Supernova gravitational waves and protoneutron star asteroseismology

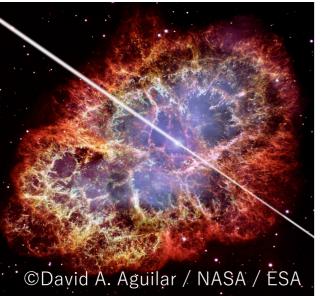
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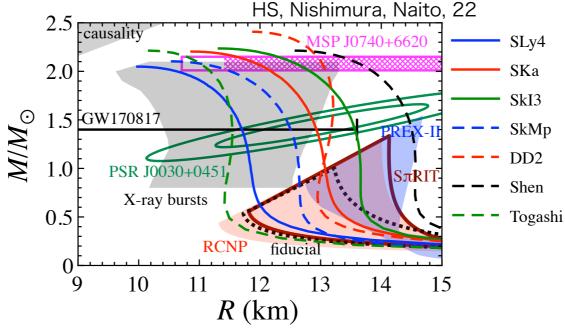
Bernhard Mueller (Monash Uni.) & Tomoya Takiwaki (NAOJ)

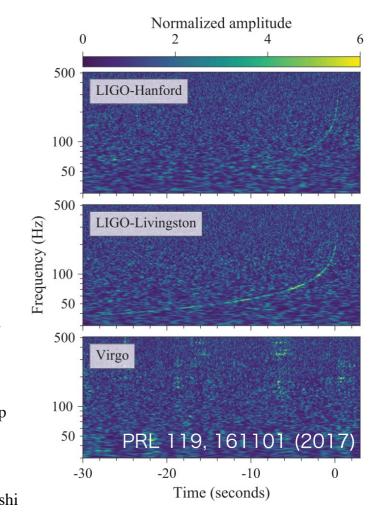
Phys. Rev. D 109, 123021 (2024)

Dawn of GW astronomy

- GWs from compact binary mergers have been detected.
 - GWs become a new tool for extracting astronomical information.
- The next candidate must be a supernova explosion.
 - GW asteroseismology





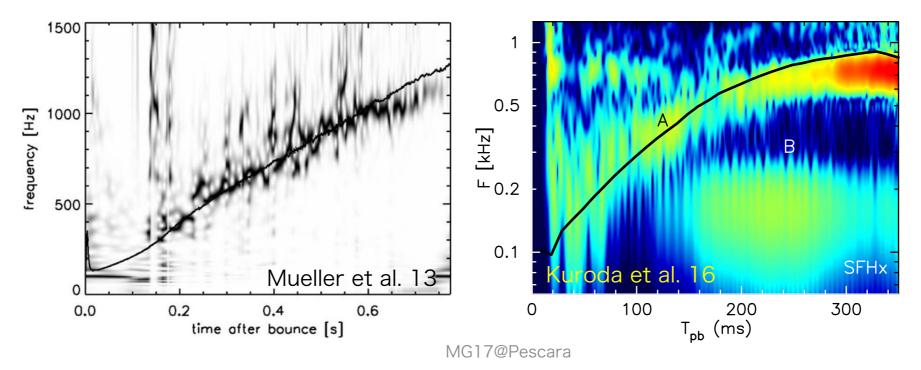


Next candidate of GW sources

core-collapse supernovae

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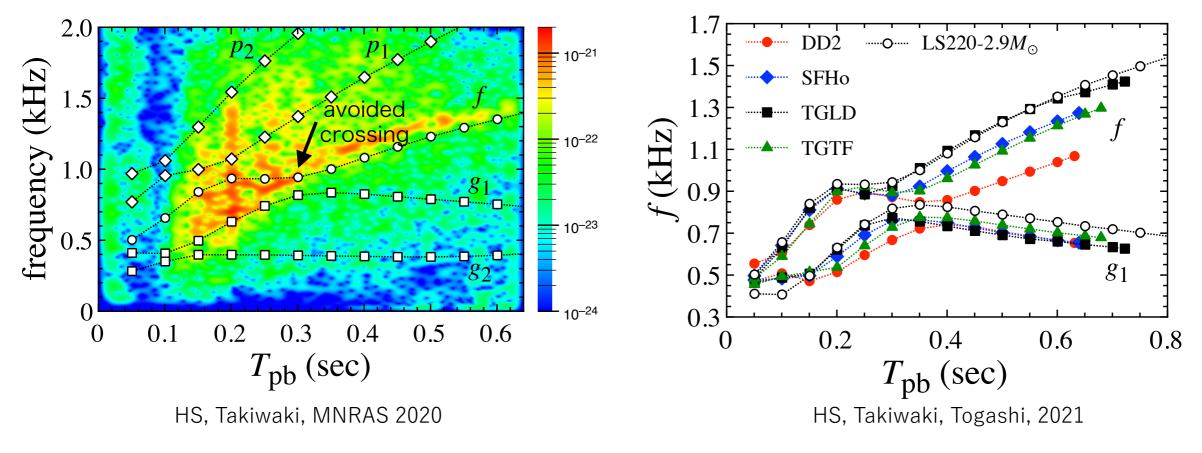
- compared to the binary merger, the system is almost spherically symmetric
 - less energy of gravitational waves
- many numerical simulations show the existence of GW signals
- SN GWs depend on the SN models, such as progenitor mass and EOS
 - how to extract the astronomical information from the GW observations?
 - what is the origin of the SN GWs?



Comparison with GW signals

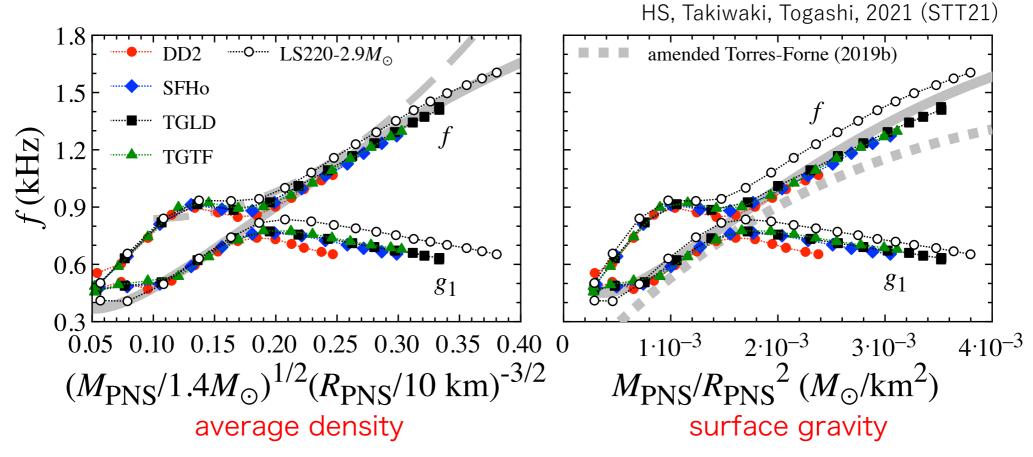
- GW signals correspond to g_1 -mode in an early phase and f-mode after avoided crossing.

• time evolution of frequencies strongly depends on supernova models

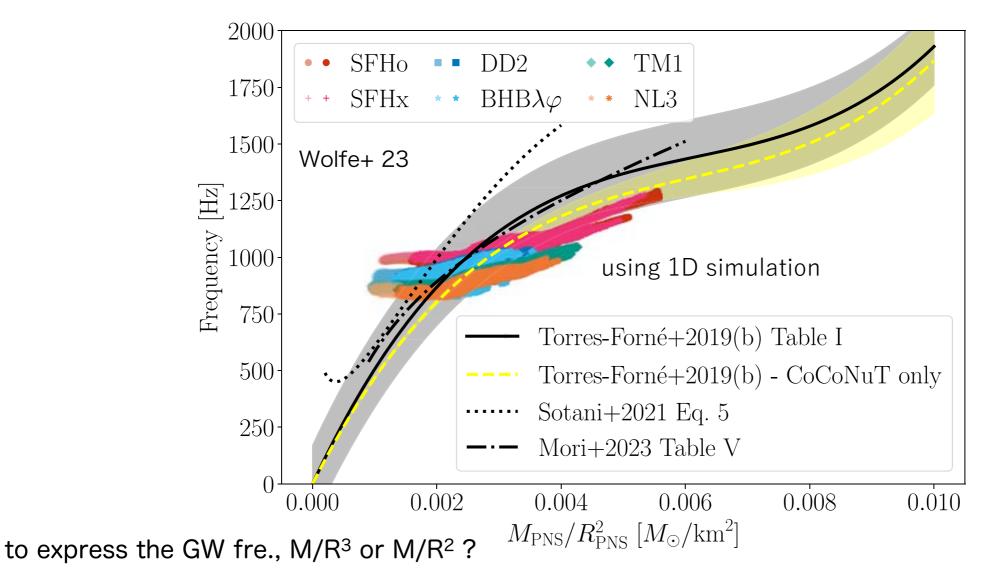


Universal relations

- The g_1 and f-mode frequencies can be well expressed as a PNS properties
 - average density seems to be more suitable than surface gravity

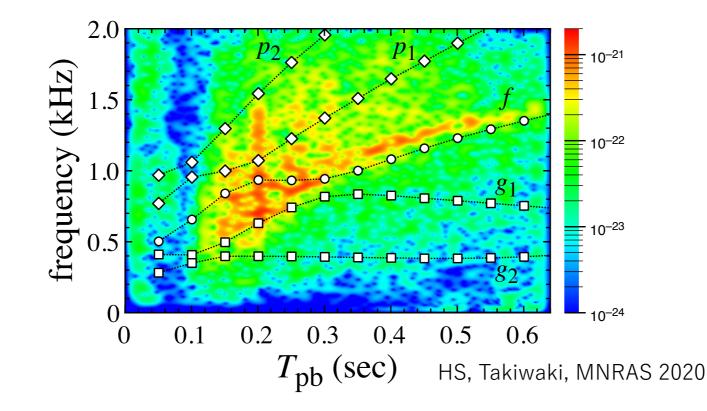


Comparison of universal relations



What we want to confirm

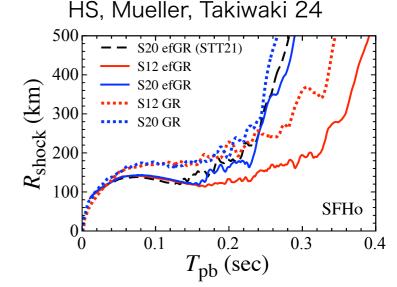
- Which is better to express the supernova gravitational waves, M/R^3 or M/R^2?
- The gravitational wave spectra in the simulation deviate from the PNS oscillation frequency.



Average density or Surface gravity

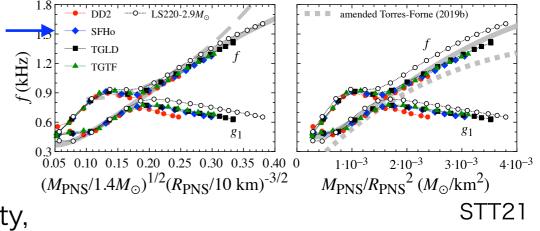
- Supernova models
 - SFHo EOS
 - S12 & S20 (Woosley & Heger 07)
- We see how PNS frequencies (corresponding to GW signals in the simulations) depend on

 interpolations in the simulations (2nd or 5th-order) in Newtonian
 - treatment of gravity in the simulations (Newtonian or GR)
- <u>Newtonian simulation</u> with approximate potential (effective GR)
 - 2nd-order interpolation with Harten-Lax-van Leer contact (STT21)
 - 5th-order interpolation with Harten-Lax-van Leer discontinuities
- <u>Relativistic simulations</u> (GR)
 - conformal flatness approximation

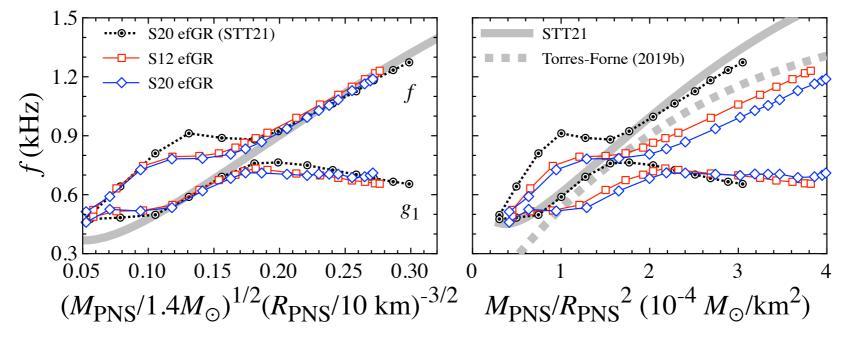


universal relations in effective GR

 the sequence of the GW signals from the g₁- to f-modes is well expressed with the empirical relation as a function of the root square of the average density, even if the interpolation in the simulations is different.



• Meanwhile, those frequencies seem to depend on the interpolation in the simulations if one considers the function of the surface gravity.



universal relations in GR

- The sequence from the g_1 to f-mode frequencies $(M_{PNS}/1.4M_{\odot})^{1/2}(R_{PNS}/10 \text{ km})^{-3/2}$ are well expressed with the protoneutron star average density, even for the case of GR simulations.
- The dependence of the g₁- and f-modes on the surface gravity with GR simulation are more or less similar to those with effective GR simulations newly done in this study, which deviate from the empirical relation derived in STT21

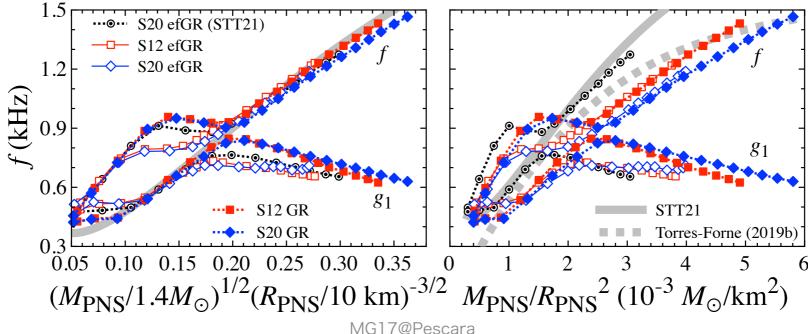
....... LS220-2.9M

0.05 0.10 0.15 0.20 0.25 0.30 0.35 0.40 0

---- TGLD

- TGTF

 $f(\mathbf{KHz}) = 0.9$



12

amended Torres-Forne (2019)

 $2 \cdot 10^{-3}$

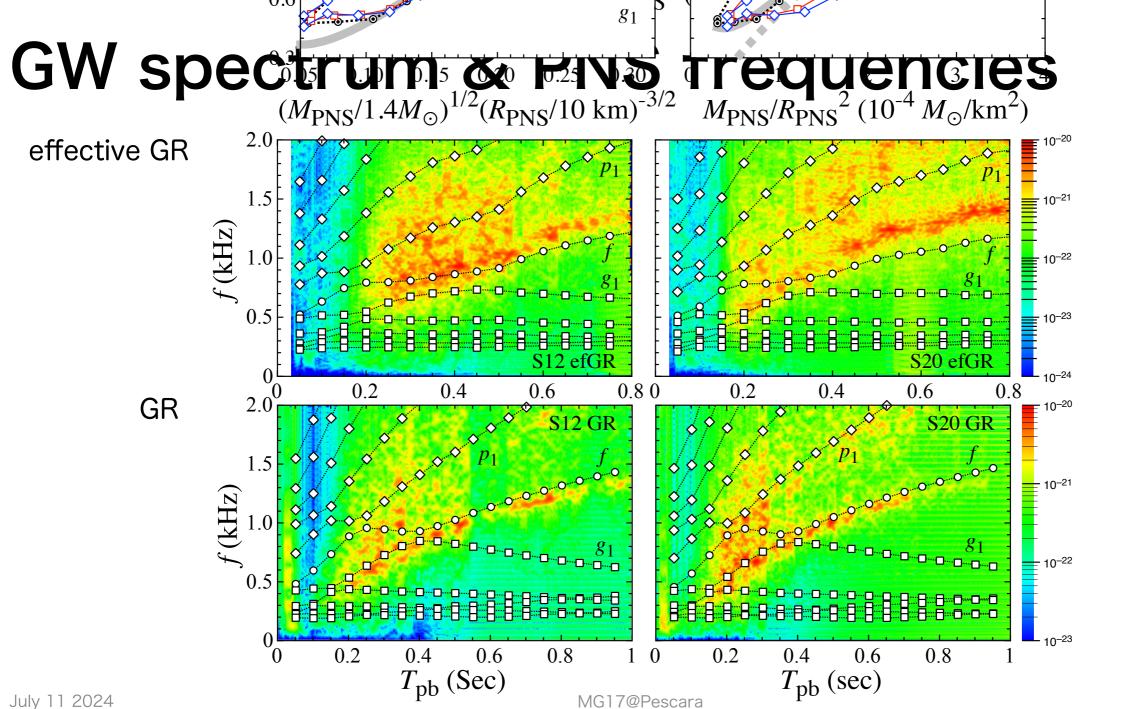
 $M_{\rm PNS}/R_{\rm PNS}^2 (M_{\odot}/{\rm km}^2)$

 $3 \cdot 10^{-3}$

 $4 \cdot 10^{-3}$

STT21

 1.10^{-3}



July 11 2024

Conclusion

- To see how the PNS frequencies (corresponding to the GW signals in the simulations) depend on the difference of the interpolation and/or the treatment of gravity in the simulation, we newly did the simulations with effective GR and GR
 - we did a linear analysis, using the resultant simulation data
- The sequence of GW signals is well expressed as a function of PNS average density, instead of the PNS surface gravity, independently of the supernova models and numerical scheme.
- With the simulation data done in the GR framework, GW spectrum can be well identified with the PNS oscillation frequencies.
- One can extract the PNS average density via the observations of GWs from SN.