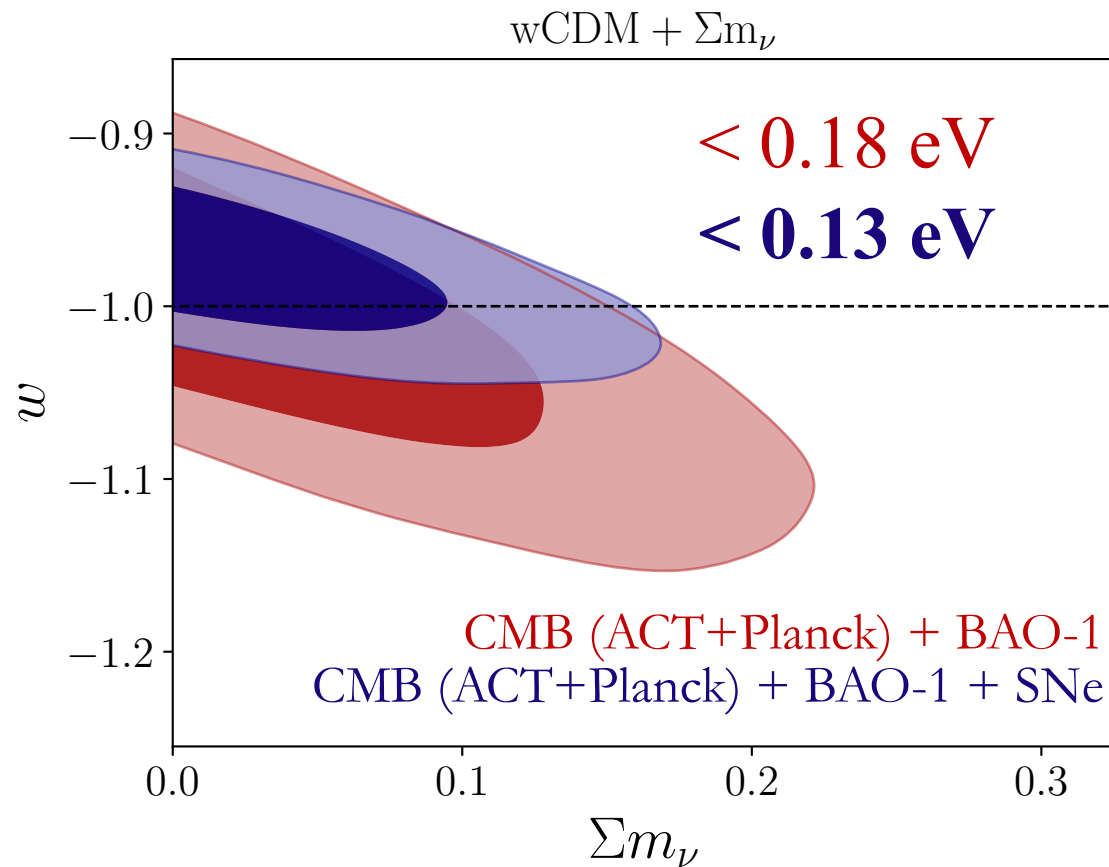
ACT Lensing rejects larger  $\Sigma m_\nu$  values

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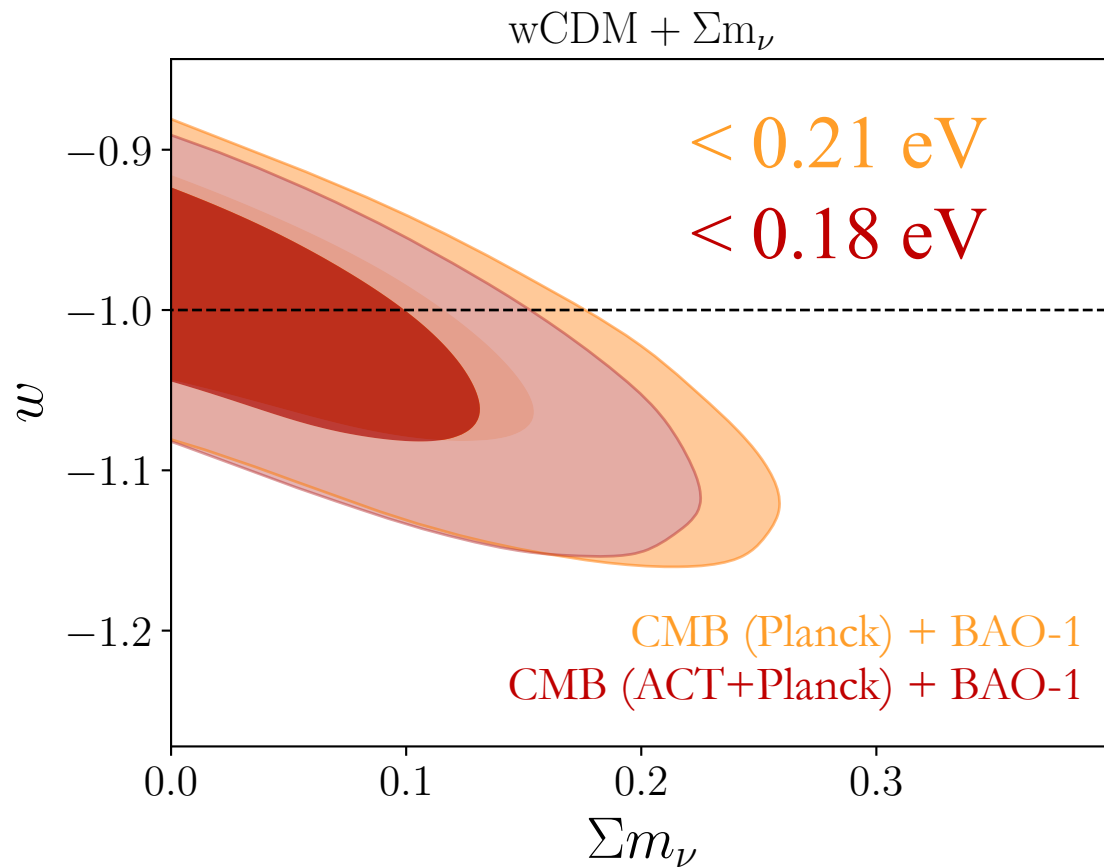


SNe data significantly reduces degeneracy

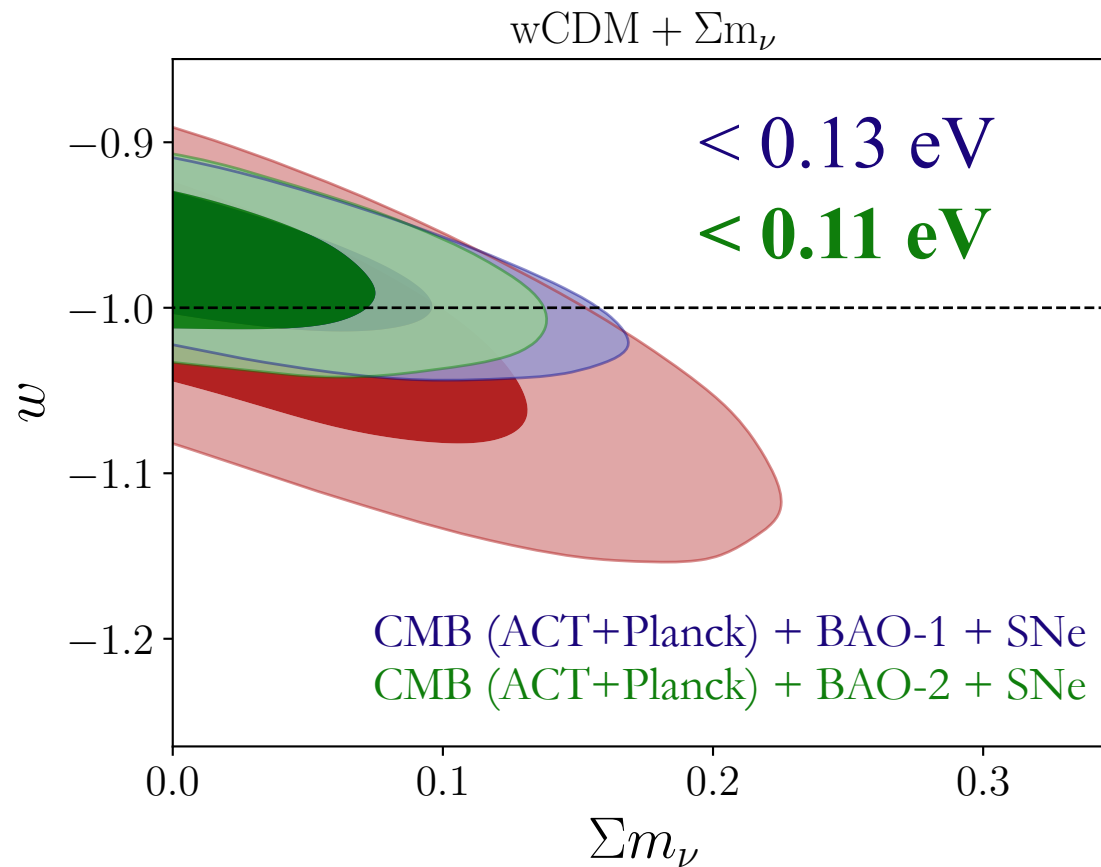


# wCDM + $\Sigma m_\nu$

$$\rho_{\text{DE}}(z) = w * p(z)$$

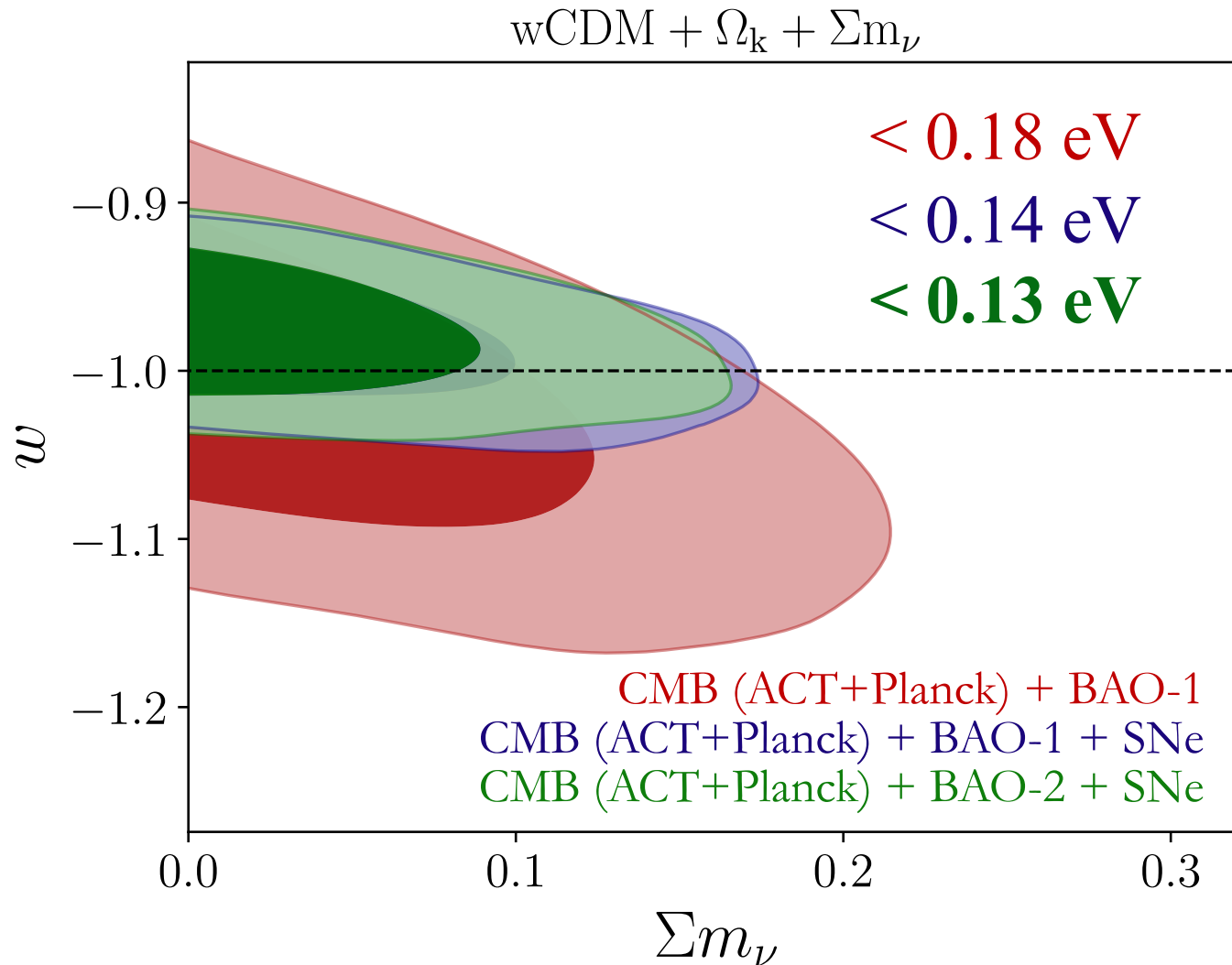


ACT Lensing rejects larger  $\Sigma m_\nu$  values



DESI data rejects larger  $\Sigma m_\nu$

# wCDM + $\Omega_k$ + $\Sigma m_\nu$

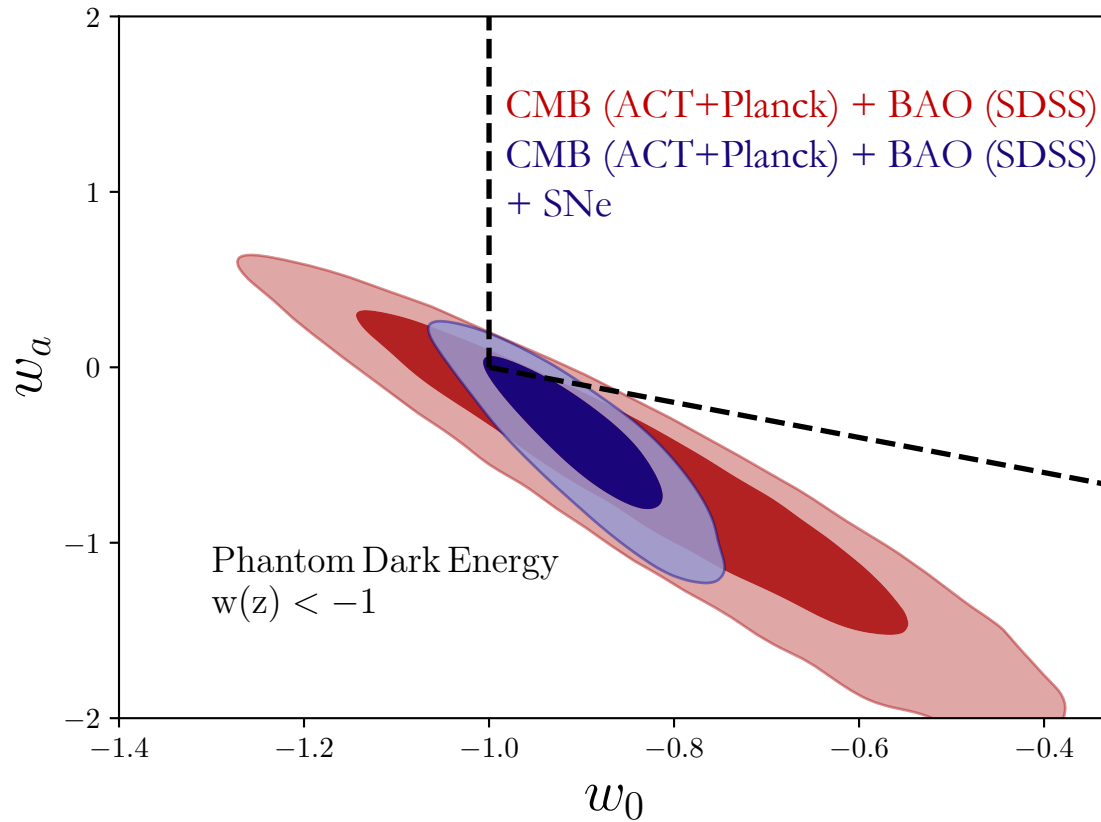


Adding curvature to previous model marginally weakens  $\Sigma m_\nu$  bounds

# $w_0 w_a$ CDM + $\Sigma m_\nu$

CPL Parameterization

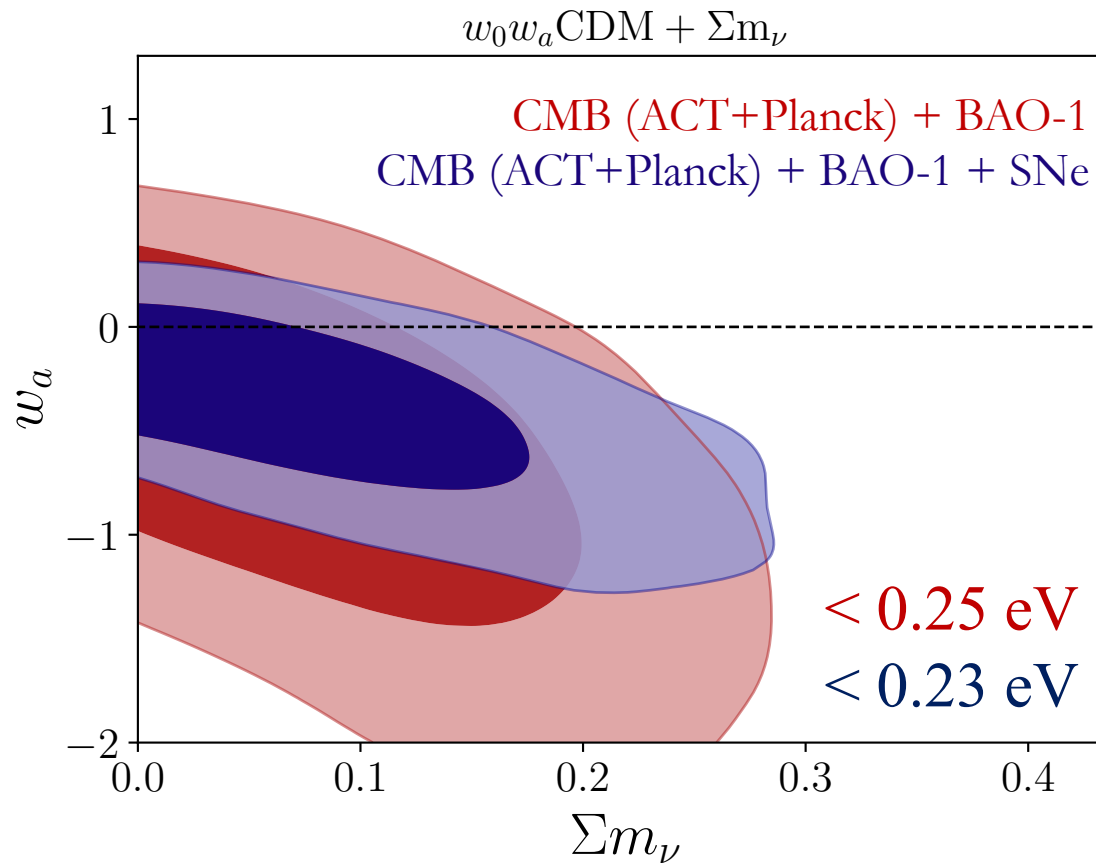
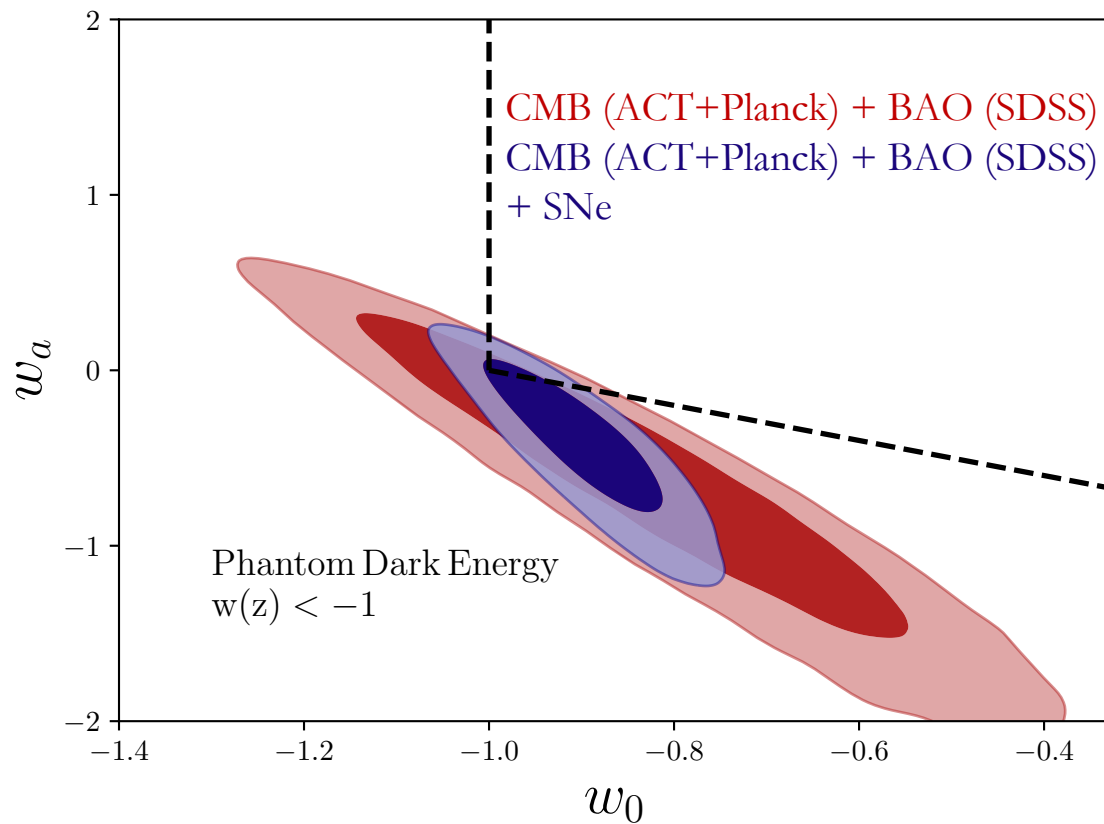
$$w(z) = w_0 + w_a(1 - a) = w_0 + w_a \frac{z}{1+z}$$



# $w_0 w_a$ CDM + $\Sigma m_\nu$

CPL Parameterization

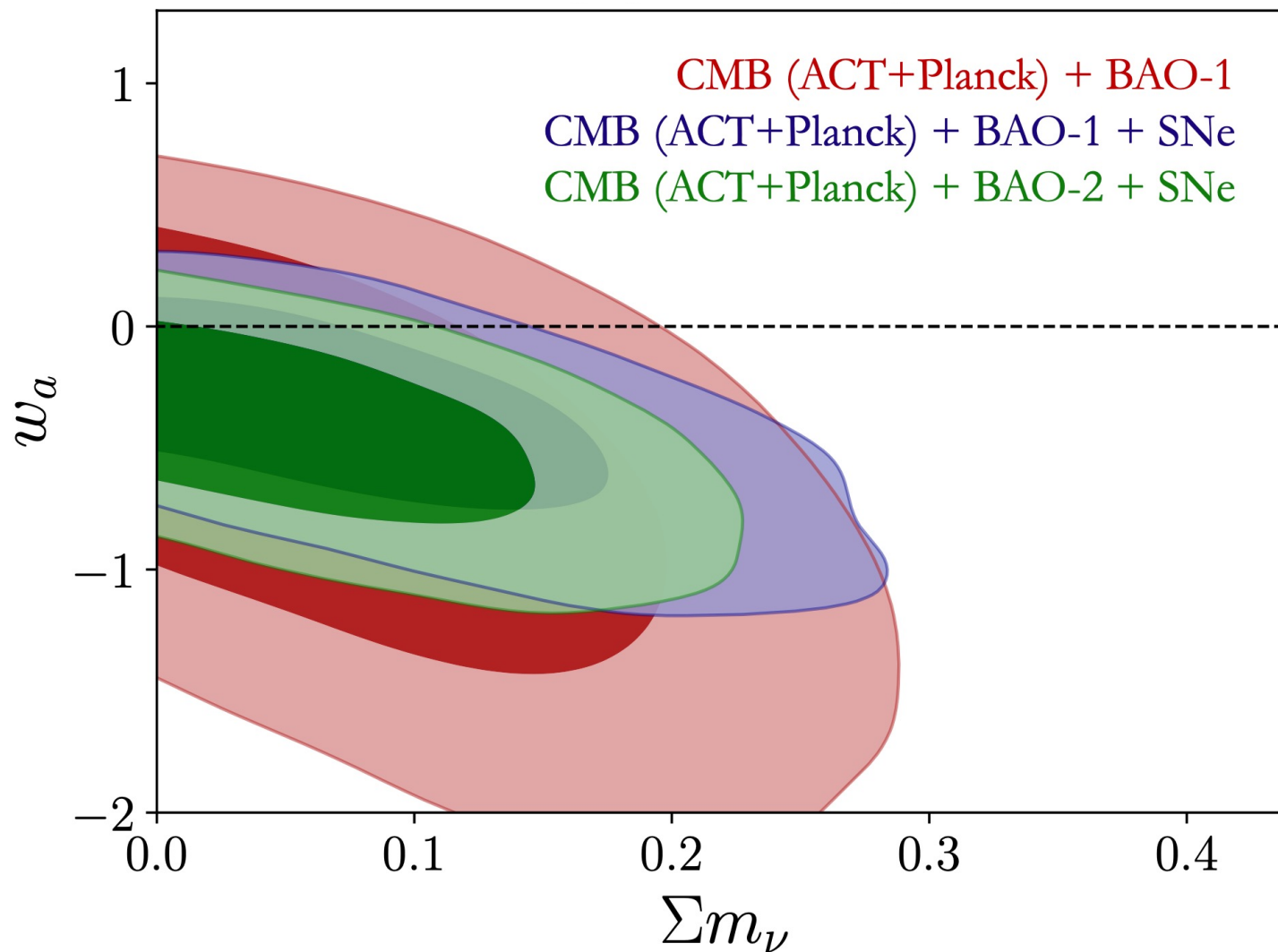
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CPL Parameterization

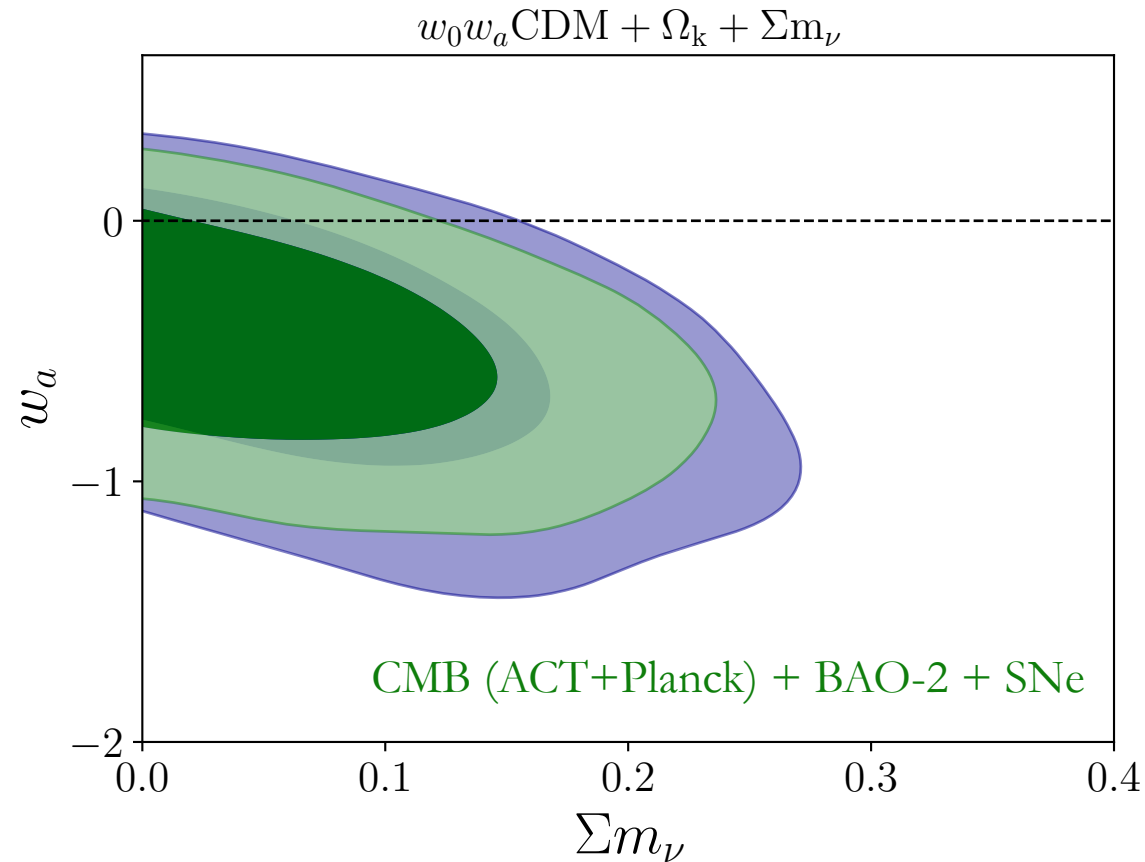
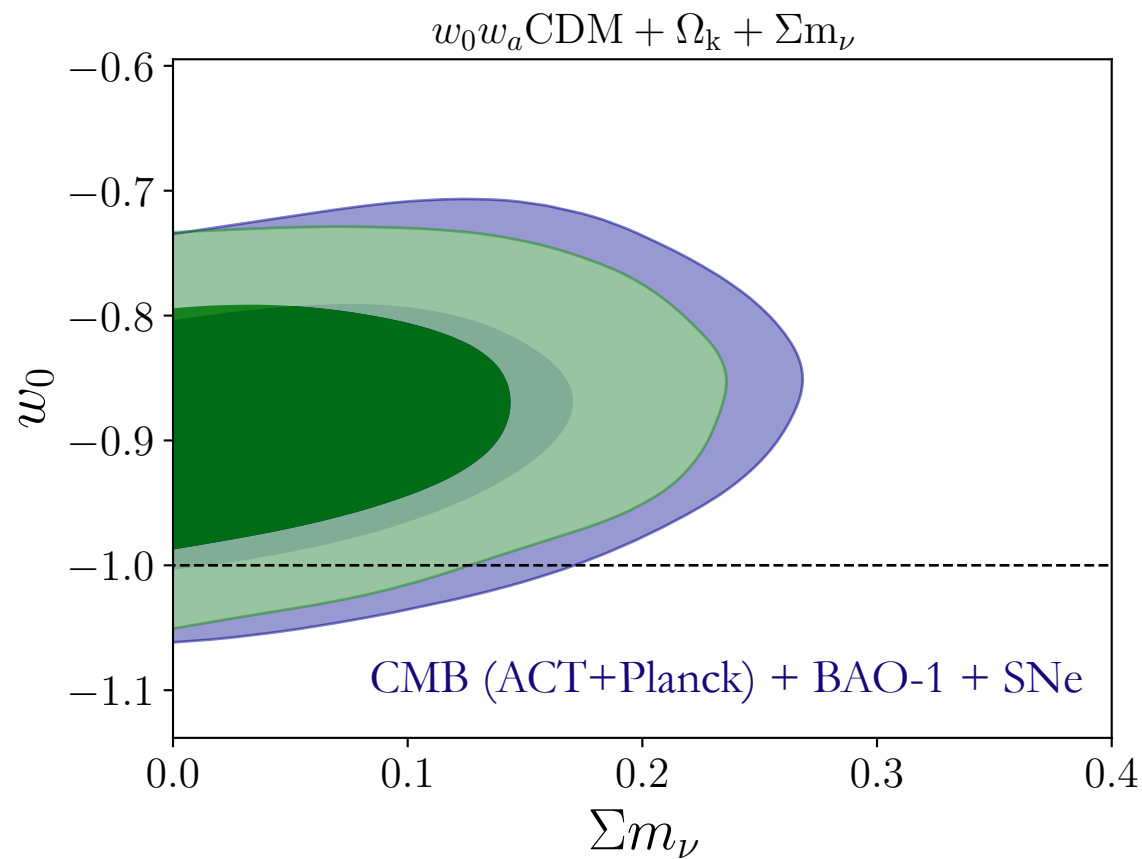
$$w(z) = w_0 + w_a(1 - a) = w_0 + w_a \frac{z}{1+z}$$



$< 0.23$  eV

$< 0.19$  eV

# $w_0 w_a \text{CDM} + \Omega_k + \Sigma m_\nu$



$< 0.23 \text{ eV} \rightarrow < 0.19 \text{ eV}$

# Conclusions

- $\Sigma m_\nu$  bound **remains robust** to:
  - Dark energy ( $w$ )
  - Phantom DE
  - Time-dependent DE  $w(z; w_0, w_a)$
  - Curvature

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- **DESI+SDSS**: Inverted hierarchy still viable in  $\Lambda$ CDM
- **Future**: DESI full-shape, Euclid, SO, LiteBIRD, ...