

Analyzing right-handed neutrino dark matter with electron recoil events



Seventeenth
Marcel Grossmann
Meeting
2024

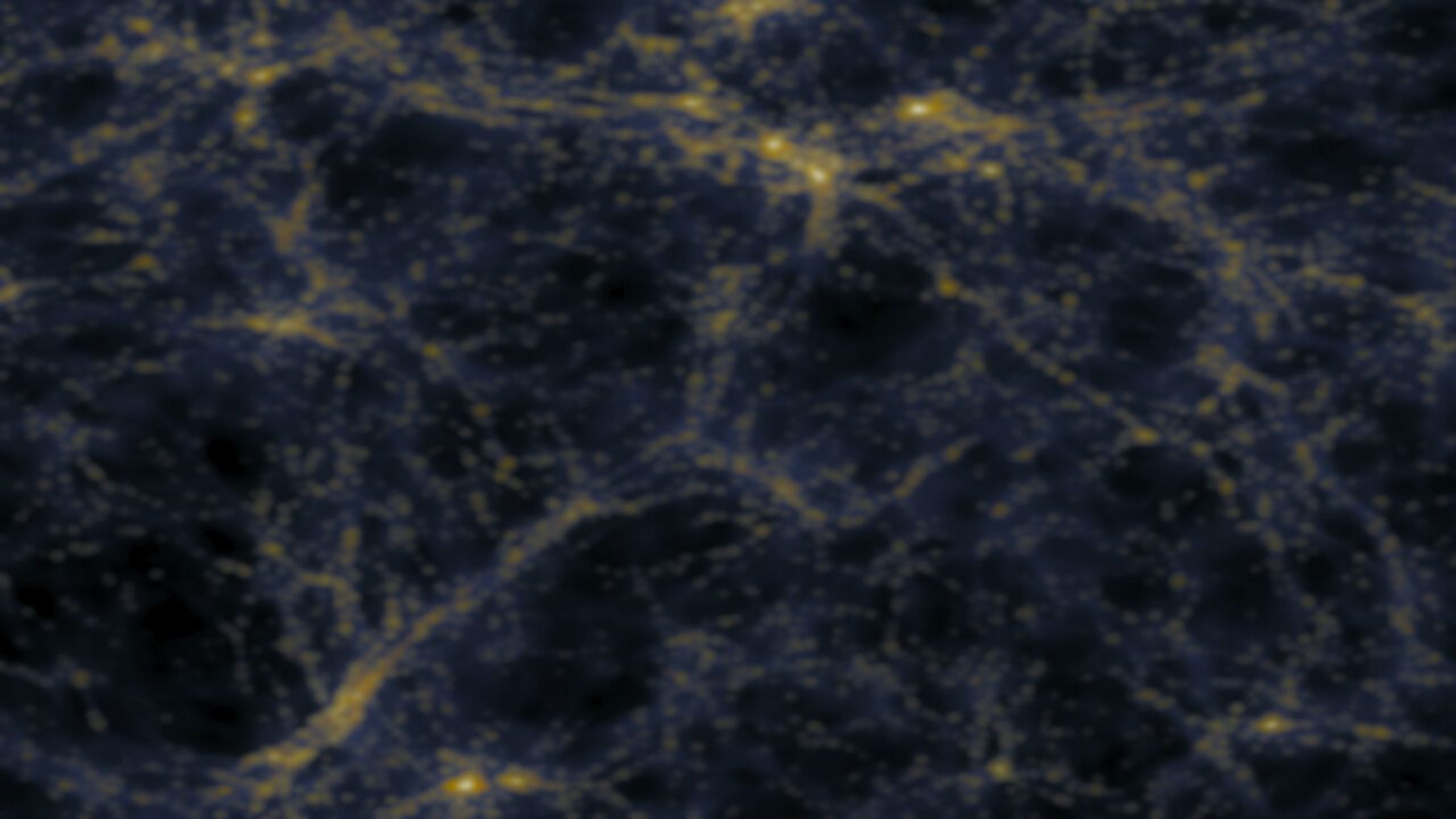
Santiago Collazo^{1 2}

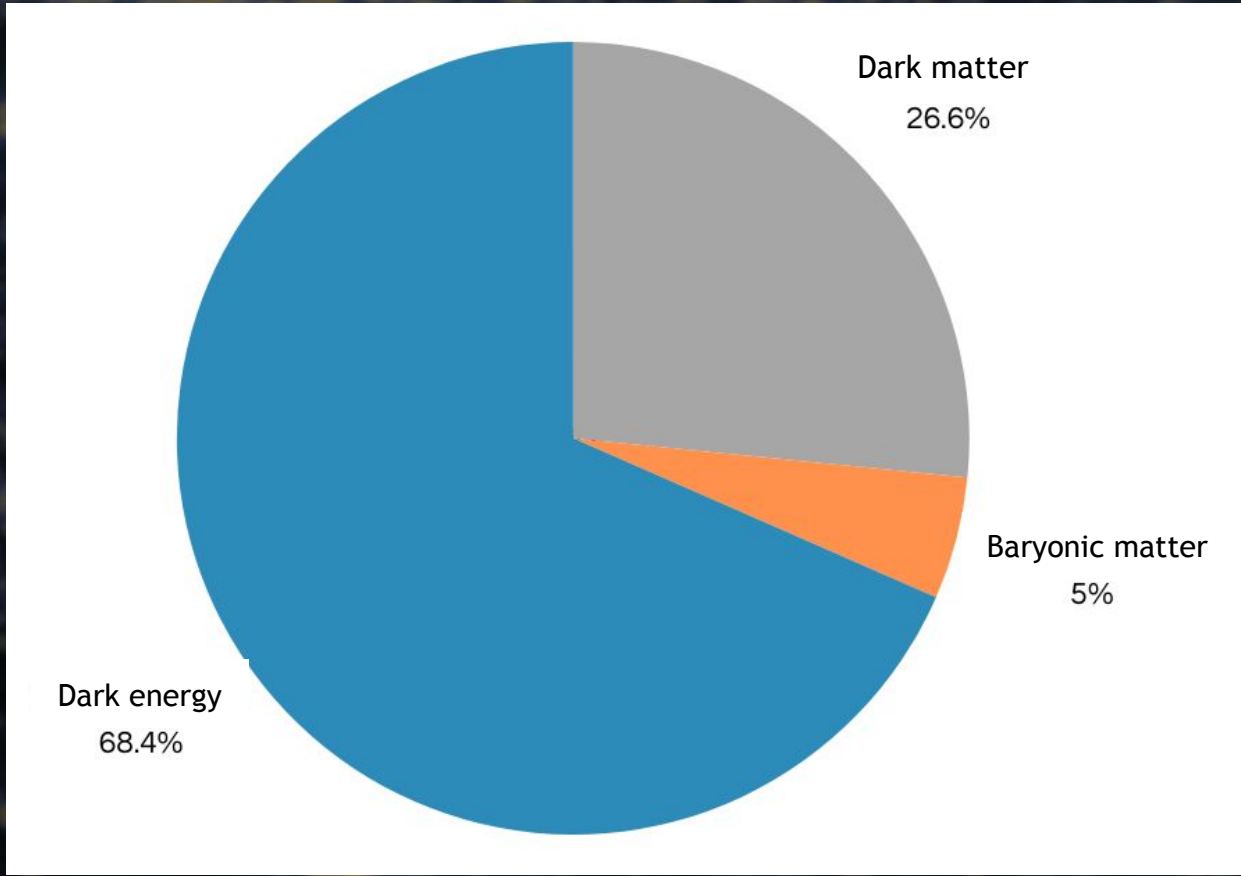


¹ Instituto de Astrofísica de La Plata, CONICET

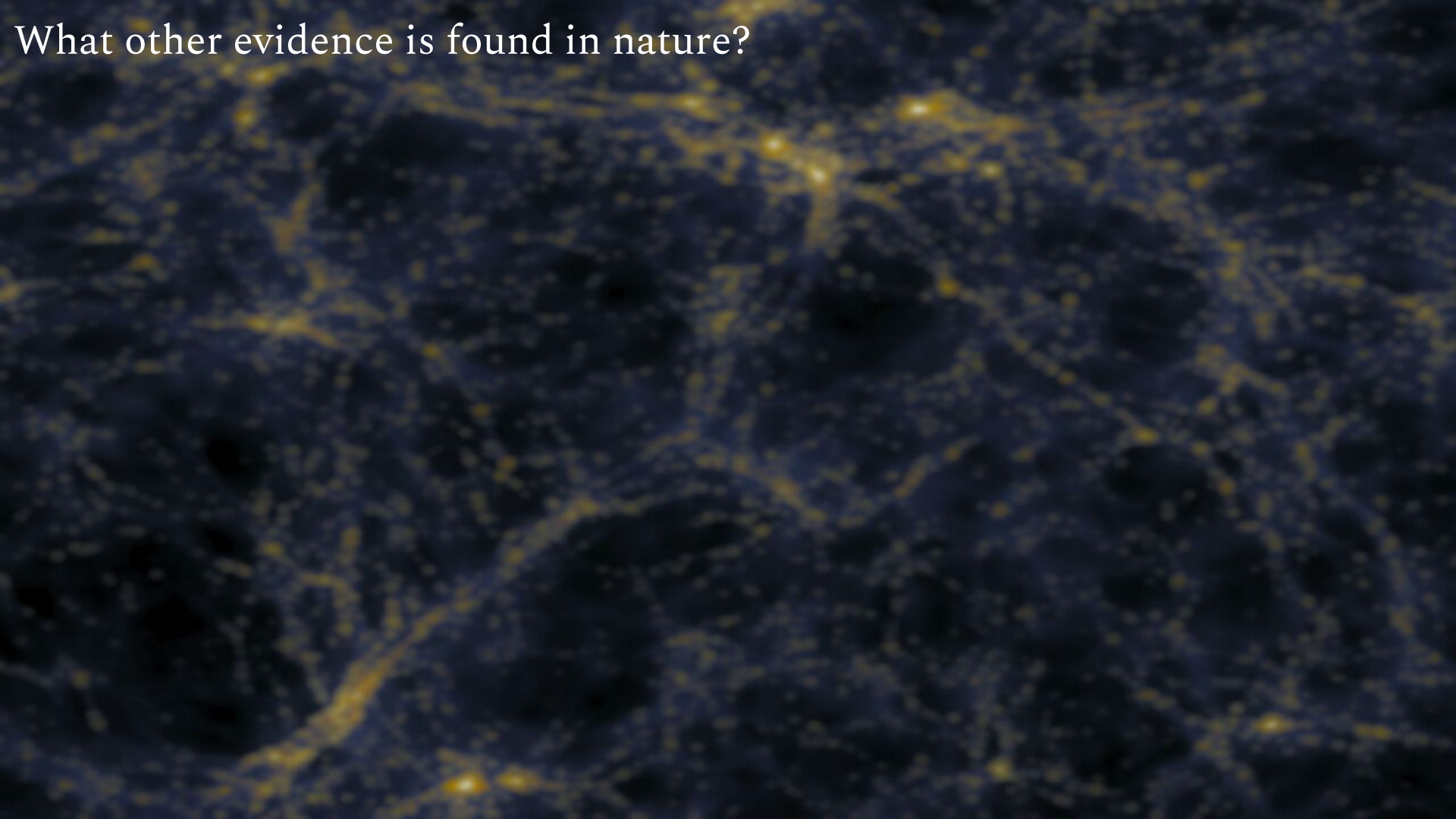
² Facultad de Ciencias Astronómicas y Geofísicas de La Plata, UNLP

Collaborators: Carlos Argüelles,
Soroush Shakeri



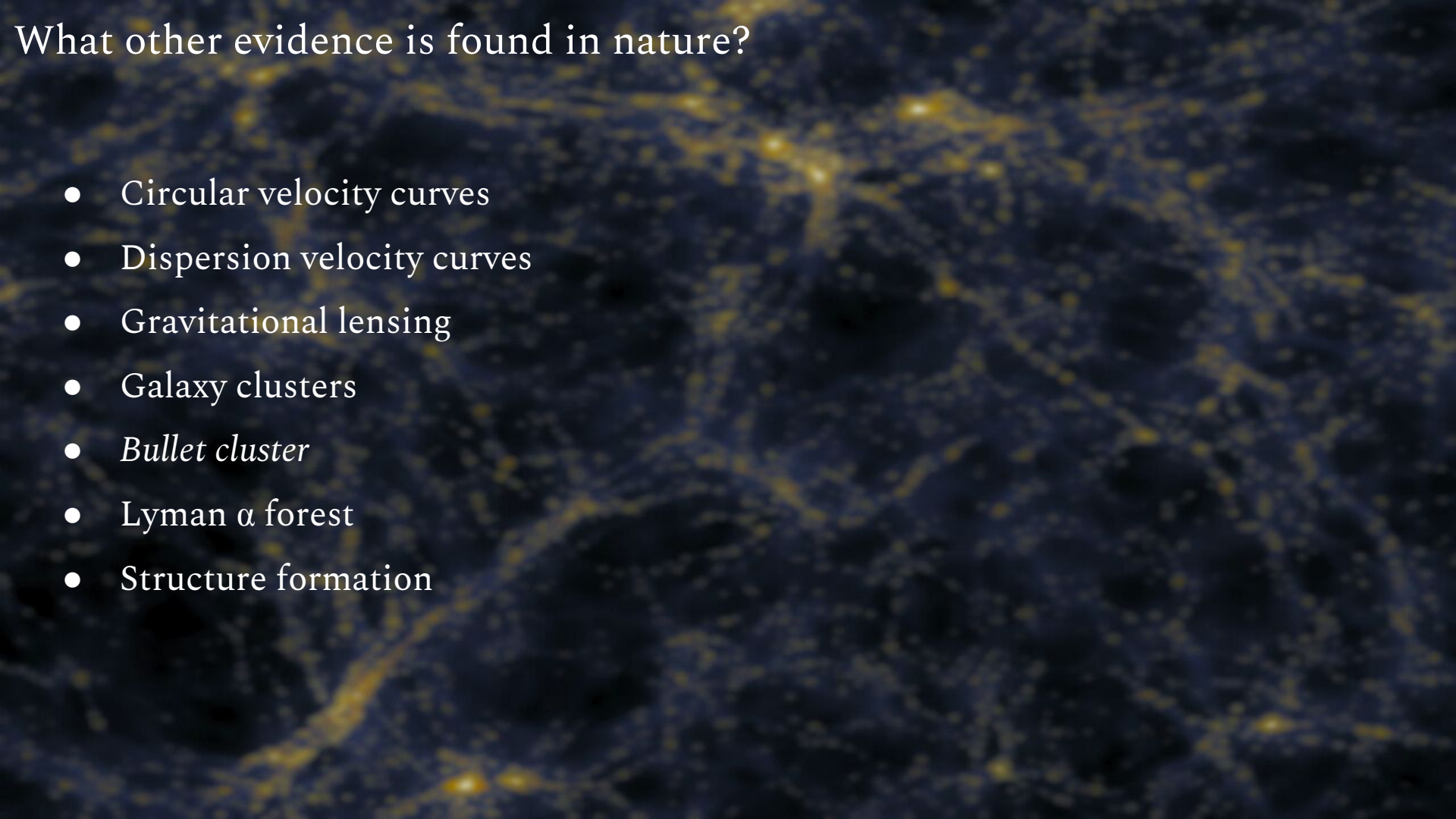


What other evidence is found in nature?



What other evidence is found in nature?

- Circular velocity curves
- Dispersion velocity curves
- Gravitational lensing
- Galaxy clusters
- *Bullet cluster*
- Lyman α forest
- Structure formation

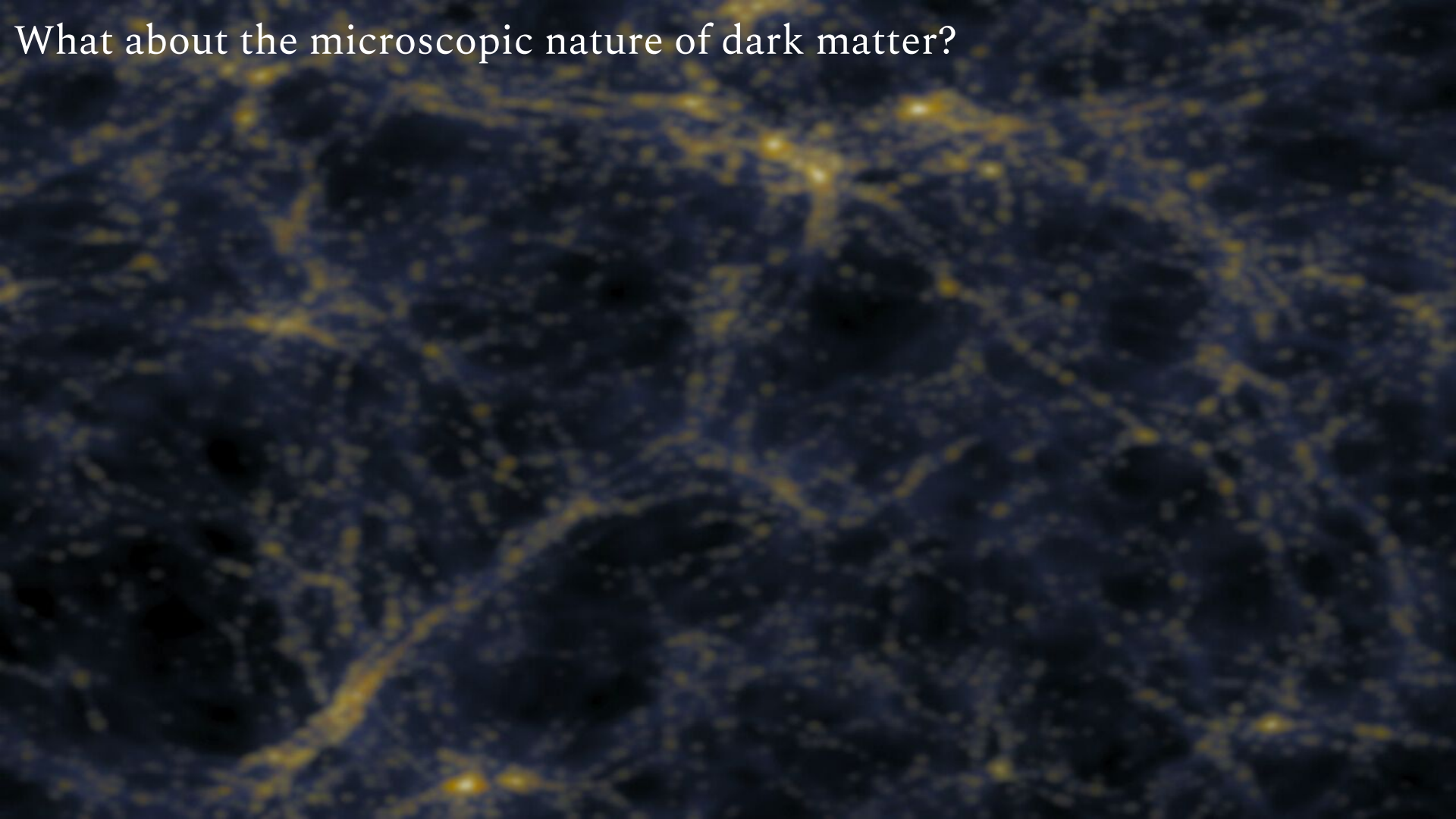


What other evidence is found in nature?

- Circular velocity curves
- Dispersion velocity curves
- Gravitational lensing
- Galaxy clusters
- *Bullet cluster*
- Lyman α forest
- Structure formation

Astronomy can help us understand more about dark matter!

What about the microscopic nature of dark matter?



What about the microscopic nature of dark matter?

We have a plethora of different dark matter models to try



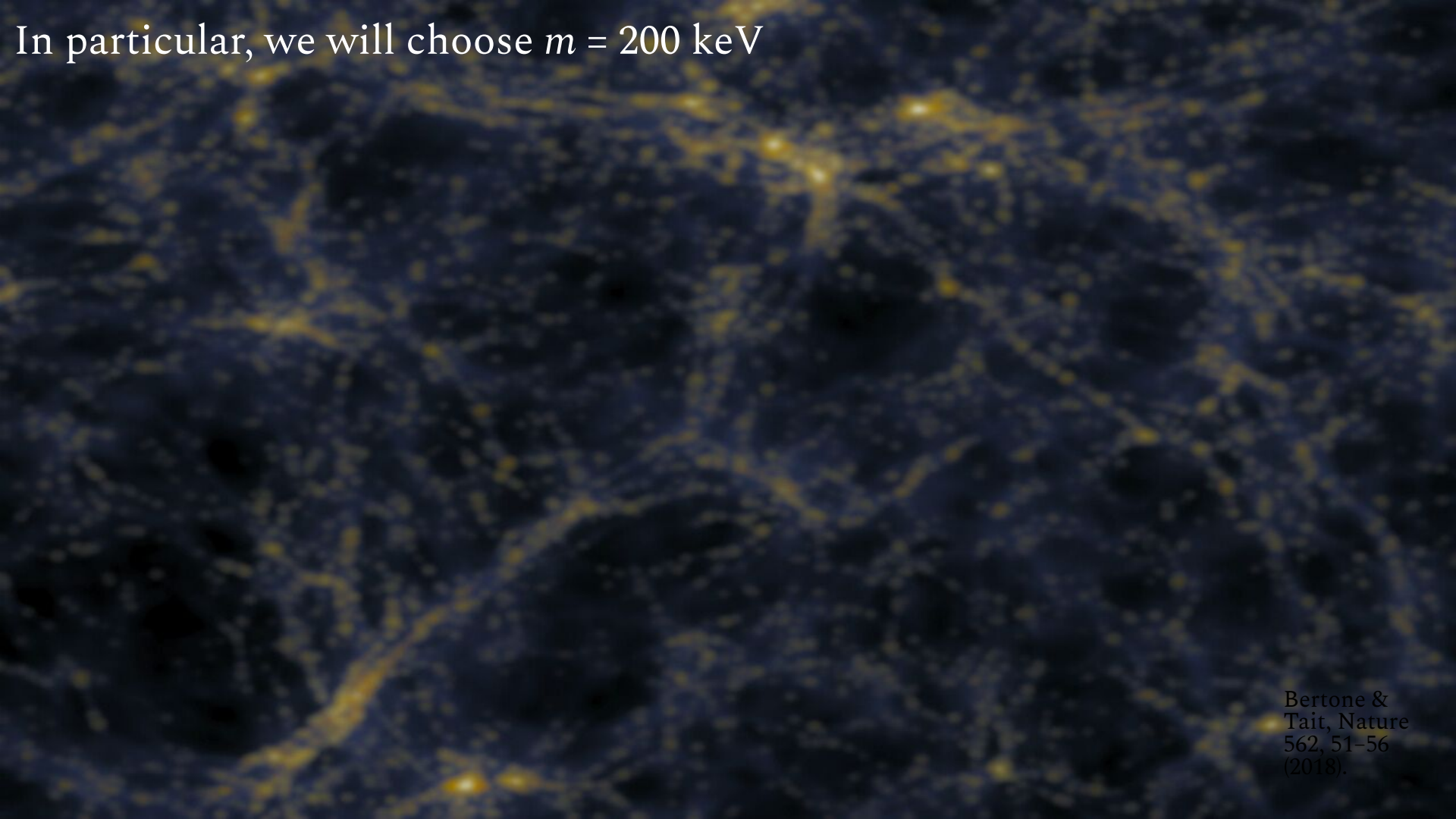
What about the microscopic nature of dark matter?

We have a plethora of different dark matter models to try

We will adopt as DM candidate a *right-handed neutrino* of mass of order keV



In particular, we will choose $m = 200$ keV



Bertone &
Tait, Nature
562, 51–56
(2018).

In particular, we will choose $m = 200$ keV

- This value is according to beyond Λ CDM theories (light DM)

In particular, we will choose $m = 200$ keV

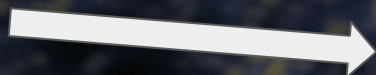
- This value is according to beyond Λ CDM theories (light DM)
- And is a suitable candidate to be the fermion of a successful fermionic dark matter *core-halo* model



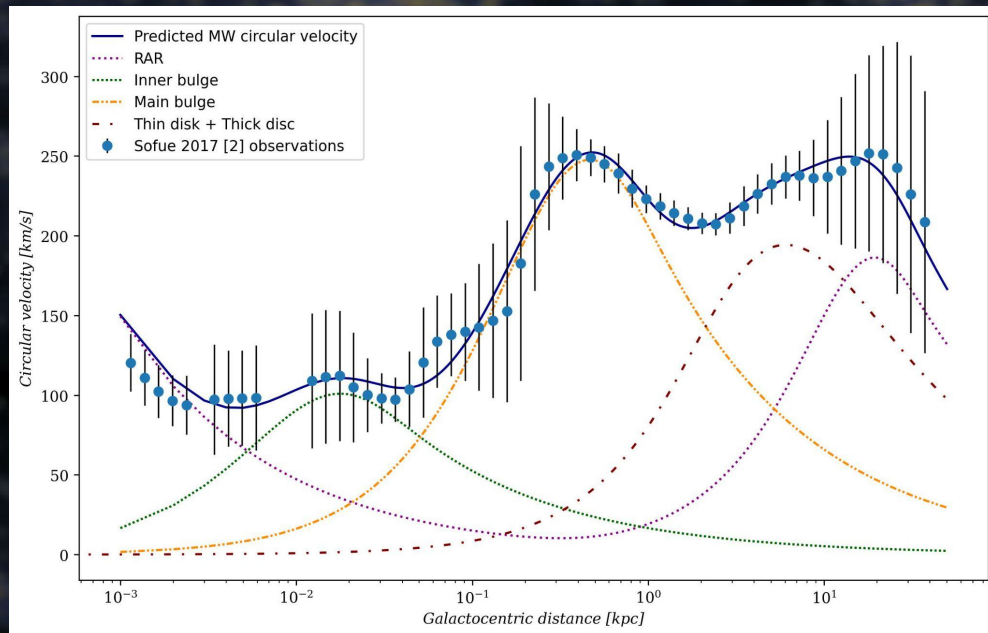
Argüelles et al 2018,
PDU, 21, 82-89

In particular, we will choose $m = 200$ keV

- This value is according to beyond LCDM theories (light DM)
- And is a suitable candidate to be the fermion of a successful fermionic dark matter *core-halo* model



Argüelles et al 2018,
PDU, 21, 82-89

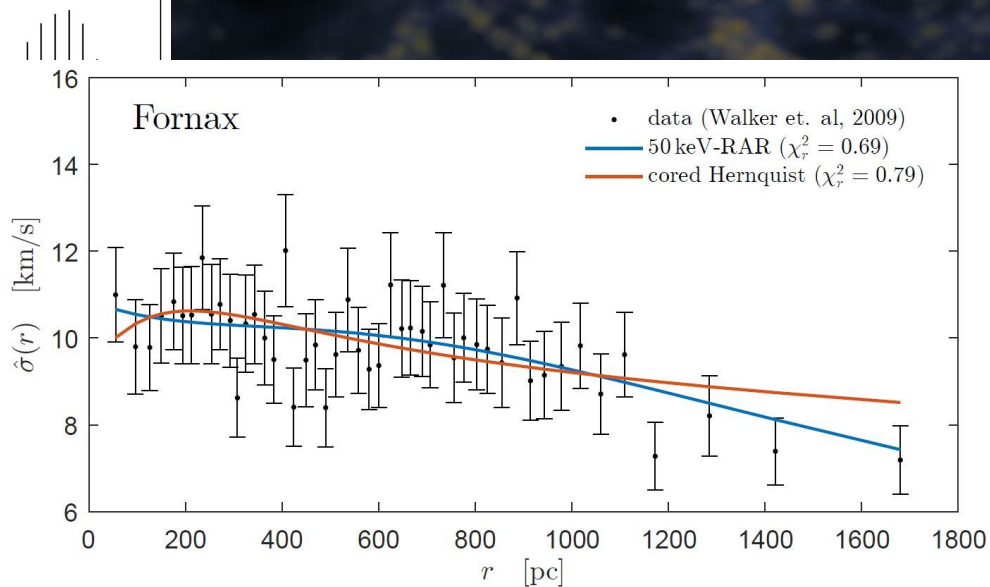
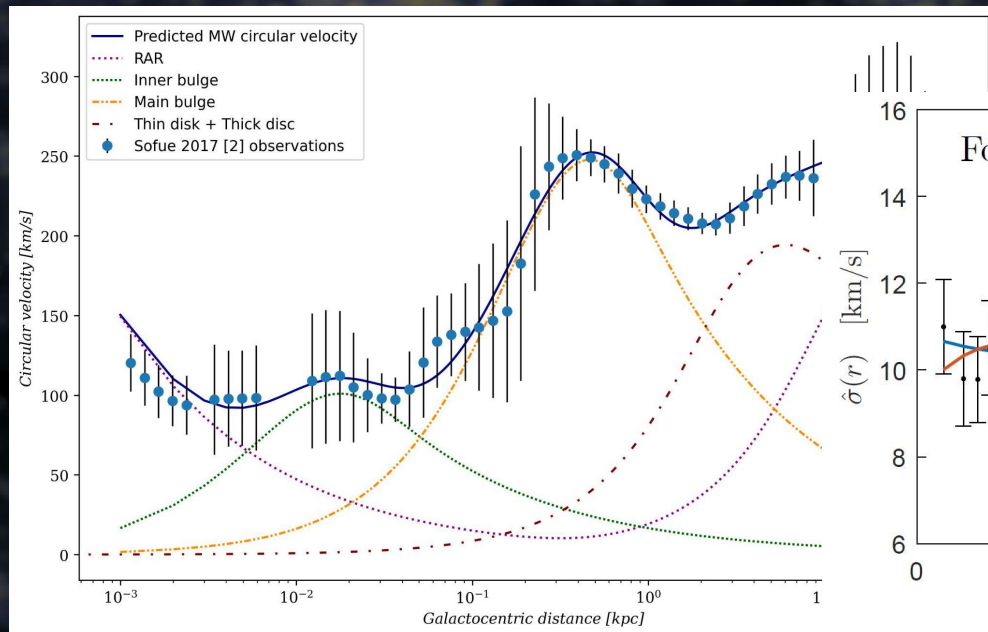


Bertone &
Tait, Nature
562, 51–56
(2018).

In particular, we will choose $m = 200$ keV

- This value is according to beyond LCDM theories (light DM)
- And is a suitable candidate to be the fermion of a successful fermionic dark matter *core-halo* model

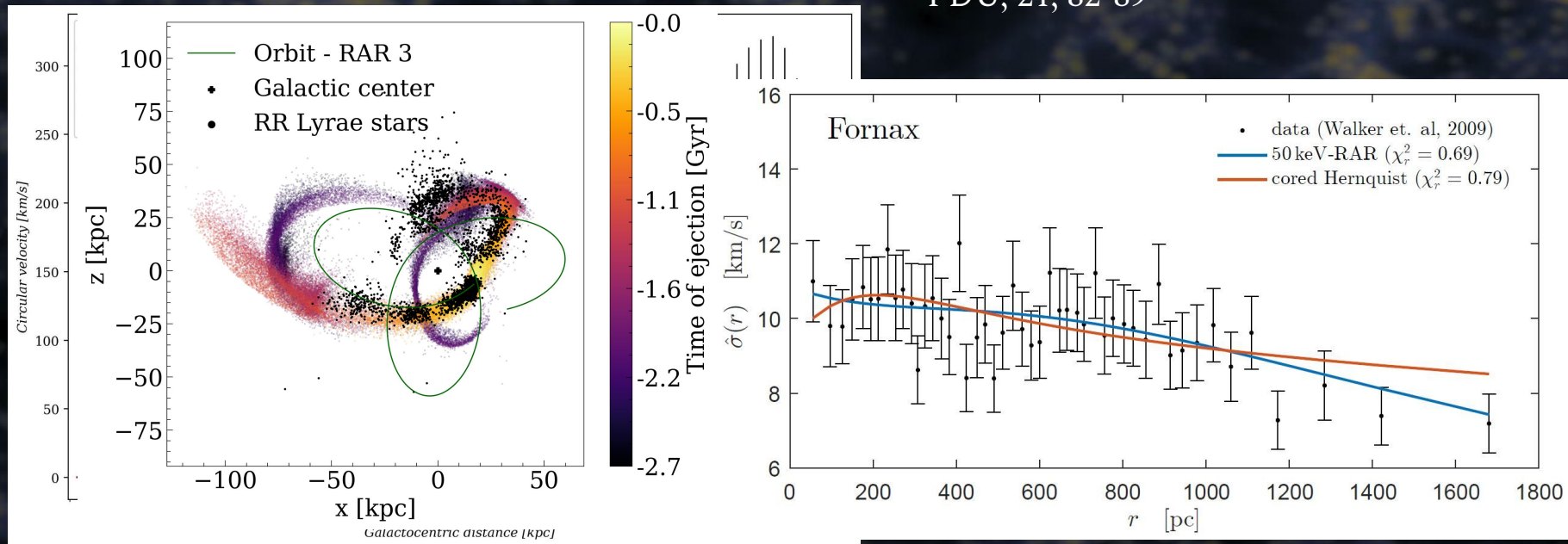
Argüelles et al 2018,
PDU, 21, 82-89



In particular, we will choose $m = 200$ keV

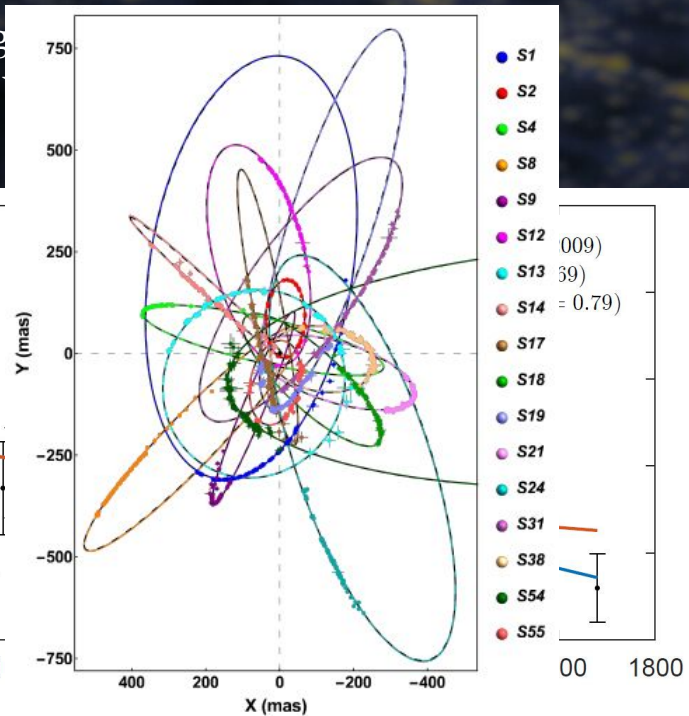
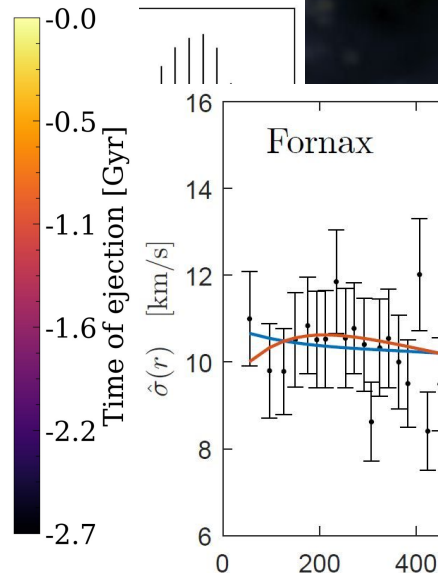
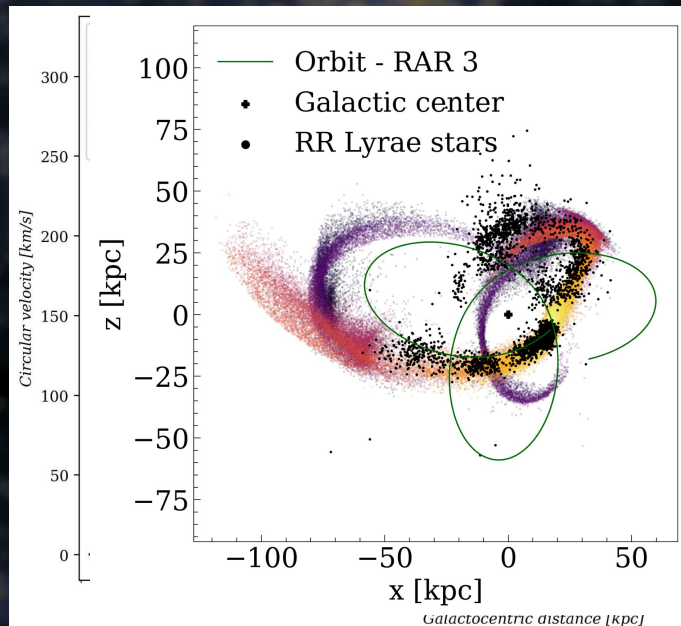
- This value is according to beyond LCDM theories (light DM)
- And is a suitable candidate to be the fermion of a successful fermionic dark matter *core-halo* model

Argüelles et al 2018,
PDU, 21, 82-89



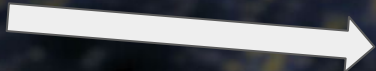
In particular, we will choose $m = 200$ keV

- This value is according to beyond LCDM theories (light DM)
- And is a suitable candidate to be the fermion of a successful fermionic dark matter *core-halo* model

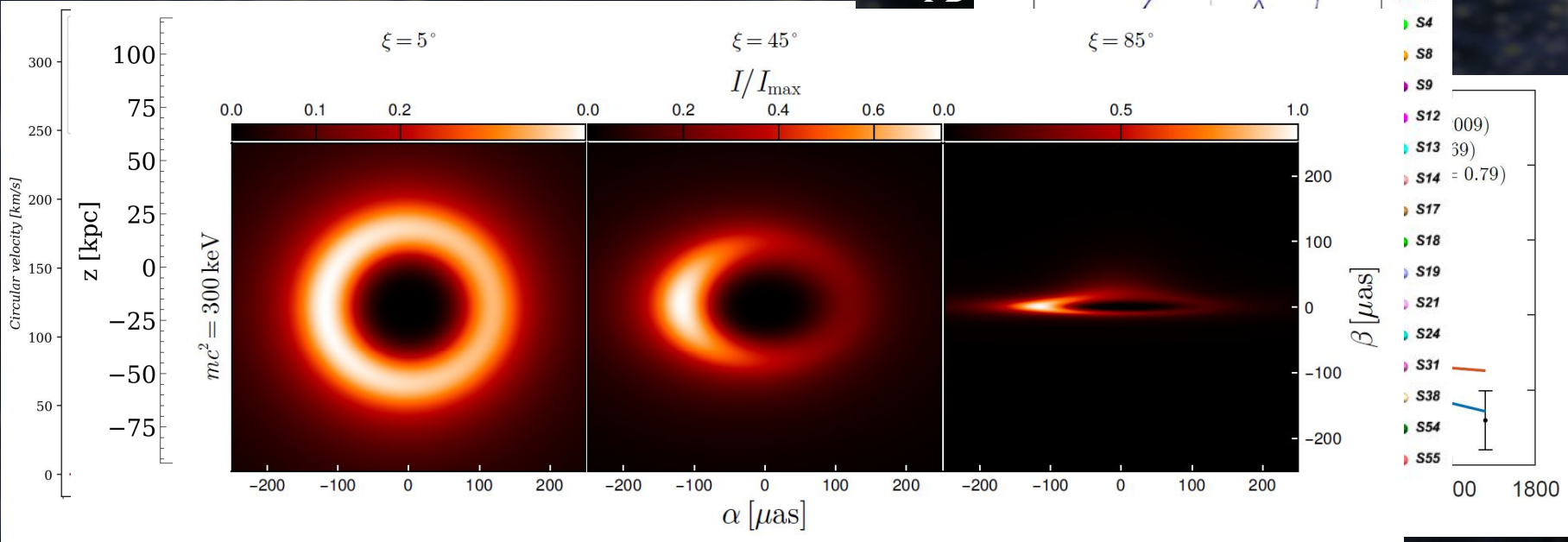
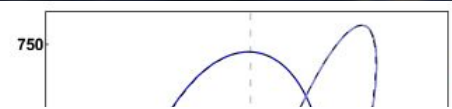


In particular, we will choose $m = 200$ keV

- This value is according to beyond LCDM theories (light DM)
- And is a suitable candidate to be the fermion of a successful fermionic dark matter *core-halo* model

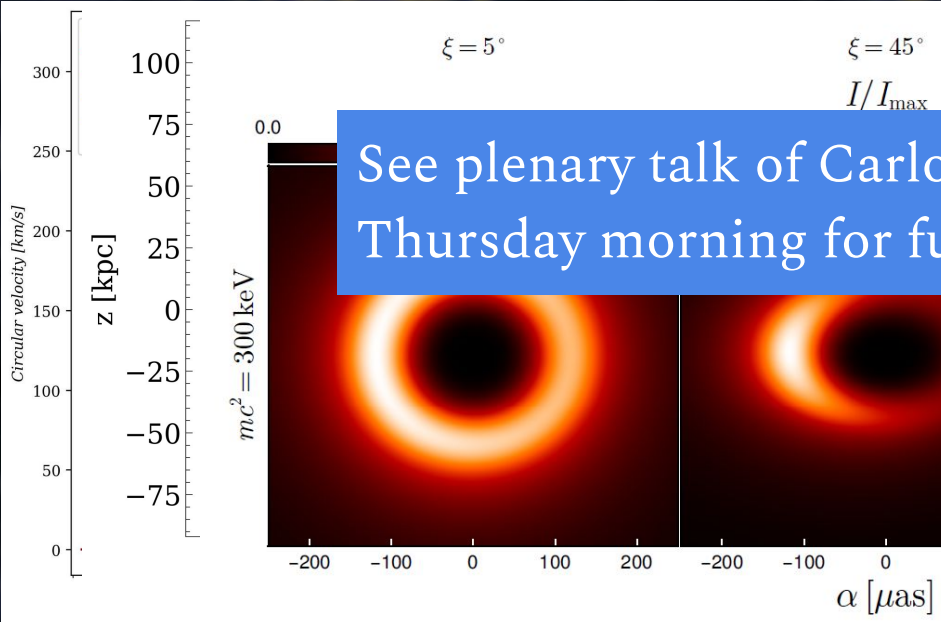
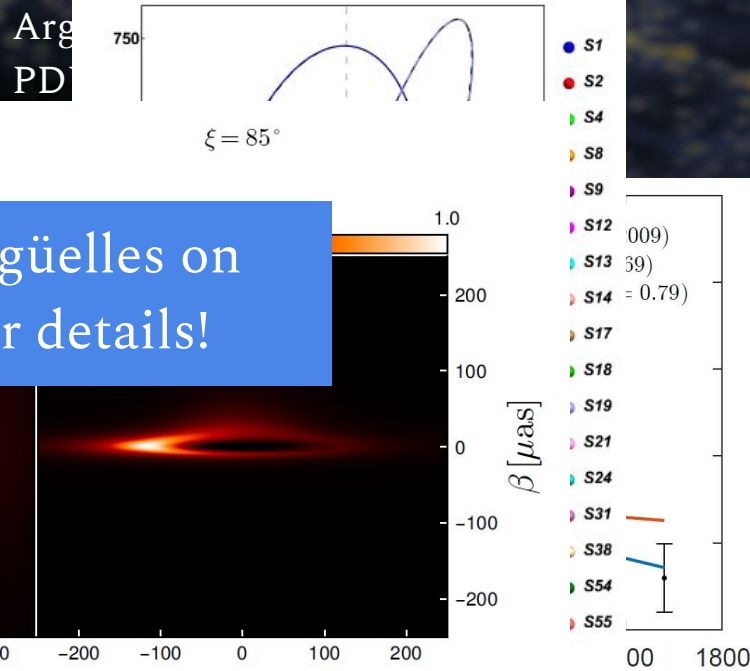


Arg
PD



In particular, we will choose $m = 200$ keV

- This value is according to beyond LCDM theories (light DM)
- And is a suitable candidate to be the fermion of a successful fermionic dark matter *core-halo* model

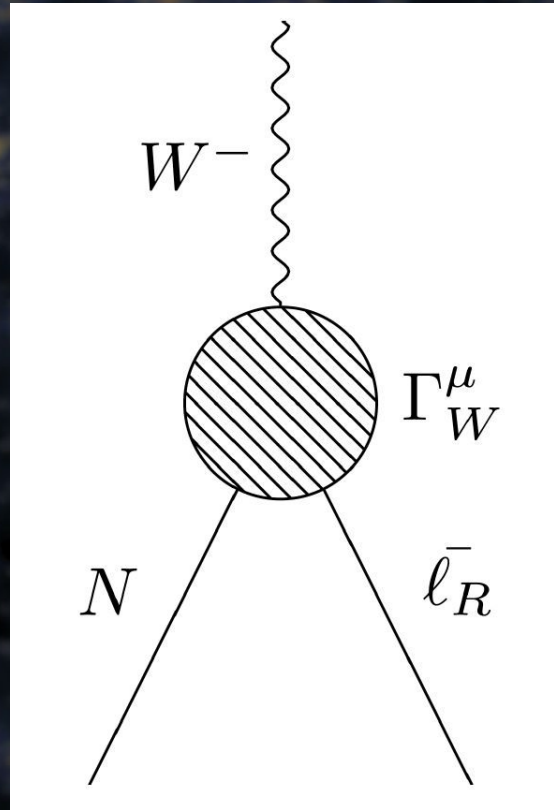


See plenary talk of Carlos Argüelles on Thursday morning for further details!

The model is in the IR domain of a *four-fermion* interaction of NJL type
(Nambu & Jona-Lasinio 1961, Phys. Rev. 124, 246)

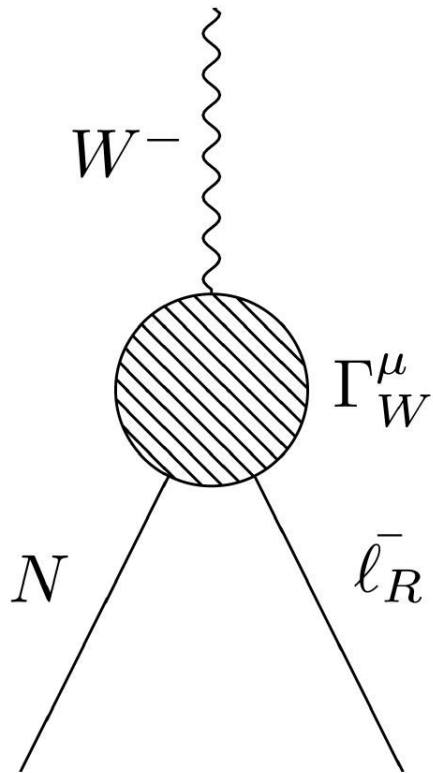


The model is in the IR domain of a *four-fermion* interaction of NJL type
(Nambu & Jona-Lasinio 1961, Phys. Rev. 124, 246)



← This induces

The model is in the IR domain of a *four-fermion* interaction of NJL type
 (Nambu & Jona-Lasinio 1961, Phys. Rev. 124, 246)



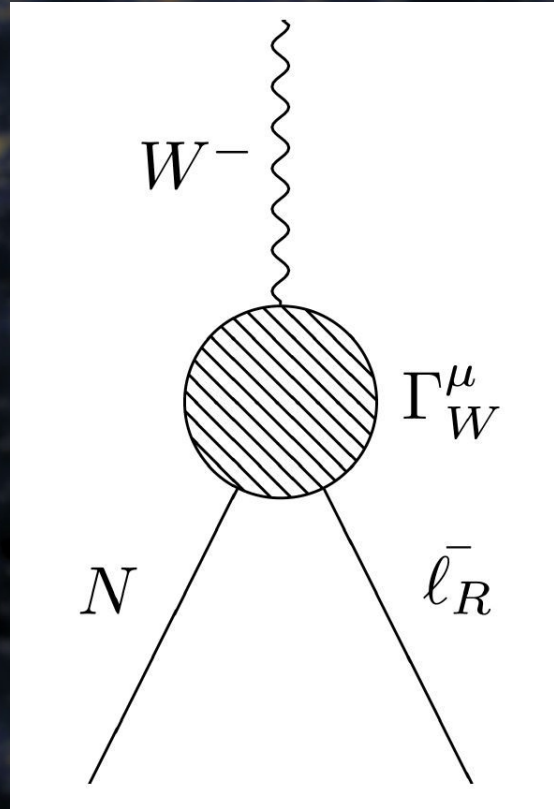
This induces

Which
 corresponds to



$$\mathcal{L} \supset \mathcal{G}_R \left(g_w / \sqrt{2} \right) \left[(U_R^l)^\dagger U_R^\nu \right]^{ll'} \bar{l}_R \gamma^\mu N_R^{l'} W_\mu^- + \text{h.c.}$$

The model is in the IR domain of a *four-fermion* interaction of NJL type
 (Nambu & Jona-Lasinio 1961, Phys. Rev. 124, 246)



← This induces

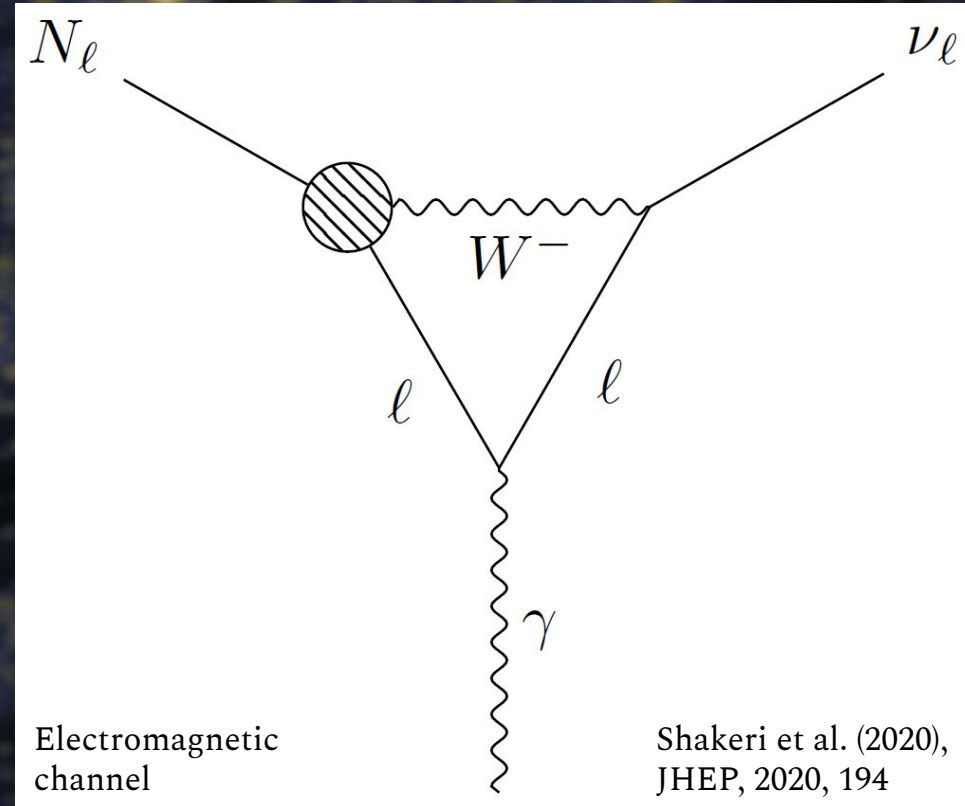
Which corresponds to ↓

But at tree level, right-handed neutrino electron interaction using this coupling is not dominant



$$\mathcal{L} \supset \mathcal{G}_R \left(g_w / \sqrt{2} \right) \left[(U_R^l)^\dagger U_R^\nu \right]^{ll'} \bar{l}_R \gamma^\mu N_R^{l'} W_\mu^- + \text{h.c.}$$

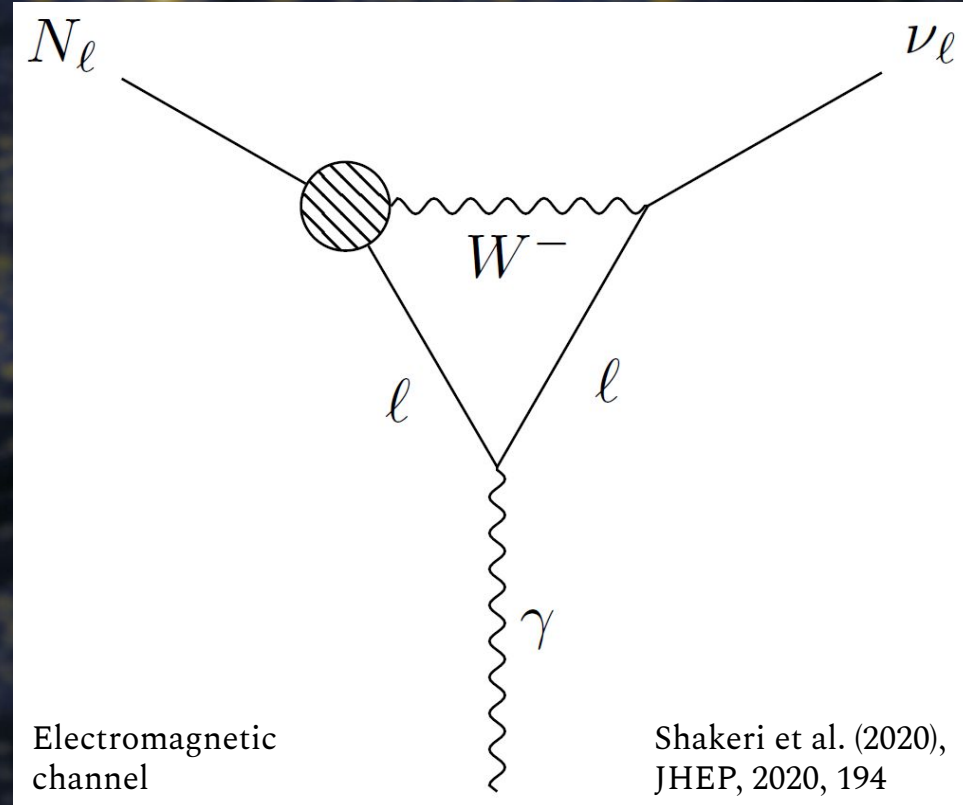
The right-handed neutrinos N can radiatively decay into a left-handed SM neutrino ν and a photon γ .



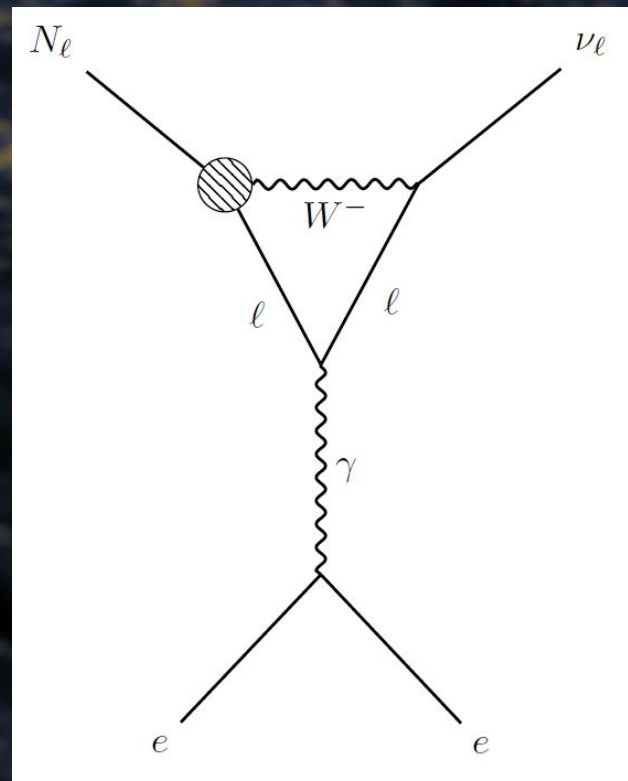
The right-handed neutrinos N can radiatively decay into a left-handed SM neutrino ν and a photon γ .

This vertex is represented as
an effective operator

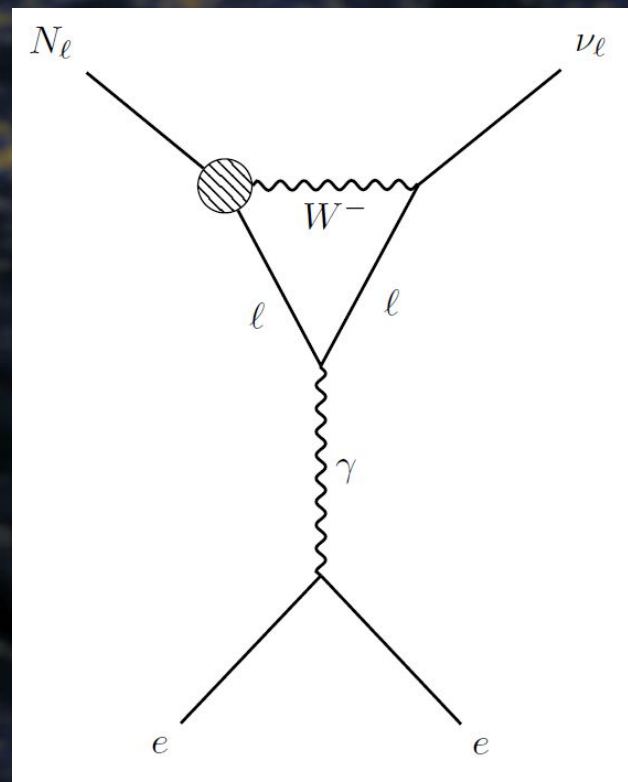
$$\hat{\mathcal{O}} = \left(U_L^\nu U_L^\ell \right)^{ll'} \bar{\nu}_L^l \Lambda_{\nu'}^\mu N_R^{l'} A_\mu + \text{h.c.}$$



Hence, the interaction between a right-handed neutrino and a bounded electron on an atom of the detector will be described by



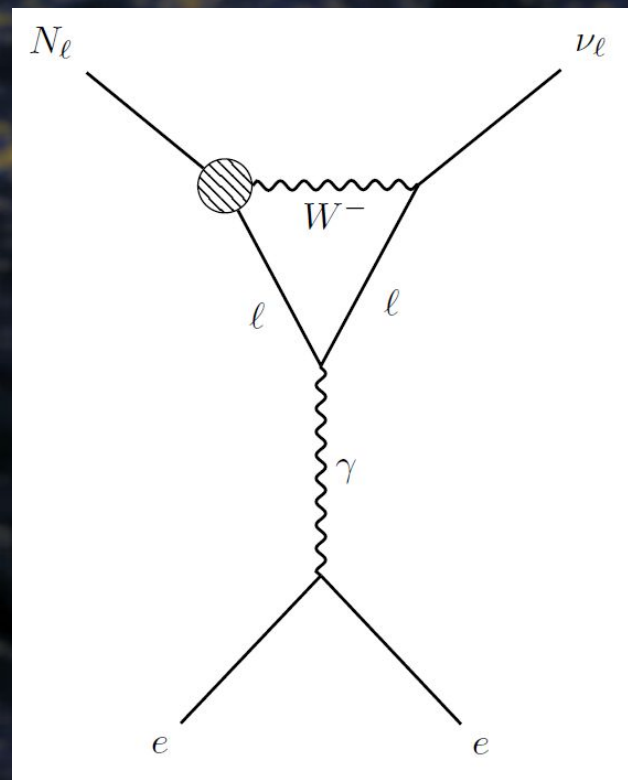
Hence, the interaction between a right-handed neutrino and a bounded electron on an atom of the detector will be described by



Interaction Lagrangian

$$\mathcal{L}_{\text{eff}} = -2\sqrt{2}G_F \left([\bar{N}_e \gamma^\mu \mathcal{G}_R P_R u_e] [\bar{u}_e \gamma_\mu P_L \nu_e] \right)$$

Hence, the interaction between a right-handed neutrino and a bounded electron on an atom of the detector will be described by

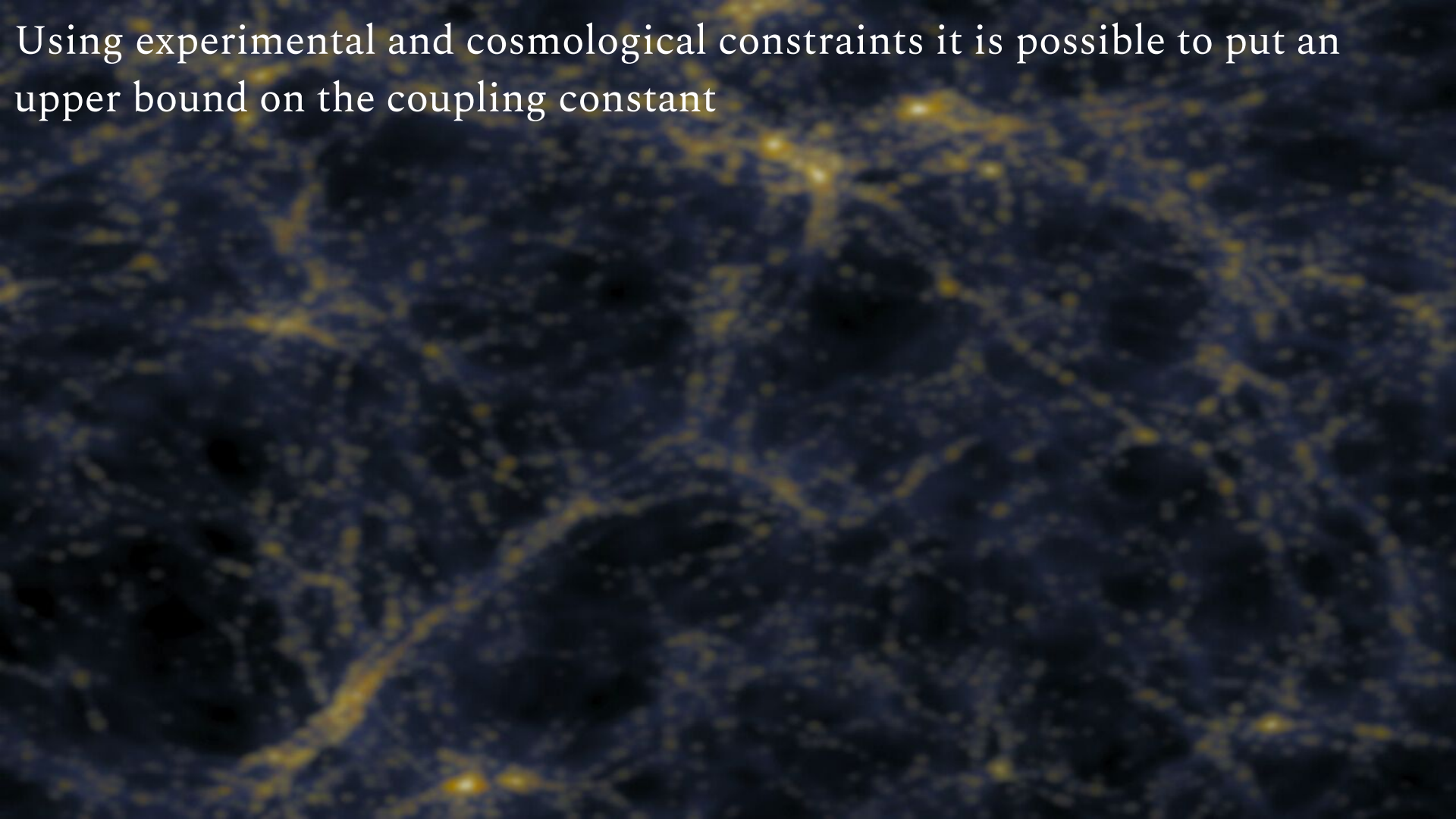


The squared matrix element is given by

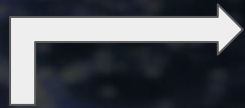
$$|M|^2(E_R, q^2, v) = \left(\frac{4m_l^2}{q^4} \right) \left(\frac{\alpha^2 g_w^4 \mathcal{G}_R^2}{16\pi^2} \right) (2m_\chi m_\nu + 2m_e E_R + m_\chi^2) \\ \left\{ (2C_1 + C_0)^2 [m_e (2m_e E_\chi + m_\chi^2) (E_\chi - E_R)] + \right. \\ \left. + (2C_2 + C_0)^2 [m_e (2m_\chi E_R + m_\chi^2) (E_\chi - E_R)] + \right. \\ \left. + (2C_1 + C_0) (2C_2 + C_0) [2m_e^2 (E_\chi^2 + E_R^2 - 2E_\chi E_R) + m_e m_\chi^2 (E_\chi - E_R)] \right\}$$

$$q^2 = q_\mu q^\mu$$

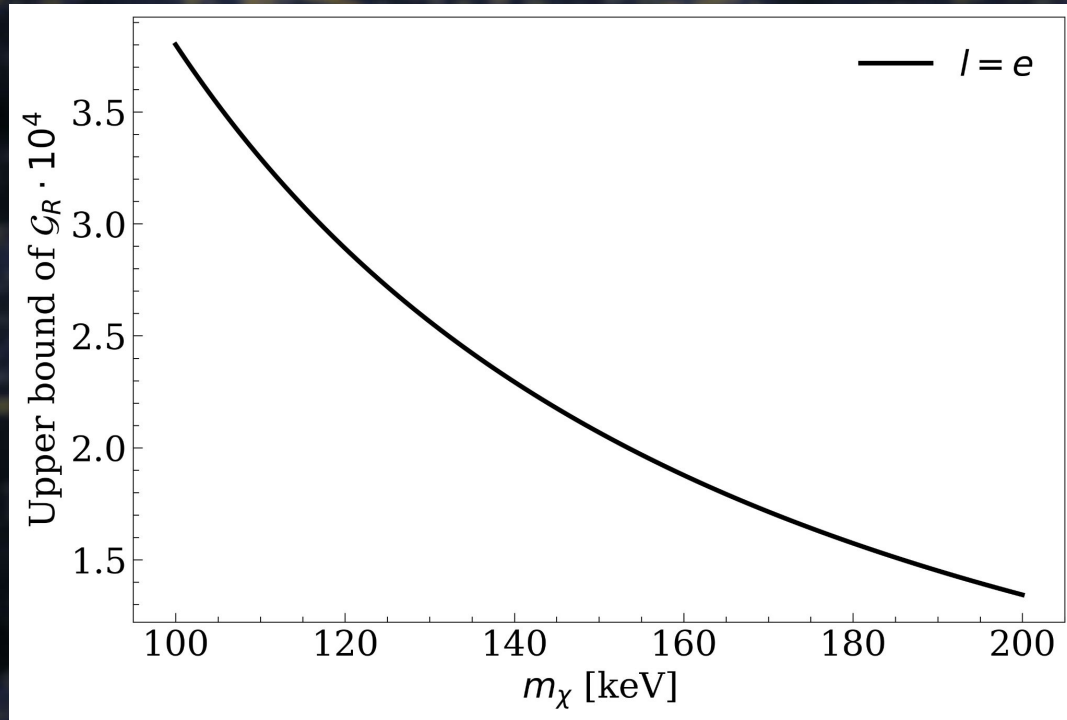
Using experimental and cosmological constraints it is possible to put an upper bound on the coupling constant



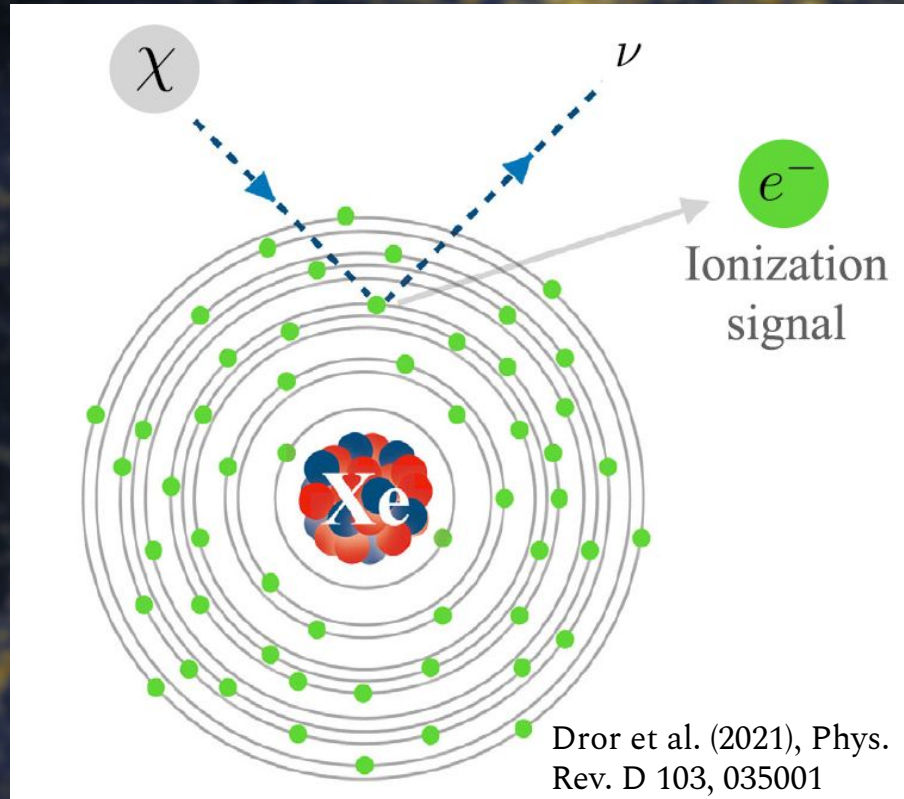
Using experimental and cosmological constraints it is possible to put an upper bound on the coupling constant



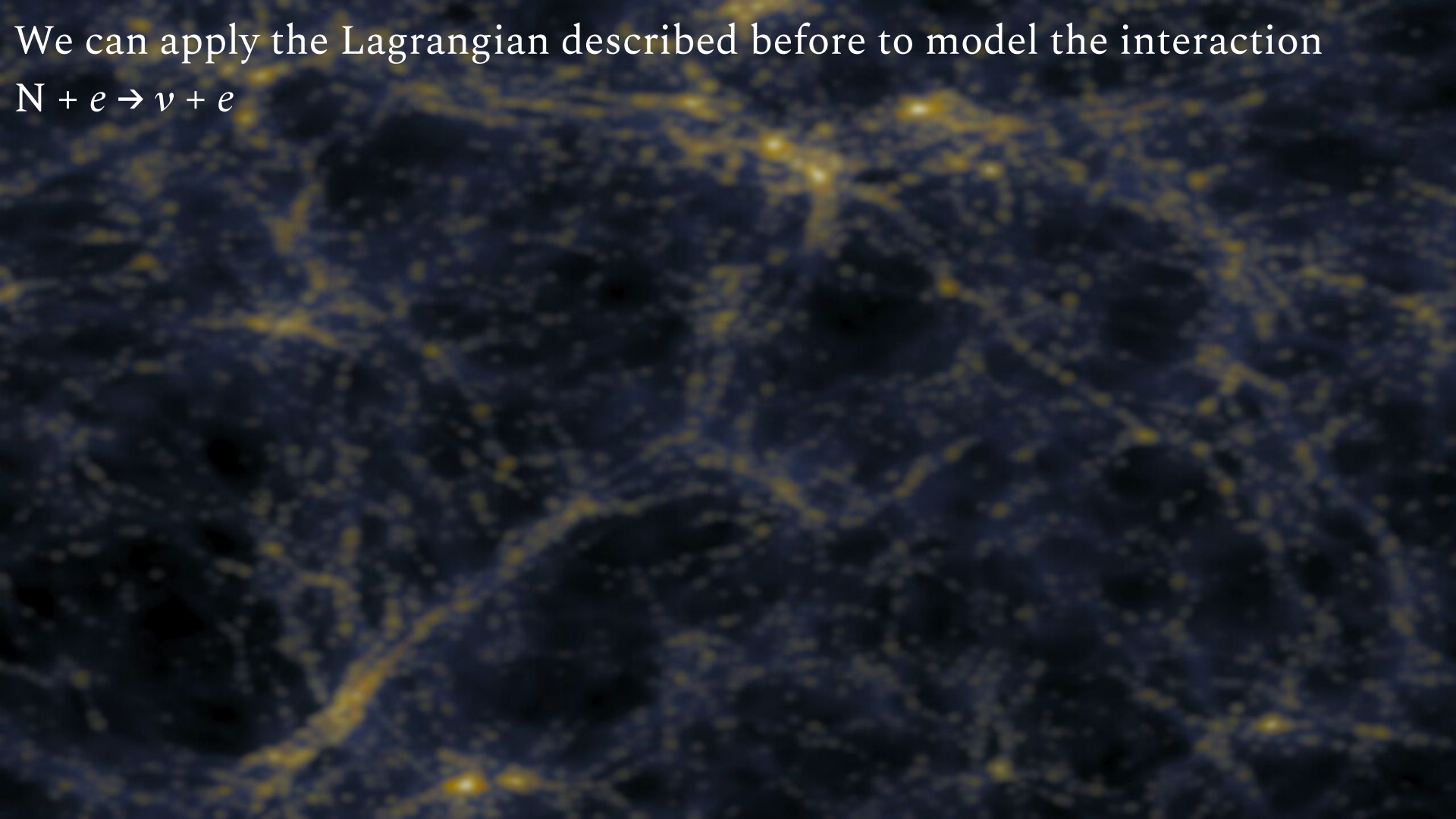
$$\mathcal{G}_R \lesssim 3.8 \cdot 10^{-4} \left(\frac{511 \text{ keV}}{m_e} \right) \left(\frac{100 \text{ keV}}{m_\chi^e} \right)^{3/2}$$



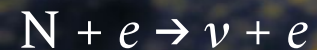
We want to study the ionization of atoms due to right-handed neutrino electron interactions



We can apply the Lagrangian described before to model the interaction

$$N + e \rightarrow \nu + e$$
A Cosmic Microwave Background (CMB) fluctuation map showing temperature variations across the sky. The map is predominantly dark blue, with numerous bright yellow and orange spots and streaks representing temperature fluctuations. The pattern is complex and non-uniform, characteristic of the CMB's anisotropy.

We can apply the Lagrangian described before to model the interaction

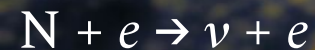


The direct interaction ionizes the atom.
This constitutes an event and will allow the
events rate to be defined.



$$\frac{dR_{\text{ion}}^{nl}}{dE_R} = \frac{\rho_\chi}{128\pi m_\chi^3 m_e^2} \int dq \frac{q}{E_R} \eta(v_{\text{min}}(q, E_R)) |M(q^2)|^2 |f_{\text{ion}}^{nl}(E_R, q)|^2$$

We can apply the Lagrangian described before to model the interaction



The direct interaction ionizes the atom.
This constitutes an event and will allow the
events rate to be defined.



$$\frac{dR_{\text{ion}}^{nl}}{dE_R} = \frac{\rho_\chi}{128\pi m_\chi^3 m_e^2} \int dq \frac{q}{E_R} \eta(v_{\text{min}}(q, E_R)) |M(q^2)|^2 |f_{\text{ion}}^{nl}(E_R, q)|^2$$



Under the assumption $mv \ll q$

$$\frac{dR_{\text{ion}}^{nl}}{dE_R} = \frac{\rho_\chi}{64\pi m_\chi^2 m_e^2} \frac{q}{E_R} |f_{\text{ion}}^{nl}(k', q)|^2 |M(q^2)|^2.$$

Where q yields

$$q = m_\chi + E_B^{nl} - E_R$$

Ionization form factor:


$$|f_{\text{ion}}^{nl}(k', q)|^2 = \frac{4k'^3}{(2\pi)^3} \sum_{l'=0}^{\infty} \sum_{L=|l-l'|}^{l+l'} (2l+1)(2l'+1)(2L+1) \begin{bmatrix} l & l' & L \\ 0 & 0 & 0 \end{bmatrix} \left| \int dr r^2 R_{k'l'}(r) R_{nl}(r) j_L(qr) \right|^2$$

It is related with the quantum mechanics of the atom


Ionization form factor:

$$|f_{\text{ion}}^{nl}(k', q)|^2 = \frac{4k'^3}{(2\pi)^3} \sum_{l'=0}^{\infty} \sum_{L=|l-l'|}^{l+l'} (2l+1)(2l'+1)(2L+1) \begin{bmatrix} l & l' & L \\ 0 & 0 & 0 \end{bmatrix} \left| \int dr r^2 R_{k'l'}(r) R_{nl}(r) j_L(qr) \right|^2$$

It is related with the quantum mechanics of the atom



Outgoing electron
radial wavefunction



Bounded electron
radial wavefunction

Ionization form factor:

$$|f_{\text{ion}}^{nl}(k', q)|^2 = \frac{4k'^3}{(2\pi)^3} \sum_{l'=0}^{\infty} \sum_{L=|l-l'|}^{l+l'} (2l+1)(2l'+1)(2L+1) \begin{bmatrix} l & l' & L \\ 0 & 0 & 0 \end{bmatrix} \left| \int dr r^2 R_{k'l'}(r) R_{nl}(r) j_L(qr) \right|^2$$

It is related with the quantum mechanics of the atom



It does not depend on the nature of the scattering process



Outgoing electron radial wavefunction



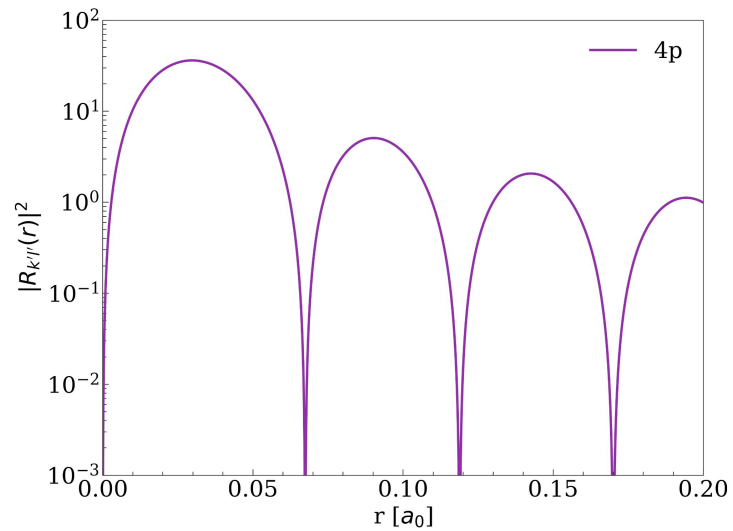
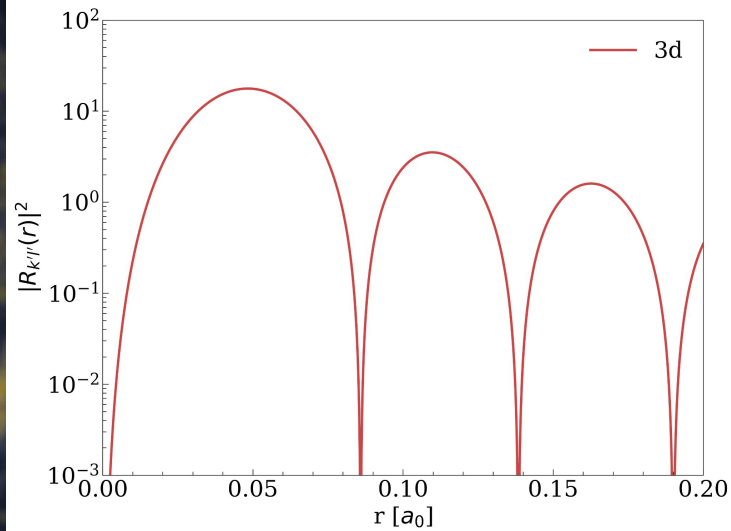
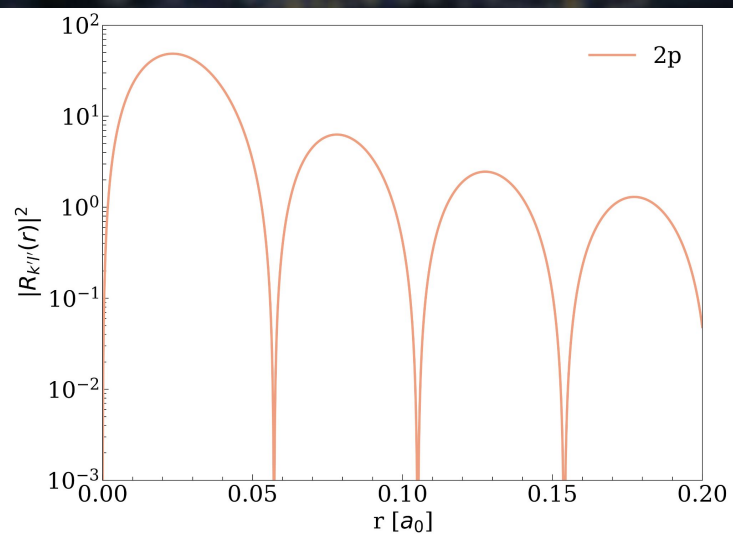
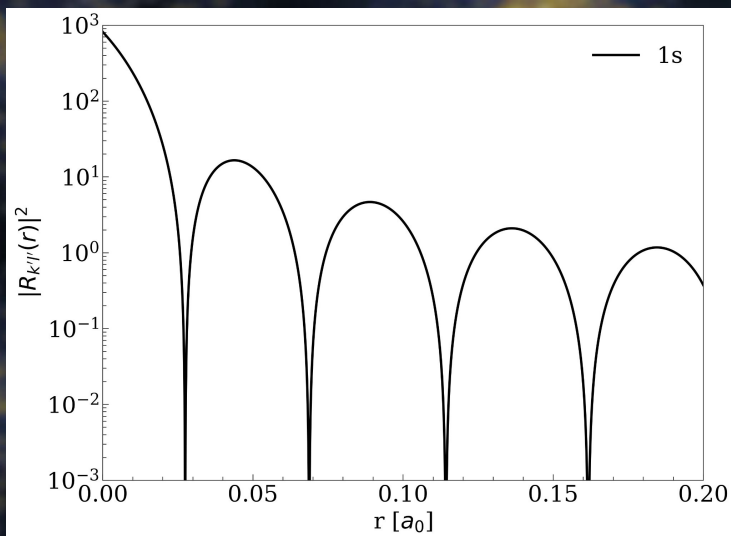
Bounded electron radial wavefunction

Outgoing radial wavefunctions

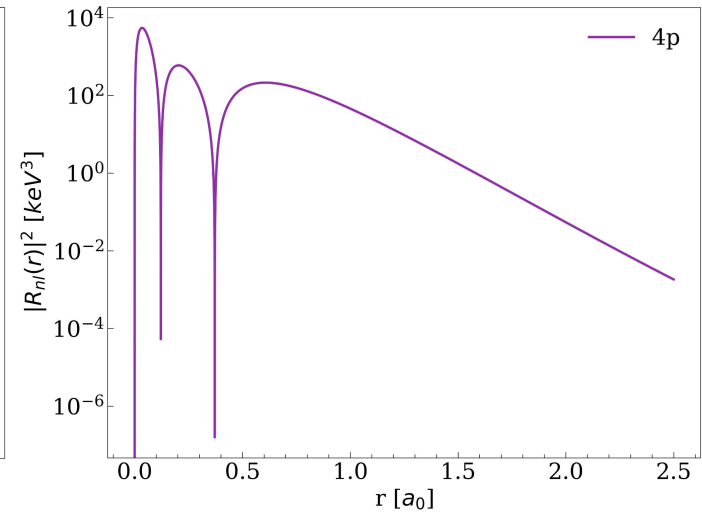
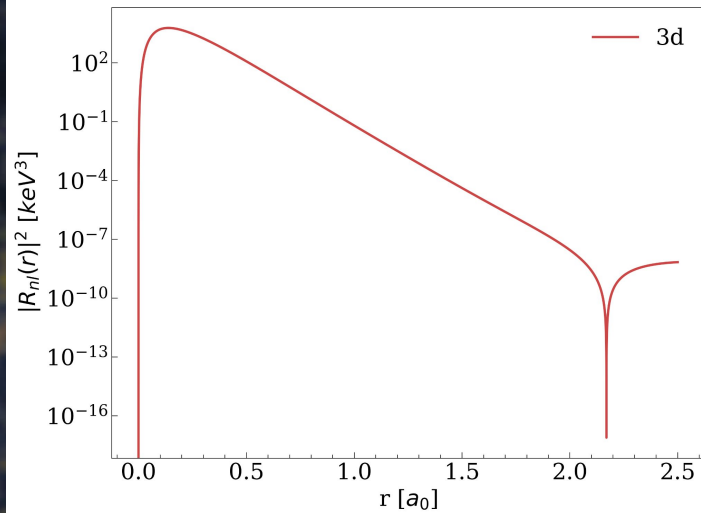
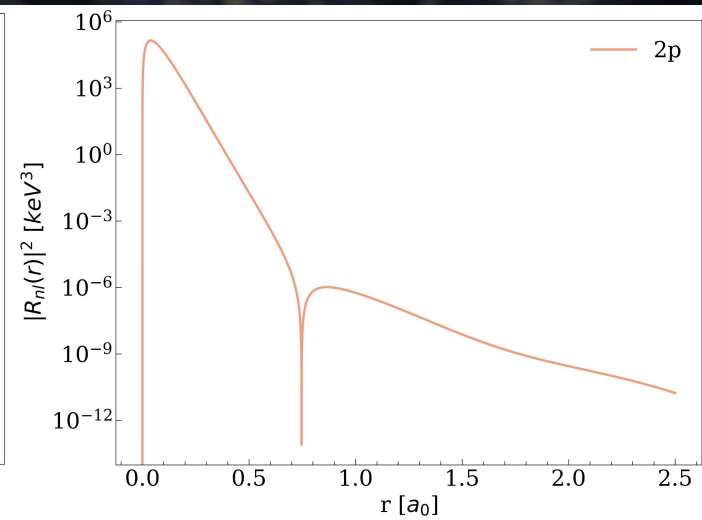
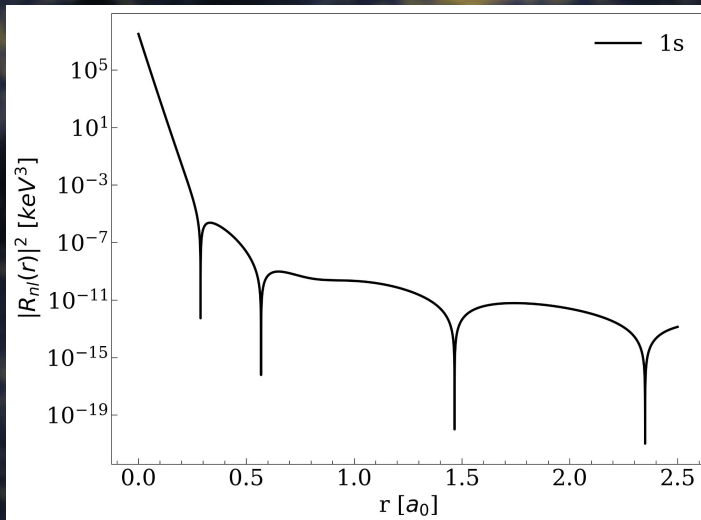
$k' = 50 \text{ keV}$

$l' = l$

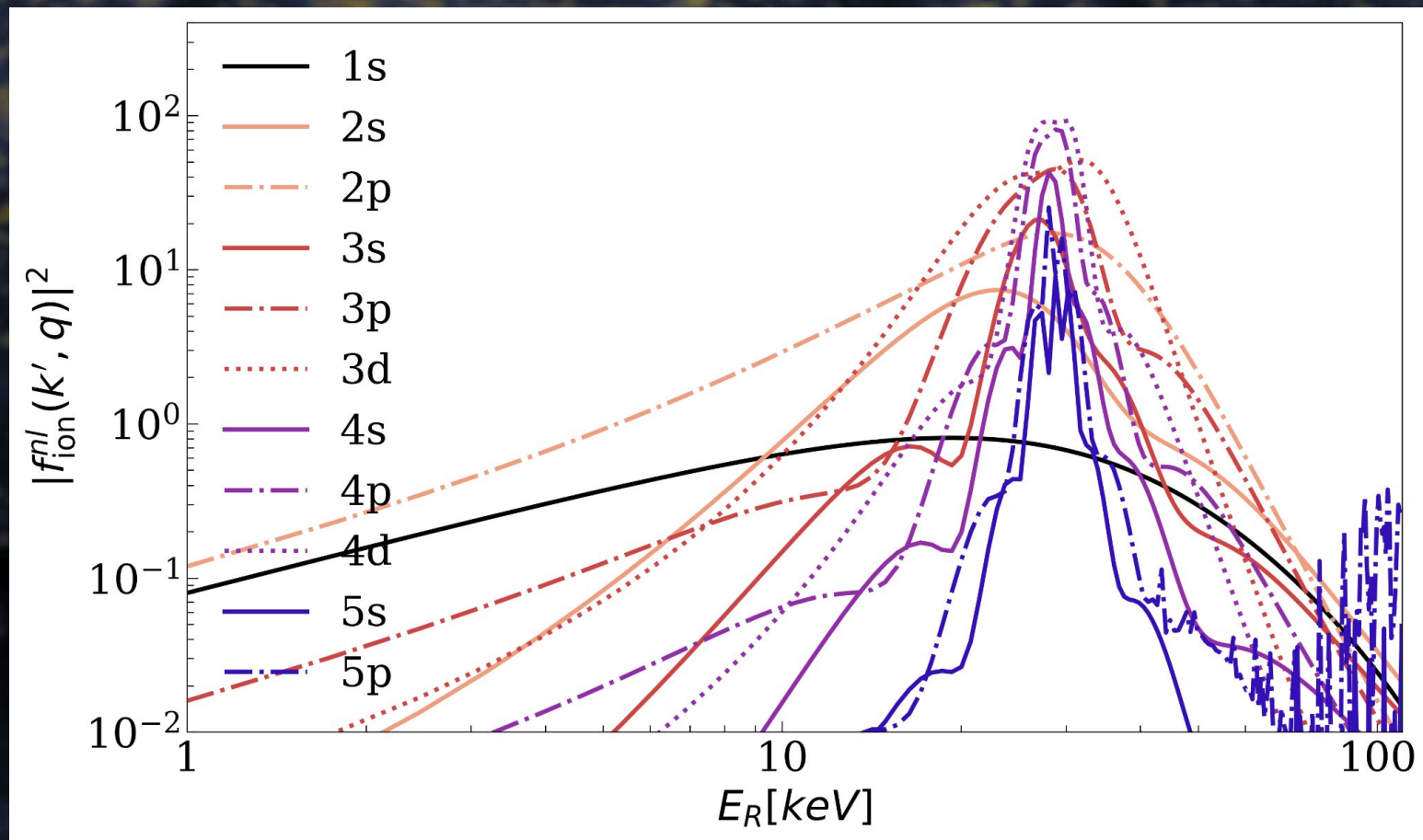
$m = 200 \text{ keV}$



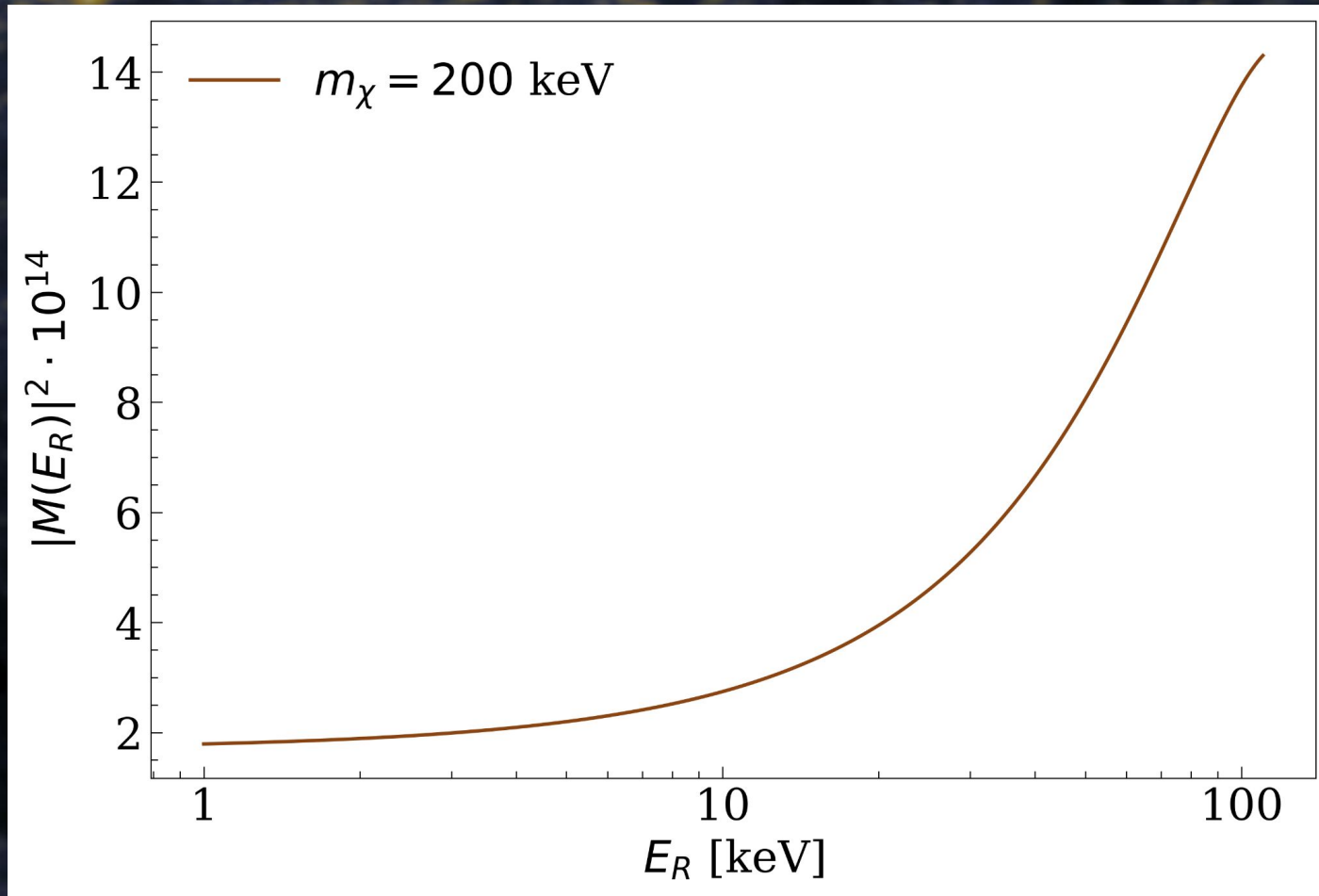
Bounded radial wavefunctions



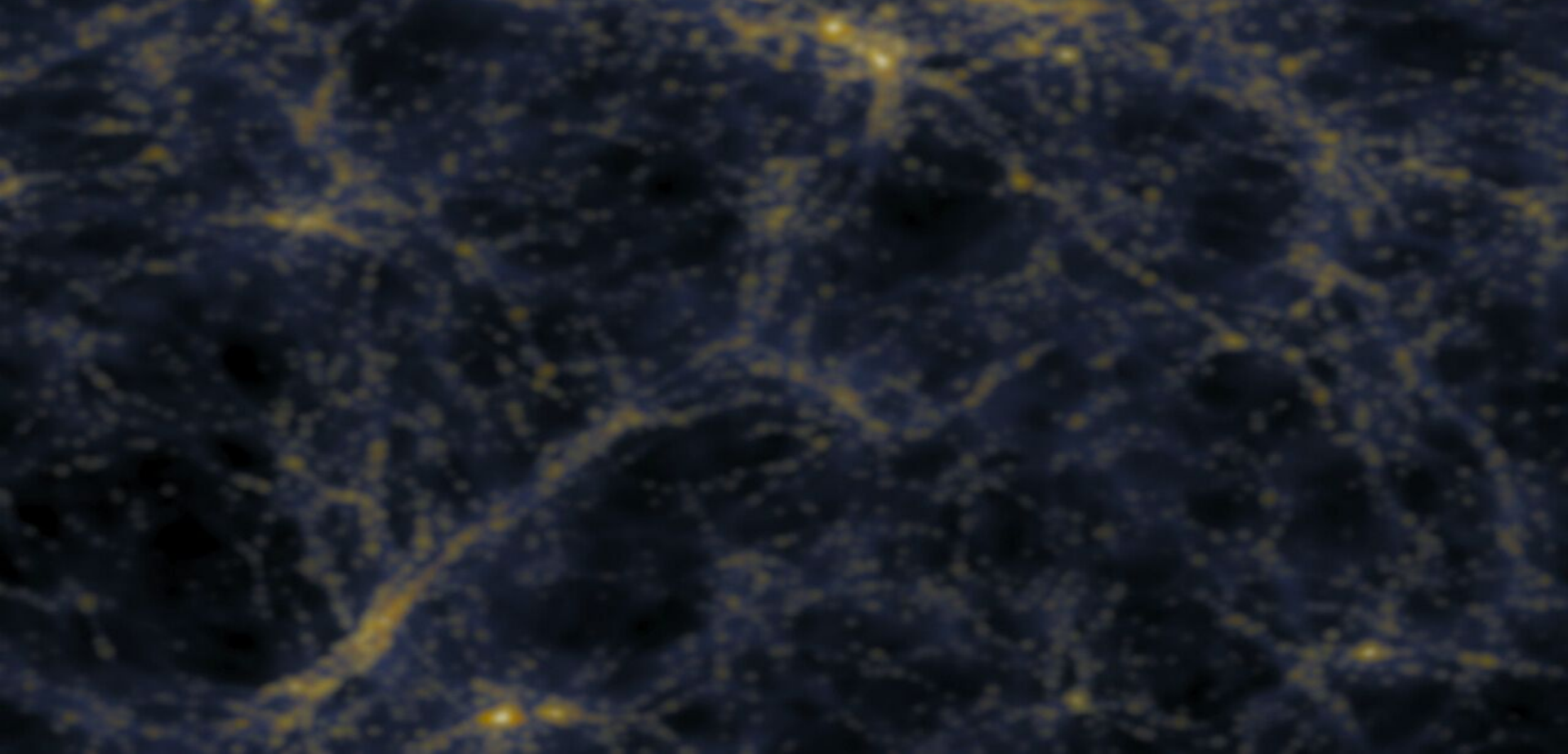
Ionization form factor



Squared matrix element



When the events rate for each shell is computed, it is possible to calculate the *total events rate*

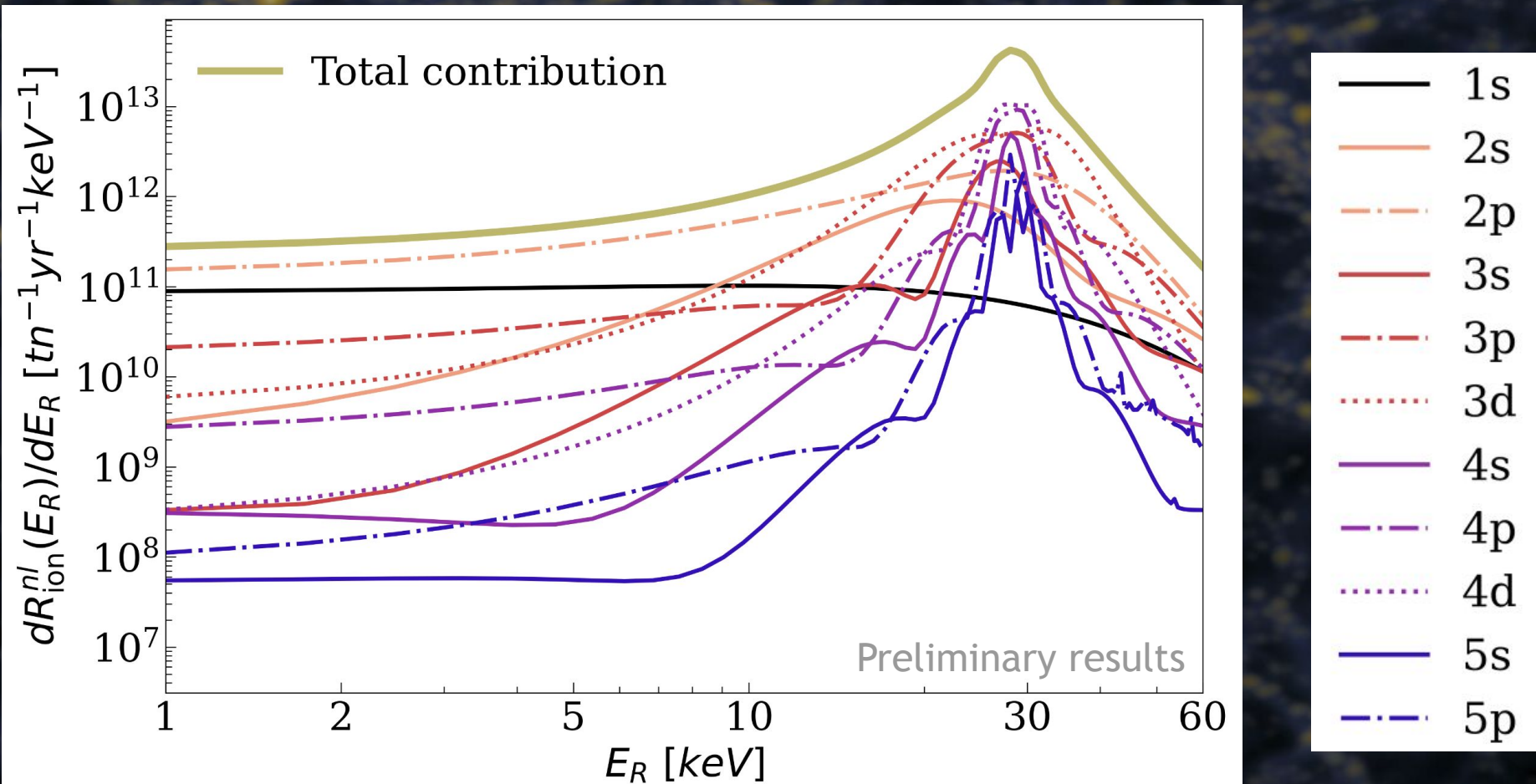


When the events rate for each shell is computed, it is possible to calculate the *total events rate*

$$\frac{dR_{\text{ion}}}{dE_R} = CN_T \sum_{nl} \frac{dR_{\text{ion}}^{nl}}{dE_R}$$

Due to the separate nature of the quantum mechanics and scattering process, each events rate will reflect the behaviour of the ionization form factor

Individual and total differential events rate



Conclusions:

- We used the radiative 1 loop decay of a right-handed neutrino as an effective vertex to study DM- e inelastic scattering processes.
- We defined a theoretical framework that allow us to compute an observable quantity.
- We developed numerical methods to compute theoretical events rate.

Conclusions:

- We used the radiative 1 loop decay of a right-handed neutrino as an effective vertex to study DM- e inelastic scattering processes.
- We defined a theoretical framework that allow us to compute an observable quantity.
- We developed numerical methods to compute theoretical events rate.

Future work:

- To use the efficiencies of different DM detectors to compute the predicted events rate.
- To compute experimental limits on \mathcal{G}_r vs. m plot.